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# Agility of spin Hall nano-oscillators

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We investigate the temporal response of constriction-based spin Hall nano-oscillators driven by pulsed stimuli using time-resolved Brillouin light scattering microscopy. Magnetization auto-oscillations, enabled by spin Hall effect and spin orbit torque, can be obtained using input voltage pulses of a few nanoseconds in duration. The combination of voltage and microwave pulses allows to generate auto-oscillation signals with multi-level amplitude and frequency in the time-domain. Our findings suggest that the lead time of processes such as synchronization and logic using spin Hall nano-oscillators can be reduced to the nanosecond time-scale.

## I. INTRODUCTION

Magnetic oscillators are among the most promising means to perform brain inspired solid-state based computation [1, 2]. These are primarily based on magnetization auto-oscillations (AOs) in the gigahertz frequency range. AOs arise when the Gilbert damping is compensated by the torque transferred from a pure spin or spin polarised current to the magnetization, due to spin orbit torque (SOT) or spin transfer torque [3–7]. Here, the pure spin current is generated via spin Hall effect [8, 9], in an adjacent non-ferromagnetic, metallic layer with large spin Hall angle [10–12]. Over the recent years, two main prototypical oscillator geometries have surfaced: the spin Hall nano-oscillators (SHNO) [13–15] and the spin torque nano-oscillators [16, 17]. Often, these are physically arrayed into a network, when synchronisation between oscillators [18–20] allows for complex operations, such as pattern recognition [21, 22]. To some extent, an isolated magnetic oscillator in itself can mimic a pseudo-network of oscillators [23, 24] if external time-dependent stimuli are applied to exploit its nonlinear response. Thus, an important requisite for a magnetic oscillator is agility, that is, the ability to respond to time-dependent external stimuli in a way that the resulting amplitude, frequency or phase can be utilized reliably as a processing output.

In this manuscript, we investigate the temporal response of SHNOs driven by voltage pulses ( $V_p$ ) and microwave pulses ( $RF_p$ ). We found that AO signals can be generated using few-nanosecond wide voltage pulses. We discuss how the AO response can be improved by means of injection-locking to an external microwave pulse. Furthermore, we demonstrate how the pulsed operation results in a reliable multi-level AO amplitude and frequency in the time-domain.

## II. SHNO GEOMETRY AND METHODS

Figure 1(a) shows a top-view scanning electron microscopy (SEM) image of the SHNO. The two magnetic disks have a radius of 2.6  $\mu\text{m}$  and overlap by ap-

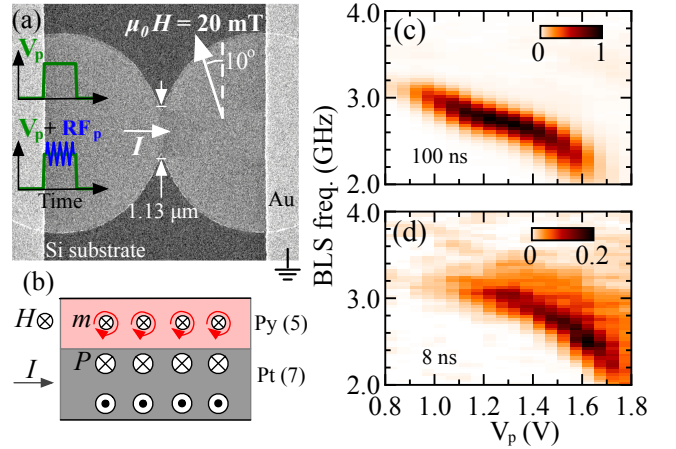


FIG. 1 (Color online). (a) SEM image of the SHNO and measurement geometry. (b) Schematic illustration of the layer stack, highlighting the direction of the current ( $I$ ), the polarisation of the pure spin current ( $P$ ) and the precession induced on the magnetic moment ( $m$ ) of the Py ( $\text{Ni}_{81}\text{Fe}_{19}$ ) layer. (c)-(d) BLS spectra for voltage pulses with durations of (c) 100 ns and (d) 8 ns.

proximately 50 nm, resulting in a constriction width of 1.13  $\mu\text{m}$ . The structures were fabricated on a silicon substrate using a resist mask created by electron-beam-lithography (EBL), followed by sputtering of the thin film layers Ta(2 nm)/Pt(7 nm)/Ni<sub>81</sub>Fe<sub>19</sub>(5 nm)/Ta(2 nm) and lift-off. The electrical contacts were created using an additional EBL resist mask followed by thermal evaporation of the metals (Cr/Au) and lift-off. The structure under test has an average resistance 350  $\Omega$ .

