# Electromagnetically driven convection suitable for mass transfer enhancement in liquid metal batteries

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# Electromagnetically driven convection suitable for mass transfer enhancement in liquid metal batteries

Norbert Weber[a], Michael Nimtz[a], Paolo Personnettaz[a,c], Alejandro Salas[a,b], Tom Weier[a]

[a] *Helmholtz-Zentrum Dresden – Rossendorf, Bautzner Landstr. 400, Dresden, Germany*
[b] *Instituto Tecnológico y de Estudios Superiores de Monterrey, Monterrey, Mexico*
[c] *Politecnico di Torino, Corso Duca degli Abruzzi 24, 10129 Torino, Italy*

**Abstract**

Liquid metal batteries (LMBs) were recently proposed as cheap large scale energy storage. Such devices are urgently required for balancing highly fluctuating renewable energies. During discharge, LMBs tend to form intermetallic phases. These do not only limit the up-scalability, but also the efficiency of the cells. Generating a mild fluid flow in the fully liquid cell will smoothen concentration gradients and minimise the formation of intermetallics. In this context we study electro-vortex flow numerically. We simulate a recent LMB related experiment and discuss how the feeding lines to the cell can be optimised to enhance mass transfer. The Lorentz forces have to overcome the stable thermal stratification in the cathode of the cell; we show that thermal effects may reduce electro-vortex flow velocities considerable. Finally, we study the influence of the Earth magnetic field on the flow.

*Keywords:* liquid metal battery, mass transfer, electro-vortex flow, swirl, Rayleigh-Bénard convection, OpenFOAM

## 1. Introduction

Integrating highly fluctuating renewable energies (such as photovoltaics and wind power) into the electric grid calls for large scale energy storage. Such storage must be, first of all, safe and cheap. The liquid metal battery (LMB) promises both. After being intensively investigated in the 1960s, and abandoned later, LMB research experienced a renaissance some ten years ago. For an overview of the pioneering work, see [1–3] (recommended [4]) and for the recent work [5] and [6].

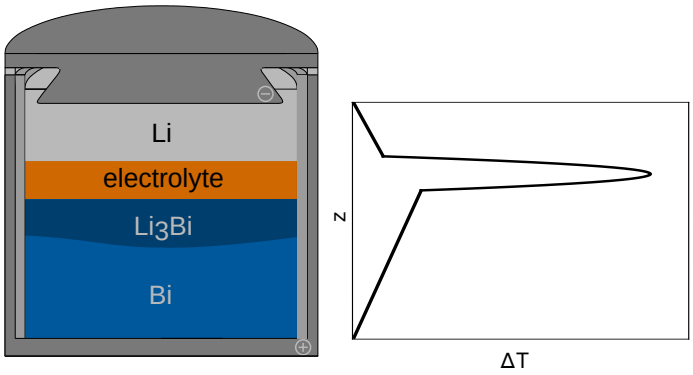


Figure 1: Sketch of a typical Li||Bi liquid metal battery with an intermetallic phase forming in the cathode (left) and vertical temperature distribution in the three layers for pure diffusion (right).

Fig. 1a shows a sketch of a typical LMB. A dense metal on the bottom (cathode, positive electrode) is separated by a liquid salt from a lighter metal at the top (anode, negative electrode). All three phases float above each other; the salt acts as the electrolyte. The word "liquid metal battery" names only a type of battery (which may consists of many different active metals). Typical cells include Ca||Bi [7, 8], Ca||Pb [9], K||Hg [10, 11], Li||Bi [1, 12–16], Li||Pb [1, 17], Li||Sb [5, 17], Li||Sn [1, 14, 18–20], Li||Zn [1], Mg||Sb [5, 21, 22], Na||Bi [1, 14, 18, 20, 23–27], Na||Hg [5, 28, 29], Na||Pb [1, 14, 20, 27, 30], Na||Sn [1, 11, 18, 20, 31, 32] and Na||Zn [33, 34] as well as exotic ones such as Li||Se [1, 35, 36] or Li||Te [1, 14, 15, 35, 36].

During discharge, the anode metal is oxidised, crosses the electrolyte layer and alloys in the bottom layer with the dense metal ("concentration cell"). Commonly, the ohmic resistance of the electrolyte layer represents the most important overvoltage. However, at higher discharge currents concentration polarisation enters the field [5, 11, 22, 28, 32, 37]. Example: when *discharging* a Li||Bi cell, Li-rich alloy will concentrate at the cathode-electrolyte interface. When a certain local concentration is exceeded, a solid intermetallic phase ($Li_3Bi$) will form (fig. 1a) [1, 24]. Such intermetallics often float on the cathode metal [38]. Sometimes they expand during solidification. As the walls impede a lateral expansion, the intermetallic will form a dome until finally short-circuiting the electrolyte. Especially in Ca based cells, locally growing dendrites may additionally short-circuit the cell [7]. Besides of all the mentioned drawbacks, the formation of intermetallics has one advantage: it removes anode metal from the melt and keeps thereby the voltage constant. It should be also mentioned that some intermetallics have high resistances while others are good conductors.