The temporal response of the SHNOs was tested under two types of pulse excitations, as illustrated in Fig. 1(a). The first type concerned the use of voltage pulses ( $V_p$ ) to drive the AOs and the second type concerned the combined use of voltage and microwave pulses ( $RF_p$ ) in order to induce injection-locking of the AOs to the external RF stimuli.

Figures 1(a)-(b) highlight the magnetic field and current directions necessary for generating AOs by means

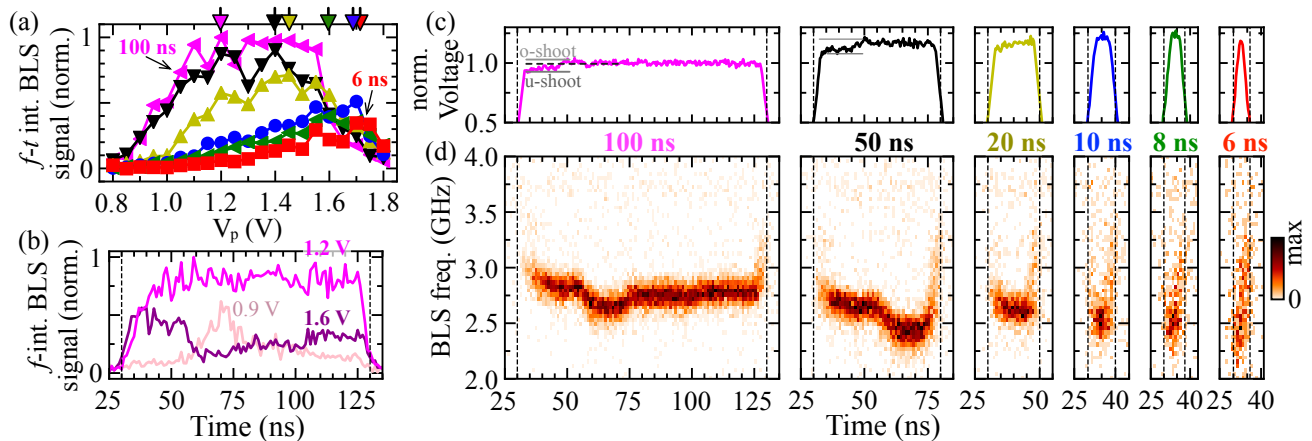


FIG. 2 (Color online). (a) Frequency- and time-integrated BLS signal plotted as a function of  $V_p$ , for the various pulse durations. Signal integrated between 1.8 GHz and 7.1 GHz, over the pulse width and normalised with respect to the signal obtained using 100 ns pulses. (b) Frequency-integrated TR-BLS data obtained using 100 ns wide pulses, for  $V_p$  values of 0.9 V, 1.2 V ( $V_{op}$ ), and 1.6 V. Vertical dashed lines are coincident with the onset and outset of the AOs (same for (d)). (c) Time dependence of  $V_p$ , measured using an oscilloscope and normalised with respect to  $V_{op} = 1.2$  V. (left panel) (u)under-shoot and (o)over-shoot highlight the variations of the instantaneous voltage with respect to  $V_p$ . (d) TR-BLS spectra obtained at  $V_{op}$ , for the different pulse durations. The values of  $V_{op}$  are indicated in (a) by the vertical arrows. From left to right, the maximum of the intensity-coded scale-bars have the values of 1, 0.8, 0.8, 0.4, 0.3 and 0.2, respectively.

of SHE and SOT [3, 4, 10]. In particular, the direction of the injected current ( $I$ ), the polarisation of the pure spin current ( $P$ ) arising due to SHE and the direction of the magnetic moment ( $m$ ) in the presence of an in-plane magnetic field ( $H$ ). The external magnetic field must be applied in the direction perpendicular to the current flow, as the SOT efficiency is maximised [5, 10, 13]. At sufficiently large current densities, this leads to damping compensation and consequent emergence of AOs in the constriction region. In the present experiments,  $H$  is tilted by 80 degrees with regard to  $I$ , so that the field-like torque induced by the microwave current in the Pt layer, has a component orthogonal to  $m$ . This results in an increased coupling between the AOs and the external microwave field, with little impact on the AOs [25, 26]. In all experiments reported, the magnitude of  $H$  was first increased to 200 mT for the purpose of saturating the magnetization, and then decreased to 20 mT.

Time-resolved Brillouin light scattering microscopy (TR-BLS) was employed to measure the frequency spectra of the AOs as a function of time. Using this spectroscopic technique, nanosecond time resolution and sub-micron spatial resolution can be achieved [27]. The measurement apparatus included electrical inputs for injecting voltage pulses and RF signals, generated by an arbitrary waveform generator and microwave source, combined via a microwave diplexer. The voltage pulses have a trapezoidal shape, with rise and fall time of 4 ns and a repetition rate of 4 MHz.

### III. MAGNETIZATION AUTO-OSCILLATIONS DRIVEN BY VOLTAGE PULSES

Figures 1(c)-(d) show the BLS spectra as a function of  $V_p$ , obtained using pulses with durations of 100 ns and 8 ns, respectively. This data representation provides an overview of the frequency and intensity of the generated AOs. Despite the difference between the BLS intensity obtained using 100 ns and 8 ns voltage pulses, both spectra exhibit a similar trend, where the frequency of the AO mode observed varied from 3 GHz to 2.2 GHz with increasing  $V_p$ . Such frequency downshift is consistent with theory and with previous experiments involving SHNOs with a similar geometry [5, 13]. Note that in the BLS data obtained with the 100 ns pulses, the maximum intensity is obtained at  $V_p = 1.2$  V while the BLS data obtained with the 8 ns pulses exhibited a maximum intensity at  $V_p = 1.6$  V. Importantly, we provide first hand-demonstration that AOs can be obtained using few-nanosecond wide voltage pulses.

Figure 2(a) shows a summary of the frequency- and time-integrated BLS intensity, as a function of  $V_p$  and pulse width. The voltages that resulted in the maximum integrated AO amplitude were designated as optimal voltages  $V_{op}$  and are indicated by the vertical arrows. Here, we find that  $V_{op}$  increases from 1.2 V to 1.7 V with decreasing the pulse width from 100 ns to 6 ns. The integrated AO signal obtained using 100 ns and 50 ns wide pulses, shows a similar maximum amplitude. The 20 ns wide pulses resulted in a 25 % reduction of the maximum amplitude, while the 6 ns pulses resulted in a 65 % decrease of the integrated AO amplitude.

Figure 2(b) shows the time dependence of the frequency-integrated BLS signal obtained using 100 ns wide voltage pulses, for three different values of  $V_p$ . We found that the trapezoidal time-dependence of the input voltage was best converted to the time-dependence of the AO signal when  $V_{op}$  was applied. If the nominal input voltage was either below or above  $V_{op}$ , the amplitude of the AOs was not distributed evenly within the pulse width, as exemplified by the AO signal obtained for  $V_p$  values of 0.9 V and 1.6 V.

The time dependence of the voltage signals applied to the SHNO, measured using an oscilloscope, are shown in Fig. 2(c). Note that the initial segment of the voltage signal exhibits an undershoot and an overshoot of 6 % and 4 %, respectively, as highlighted by the horizontal dashed lines for the case of the 100 ns wide pulse, but it can also be observed in the 50 ns pulse. Such behaviour is reminiscent of the ringing effect in the RLC-equivalent circuit formed by the electrical cables, the electrical contacts on the substrate and the SHNO, as response to sudden changes in the input signal.