When *charging* the cell of fig. 1a, the cathode-electrolyte interface will deplete of Li and a similar concentration gradient may develop [24]. This effect is undesirable, too. Finally, all the same effects may theoretically happen in the anode compartment, too, if an alloyed top electrode is used (e.g. CaMg [8, 21]). However, such effects were not reported, yet.

It was early proposed that a mild fluid flow may counterbalance concentration gradients and increase thereby the efficiency of LMBs [1, 24, 37]. While "mechanical stirring" [1, 37] seems difficult to realise, a localised heating or cooling inducing thermal convection may be a very good option [39, 40]. Electrovortex flow (EVF) may be used for an efficient mass transfer enhancement, too [41–43]. Simply saying, EVF always may develop when current lines are not in parallel. It can therefore easily be adjusted by choosing the diameter/geometry of the current collectors and feeding lines appropriately. EVF drives a jet away from the wall, forming a poloidal flow [44]. For a classical example of the origin of EVF, see Lundquist [44] and Shercliff [45], for a good introduction Davidson [46] and a detailed overview including many experiments Bojarevics et al.

[47]. Its relevance for LMBs is outlined by Ashour et al. [43]. It should also be mentioned that other flow phenomena like the Tayler instability [48–56] , Rayleigh-Bénard convection [57, 58] or interface instabilities [59–63] may enhance mass transfer in LMBs, as well.

This article is dedicated (mainly) to electro-vortex flow. It's aim is twofold: first, we will show how the connection of the supply lines to the cell influences the flow. Second, we study how electro-vortex flow and thermal convection interact. For this purpose we combine numerical simulation with a simple 1D conduction model. These models – and the experiment which inspired our studies – are described in the following section.

## 2. Physical, mathematical and numerical model

In this section we will first present the experiment [64] which inspired this article. Thereafter we explain the way in which we estimate the temperature gradient appearing in the cathode of a liquid metal battery (LMB). Finally, we give an introduction to the 3D numerical models used.

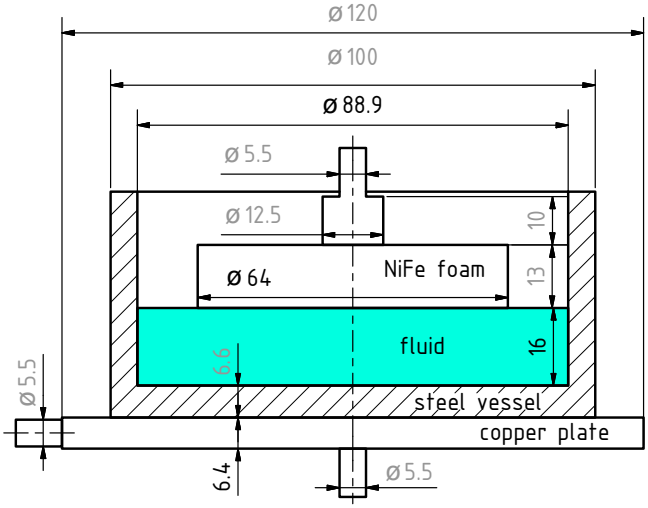


Figure 2: Dimensions of the experiment and simulation model (in mm). The grey values are not exactly known; they are estimated from the sketch in [64]. The wires are assumed to be made of copper.

Fig. 2 illustrates the mentioned experiment, conducted by Kelley & Sadoway [64]. A cylindrical steel vessel contains a melt of eutectic lead-bismuth at 150 °C. An electric current (up to $0.375\,\mathrm{A/cm^2}$ ) is applied between a bottom and top electrode. The bottom electrode may be attached centrically or laterally. The upper electrode consists of a nickel-iron foam; such foam is often used in LMBs to contain the anode metal [6]. As the setup is heated from below, Rayleigh-Bénard cells appear. If an internal current is applied, the flow becomes much more regular at $0.05\,\mathrm{A/cm^2}$. It is deduced that convection cells align with the magnetic field. It is further claimed that the copper plate which placed between the bottom electrode and the the vessel, "ensures a uniform current density" in the melt. We will show that this is not exactly true; we will further demonstrate how electro-vortex flow may give an alternative explanation for the increase in order.

We use the following material properties of eutectic PbBi at 150 °C [43]: a kinematic viscosity of $\nu = 2.7 \cdot 10^{-7}\,\mathrm{m^2/s}$, a thermal expansion coefficient of $\beta = 1.3 \cdot 10^{-4}\,\mathrm{K^{-1}}$, an electric conductivity of $\sigma = 9 \cdot 10^5\,\mathrm{S/m}$, a density of $\rho = 10\,505\,\mathrm{kg/m^3}$, an isobaric heat capacity of $c_p = 148\,\mathrm{J/kg/K}$, a heat conductivity of $\lambda = 10\,\mathrm{W/m/K}$, a thermal diffusivity of $\alpha = 6 \cdot 10^{-6}\,\mathrm{m^2/s}$, a Prandtl number of $Pr = 0.04$ and a sound velocity of $u_\mathrm{s} = 1\,765\,\mathrm{m/s}$ [65–67]. The electric conductivity of the vessel is assumed to be $\sigma = 1.37 \cdot 10^6\,\mathrm{S/m}$ and of the wires and copper plate $\sigma = 58.1 \cdot 10^7\,\mathrm{S/m}$. The electric conductivity of the Fe-Ni foam is not easy to determine; we use a value of $\sigma = 1.37 \cdot 10^6\,\mathrm{S/m}$ without further justification.