TR-BLS spectra, resulting from applying the voltage pulses, are shown in Fig. 2(d) at the indicated pulse widths, obtained at the corresponding  $V_{op}$  values. In general, we find that AO signal is detected for values of the instantaneous voltage above 50 % of  $V_{op}$ . This response is highlighted by the vertical dashed lines at the onset and offset of the AO signals and voltage pulses.

For 100 ns wide pulses (shown on the leftmost panel in Fig. 2(d)) we observe that in the early stages of the voltage pulse, between 35 ns and 70 ns, the AO frequency varies from 2.95 GHz to 2.65 GHz, followed by an increase to 2.80 GHz at 75 ns. The frequency oscillations in the AO signal are caused by oscillations in the instantaneous voltage (current), as discussed above. From the data shown in Fig. 1(c), we note that a variation of 6 % around  $V_{op}$  can cause shifts in the AO frequency of about 200 MHz, consistent with the frequency oscillations shown in Fig. 2(d) [28]. When  $t > 75$  ns, the AO frequency stabilizes at 2.80 GHz, as the voltage signal appears to reach a steady state. At the same time, the frequency linewidth of the signal reaches a minimum of 150 MHz. We note that this value is not the real AO linewidth but rather the result of broadening due to the TR-BLS detection method [29]. When approaching the offset of the AO signal, we observe an upshift of the AO frequency, simultaneously with a decrease of the amplitude, coincident with the sharp decrease in the voltage at the pulse outset. The sudden frequency upshift is in agreement with the results shown in Figs. 1(c)-(d), where for smaller nominal voltages, we obtain larger AO frequencies and smaller amplitudes.

The TR-BLS data obtained using shorter pulses shows a behaviour similar to that described for the 100 ns pulses, particularly, the variation of the AO frequency that follows the pulse onset and the steep frequency upshift at the pulse outset. A noticeable difference is the de-

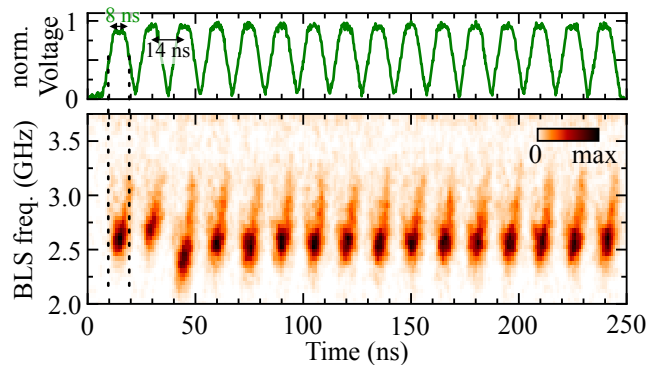


FIG. 3 (Color online). (a) (top) Time dependence of the voltage pulse train ( $V_p = 1.1$  V), measured using an oscilloscope, and (bottom) resulting TR-BLS spectra.

crease in the AO frequency with decreasing pulse width, which is explained by the increasingly larger values of  $V_{op}$ , as discussed with Fig. 2(a). In the limit of the shortest voltage pulses, one is unable to reach large AO amplitude as shown by the 60 % reduction in the integrated BLS signal, compared to that obtained with 100 ns pulses. We also note that the use of short pulses comes with the disadvantage of having a spreading of the AO frequency over the short existence of the pulse due to the rise and fall time of the pulses.

An advantage of the fast AO response is the possibility to generate a train of closely spaced AO pulses in the time-domain. This functionality is demonstrated in Fig. 3, where we show the TR-BLS spectra generated by a train of 8 ns voltage pulses with  $V_p = 1.1$  V and a period of 14 ns. It can be seen that the short bursts of AO signal can be repeated reliably over large time-scales. Next, we discuss the agility of SHNOs when in the presence of high frequency stimuli, particularly, the case where microwave pulses are utilised as a frequency-lock to the AO signal generated by voltage pulses.

#### IV. INJECTION-LOCKING USING MICROWAVE PULSES

In conventional injection-locking experiments, a magnetic field and a direct current are applied to the SHNO together with the external continuous wave (CW) RF signal that couples to the AOs [25, 30, 31]. If the frequency of the RF signal,  $f$ , is close to either the natural AO frequency,  $f_{AO}$ , or  $2f_{AO}$ , the external RF stimuli pulls the AO frequency toward its own frequency (or  $f/2$ ). This effect is observed over a range of frequencies surrounding  $f_{AO}$ , namely the injection-locking range, which can reach several hundreds of megahertz, depending on parameters such as magnetic field strength, applied direct current and microwave power [25, 30, 31]. Injection-locking is also known to result in a larger AO amplitude [26, 32, 33].



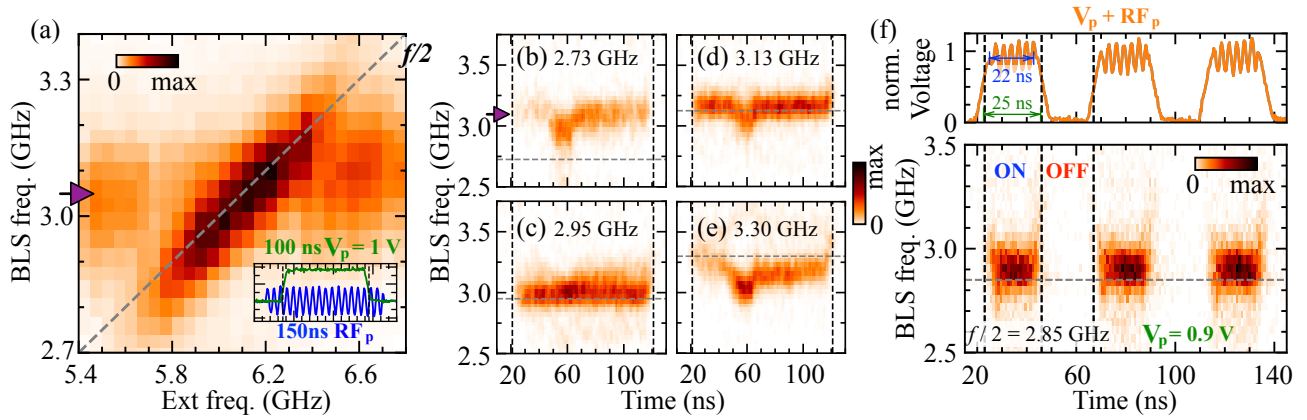


FIG. 4 (Color online). (a) BLS spectra as a function of the external RF frequency ( $f$ ) obtained using of 150 ns wide RF pulses (at  $t = 0$  ns), followed by a 100 ns wide voltage pulse (at  $t = 25$  ns), as shown in the inset plot (RF power 1 dBm). The diagonal line indicates the values of  $f/2$ . The arrow in magenta indicates  $f_{AO}$  (same as in (b)). (b)-(e) TR-BLS spectra at the  $f/2$  values of  $RF_p$ , indicated also by the horizontal dashed lines. The vertical dashed-lines indicate the onset and outset of the voltage pulse. The colour-coded intensity was normalised to a common value. (f) (top) Time-dependence of the input voltage of  $V_p + RF_p$ , and (bottom) resulting TR-BLS spectra (RF power 1 dBm).

In the present manuscript, we created the conditions for injection-locking to occur, except that instead of the direct current and CW RF signals we applied voltage and RF pulses. The BLS data, shown in Fig. 4(a), was obtained while applying 150 ns wide RF pulses to the SHNO (at  $t = 0$  ns) combined with 100 ns wide voltage pulses applied (at  $t = 25$  ns). The inset plot shows the time-dependence of the applied voltage and the RF pulse ( $RF_p$ ). The nominal voltage,  $V_p$  was set to 1 V, and the frequency ( $f$ ) of the RF pulses was varied from 5.4 GHz to 6.8 GHz ( $f \sim 2f_{AO}$ ) with a constant nominal RF power of 1 dBm. Compared to the injection-locking obtained when  $f \sim f_{AO}$ , the frequency regime of  $f \sim 2f_{AO}$ , exhibited a wider frequency locking range and larger AO amplitudes, so only this case is discussed.

In Fig. 4(a), the frequencies corresponding to  $f/2$  are illustrated by the diagonal dashed-line. For values of  $f/2$  well below 2.85 GHz, the frequency of the AO signal is constant, at  $f_{AO}$ . When  $f/2 \sim 2.9$  GHz, we observe a down-shift of the AO frequency simultaneously with an increase in the AO amplitude. Large amplitude AOs prevail as  $f/2$  increases to 3.25 GHz. Above this frequency value, the AO amplitude decreases, and  $f_{AO}$  is gradually recovered. In these measurements, we obtained a frequency locking range of approximately 350 MHz.

Figures 4(b)-(e) show the TR-BLS spectra obtained at the indicated  $f/2$  values of  $RF_p$ . An example of the AO signal in the limit of  $f/2 \ll f_{AO}$  is shown in Fig. 4(b). The spectra exhibits a weak AO mode at  $f \sim 3.0$  GHz, whose amplitude is not evenly distributed within the duration of the voltage pulse. The time-varying AO amplitude seen here is consistent with the results discussed in Fig. 2(b).

Figures 4(c)-(d) show the TR-BLS spectra obtained for  $f/2$  values within the frequency locking range, as

seen in Fig. 4(a). When  $f/2 = 2.95$  GHz, not only we obtain an overall larger AO amplitude, but we also observe that the AO frequency and amplitude remains nearly constant within the duration of the voltage pulse. In the case where  $f/2 = 3.13$  GHz, despite the large BLS signal, some oscillations in the AO frequency reappear at  $t \sim 60$  ns, as a result of a reduced injection-locking efficiency. In the example shown in Fig. 4(e), where  $f/2 \gg f_{AO}$ , the injection-locking efficiency is again low, as the time dependence of the natural AO mode is partially restored, at 3.04 GHz.

When comparing the results shown in Figs. 4(b),(e) with those shown in Figs. 4(c),(d), we note that, when  $f/2 \simeq f_{AO}$ , the amplitude of the AOs is more evenly distributed throughout the duration of the voltage pulse. Despite the voltage oscillations inherent to the ringing effect of the input circuit, the AO signal remains stable within the pulse duration, demonstrating that improvements in the agility of the SHNO are achieved by means of injection-locking.

Injection-locking allowed us to achieve pulsed AO signals with a comparably large amplitude, in addition to the frequency tunability within the locking-range. This is further demonstrated in Fig. 4(f), where the TR-BLS data shown were obtained using voltage and RF pulses with similar duration and periodicity. In this case, 25 ns wide voltage pulses were combined with 22 ns wide RF pulses. The frequency of the RF pulses shown here is within the frequency locking range of the measured device. The resulting TR-BLS spectra shows a well defined intensity in the time-domain. From an application standpoint, the time segments with well defined amplitude levels may be interpreted as output levels ON/OFF or '1'/'0'.

The results discussed so far suggest that the interplay

294 between voltage and RF pulses gives rise to multi-level  
 295 time-domain amplitude patterns. In Fig. 5 we demon-  
 296 strate two ways in which the voltage and RF inputs can  
 297 be combined in order to generate short-time segments  
 298 with well defined levels of AO amplitude.

299 In the method discussed with Figs. 5(a)-(e), voltage  
 300 pulses with a duration of 125 ns ( $V_p = 1$  V) were applied  
 301 to the SHNO. Following the onset of the AO signal, we  
 302 applied a sequence of three RF pulses, with 28 ns width  
 303 and a separation of 15 ns. The time dependence of the  
 304 input stimuli is shown in Fig. 5(a), where the vertical  
 305 dashed lines coincide with the onset and outset of each  
 306 RF pulse. Figure 5(b) shows the TR-BLS spectra of the  
 307 natural AO mode, obtained with the RF pulses switched  
 308 off. Here, the oscillations in the AO frequency and the  
 309 uneven distribution of the AO amplitude in the time-  
 310 domain are consistent with the ringing behaviour of the  
 311 AO signal, discussed with Fig. 2 (c).

312 The TR-BLS spectra of the pulsed injection-locking  
 313 sequence are shown in Figs. 5(c)-(d), for  $f/2$  values of  
 314 2.9 GHz and 3.05 GHz, respectively, chosen within the  
 315 frequency locking range of the measured device. As ex-  
 316 pected, injection-locking occurs only during the three  
 317 time segments coincident with the RF pulses. For the  
 318 other two segments, where the RF excitation is switched  
 319 off, the AO amplitude is reduced considerably as the nat-  
 320 ural AO frequency is restored.

321 Figure 5(e) shows the BLS signals integrated between  
 322 2.6 GHz and 3.5 GHz, obtained from the data shown in  
 323 Figs. 5(b)-(d). The frequency range of the integration  
 324 ( $df$ ) is illustrated by the horizontal lines. First, note  
 325 that by applying the first RF pulse immediately after the  
 326 onset of the AOs, the instantaneous amplitude increased  
 327 such that the time-profile of the AO amplitude became  
 328 similar to that of the input voltage pulse (Fig. 5(a)). The  
 329 two RF pulses that followed resulted in twice the AO  
 330 amplitude compared to the natural AO mode. Using this  
 331 approach, we obtain an amplitude modulated AO signal,  
 332 reminiscent of a two-level system alternating between the  
 333 frequency-locked state (1) and the natural AO state (0.5).

334 Next, we discuss a method which allows us to obtain  
 335 amplitude modulation of two frequencies at distinct time  
 336 segments of a voltage pulse train. The voltage of the  
 337 trapezoidal pulse varies between 1 V and 0.5 V, as shown  
 338 in Fig. 5(f). Here, the line in green corresponds to the  
 339 trapezoidal pulses with a duration of 12 ns and a period  
 340 of 30 ns, while the line in orange shows the voltage pulses  
 341 combined with a CW RF signal.

342 The TR-BLS spectra obtained when applying the volt-  
 343 age pulses only (RF<sub>p</sub> is off) is shown in Fig. 5(g), where  
 344 we note that the AO mode appears at 2.95 GHz, in the  
 345 time segments where the instantaneous voltage is equal  
 346 to  $V_p$ . Here, the frequency upshift observed at the on-  
 347 set and outset of the AO signal is coincident with the  
 348 time segments corresponding to the rise and fall of the  
 349 voltage pulses. In the time segments coincident with  
 350  $V_p/2 = 0.5$  V, the AO signal was too small to be detected,  
 351 as expected from the results presented in Fig. 1(c).

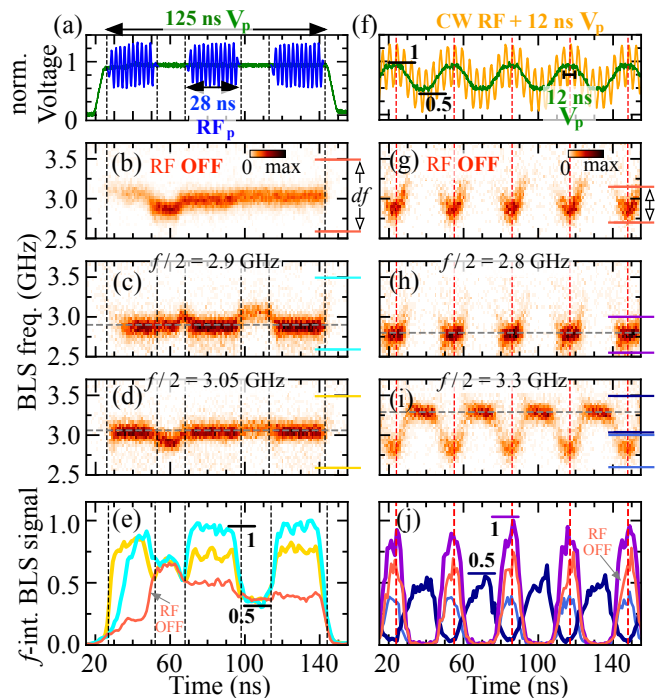


FIG. 5 (Color online). (a) Time dependence of  $V_p$  (green) and the RF pulses (blue). (b) TR-BLS spectra measured while applying  $V_p = 1$  V only (RF<sub>p</sub> off). (c)-(d) TR-BLS spectra obtained while applying  $V_p$  (1 V) and RF pulse trains with the indicated  $f/2$  values (RF power of 1 dBm). Colour coded BLS intensity of (b)-(d) was normalised to the same value. (e) TR-BLS intensity integrated from 2.6 GHz to 3.5 GHz. The integration range ( $df$ ) is illustrated by the horizontal line markers in (b)-(d). (f) Time dependence of  $V_p$  with (orange) and without (green) an added CW RF signal. (g) TR-BLS spectra measured while applying the voltage train only (RF off). (h)-(i) TR-BLS spectra obtained at two different  $f/2$  values, within the injection-locking range (RF power of 1 dBm). Colour coded intensity of (g)-(i) are normalised to the same value. (j) Frequency-integrated TR-BLS signal showing the spin wave and the AO amplitudes at distinct time segments.

When the CW RF signal was switched on, at  $f/2 = 2.8$  GHz, injection-locking is observed, as shown by the example TR-BLS spectra in Fig. 5(h), where the resulting AOs have larger amplitude compared to the natural AO signal. It is worth noting that the frequency upshift observed in Fig. 5(g) is suppressed due to injection-locking. Despite the improved frequency stability of the AO signal, no signal is detected in the time segments coincident with  $V_p/2$ .

Interestingly, when the frequency of the CW RF signal is larger than  $f_{AO}$ , as in the example shown in Fig. 5(i), a BLS signal is observed at  $f/2 = 3.3$  GHz, in the time segments coincident with the  $V_p/2$  level, while in the time segments coincident with the  $V_p$  level, the natural AO mode at  $f_{AO}$  is observed.

The observation of BLS signal in the time segments coincident with  $V_p/2$  may be interpreted in the following

manner. While the pure spin current in the  $V_p/2$  level may not be sufficient to fully compensate the damping and efficiently generate AOs, it still contributes to a decrease in the effective damping. In this scenario, a downshift of the spin wave band in the constriction region is expected, owing to partial damping compensation. As a consequence, when applying RF pulses with  $f > f_{AO}$  one is able to directly excite and detect spin waves.

Figure 5(j) shows the TR-BLS signal integrated over a 450 MHz frequency range surrounding the spin wave the AO signal, as illustrated by the horizontal lines in Figs. 5(g)-(i). The data shows two TR-BLS signals responding to  $V_p$  and  $V_p/2$ , obtained at two distinct time segments of the duty cycle. These two signals differ in frequency by 0.5 GHz, as a result of the two different external RF frequencies and the natural AO frequency.

## V. CONCLUSION

Using a single magnetic oscillator we generated nanosecond wide AO signals in the gigahertz regime, under pulsed operation. We showed that a stable AO frequency in the time-domain can be achieved for certain optimal input voltage values, which tend to increase with decreasing pulse duration. The fact that we observed the response time of the circuit in the form of a time-varying AO frequency demonstrates that AOs can

accompany the rapid changes in the instantaneous voltage of the input stimuli, at least within the nanosecond time-resolution of TR-BLS. The injection-locking experiments showed that the coupling of the SHNO to external microwave pulses results in improved temporal stability of the AO frequency and amplitude.

The control over the frequency response of magnetic oscillators plays an important role in applications. There exist a number of approaches via which the oscillation frequency can be controlled, for example, via changing the amplitude and polarity of the direct current or the external magnetic field, injection-locking and voltage control [34]. Our results suggest that such approaches may also work efficiently under pulsed operation. Furthermore, we highlight that the tunability over the frequency and amplitude of magnetic oscillators, gained when combining pulsed voltage and injection-locking, can be viewed as a way to obtain frequency encoding and multi-level amplitude as outputs in the time-domain.

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