Geometrically, the described experiment perfectly represents a liquid cathode of an LMB. However, the temperature gradient in a working LMB depends on the boundary conditions. For a single cell in an environment at room temperature it will rather be opposite to that in the experiment. As the electrolyte layer has the highest resistance (four orders larger than the metals), most heat will be generated there [57]. Fig. 1b shows a typical vertical temperature profile through all three layers. If no thermal management system induces additional temperature gradients (as suggested in [21, 40]) a stable thermal stratification

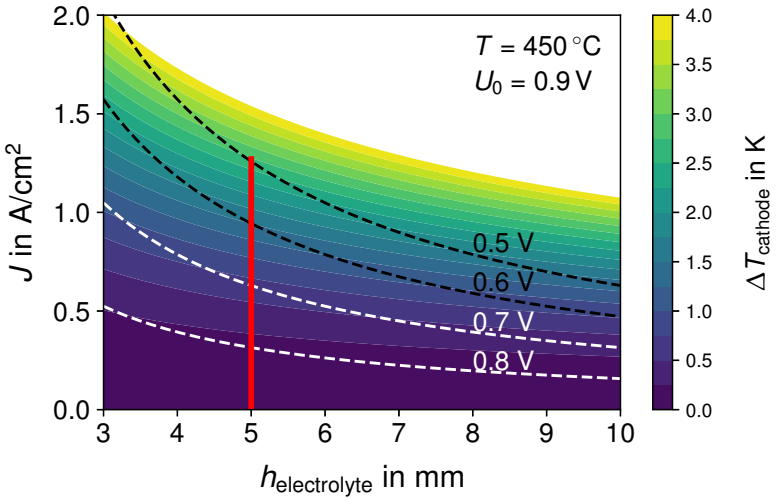


Figure 3: Temperature difference in the cathode for pure conduction in a Li||Bi cell. The same model and material properties as in [68] are used.

is expected in the cathode. To drive a flow there, any force has to overcome first this stable stratification.

The temperature difference between top and bottom of the cathode can be estimated using the simple 1D heat conduction model developed by Personnettaz et al. [68] (for a 3D study of heat transfer in a Li||PbBi cell, see [69]). He considers a Li|LiCl-KCl|Bi cell operating at 450°C. Although our cathode is made of eutectic PbBi (and not Bi), we use the same model to get a rough *estimate* of the temperature gradient in the cathode. The Li-layer is assumed to be 32 and the Bi-layer 16 mm thick; for the material parameters, see [68]. Depending on the current density and thickness of the electrolyte, the $\Delta T$ over the cathode changes as illustrated in fig. 3. In our numerical simulation we will assume the electrolyte to be 5 mm thick (realistic values are 3-15 mm [70]). We will use the temperature difference of fig. 3 as boundary condition as

$$\Delta T = \frac{h_{\mathrm{Bi}} h_{\mathrm{salt}} q \left(2 h_{\mathrm{Li}} \lambda_{\mathrm{salt}} + h_{\mathrm{salt}} \lambda_{\mathrm{Li}}\right)}{2 h_{\mathrm{Bi}} \lambda_{\mathrm{Li}} \lambda_{\mathrm{salt}} + 2 h_{\mathrm{Li}} \lambda_{\mathrm{Bi}} \lambda_{\mathrm{salt}} + 2 h_{\mathrm{salt}} \lambda_{\mathrm{Bi}} \lambda_{\mathrm{Li}}}, \tag{1}$$

with $h$, $\lambda$ and $q$ denoting the layer heights, the thermal conductivities and the

volumetric heat source in the electrolyte. We will study, if electro-vortex flow can overcome the stable stratification.

The numerical model is implemented in OpenFOAM [71]; the electro-vortex flow solver is explained in detail in [72]. Basically, it computes the electric potential $\phi$ and current density $\boldsymbol{J}$ on a global mesh as

$$\nabla \cdot \sigma \nabla \phi = 0 \tag{2}$$

$$\boldsymbol{J} = -\sigma \nabla \phi \tag{3}$$

with $\sigma$ denoting the electric conductivity. All conducting regions (of different conductivities) are fully coupled. The results are then mapped on a separate fluid mesh. Induced currents and magnetic fields are neglected, which is justified as long as the velocities are small. On the fluid mesh the following set of equations is solved:

$$\frac{\partial \boldsymbol{u}}{\partial t} + (\boldsymbol{u} \cdot \nabla)\, \boldsymbol{u} = -\nabla p + \nu \Delta \boldsymbol{u} + \frac{\boldsymbol{J} \times \boldsymbol{B}}{\rho} \tag{4}$$

$$\boldsymbol{B}(\boldsymbol{r}) = \frac{\mu_0}{4\pi} \int \frac{\boldsymbol{J}(\boldsymbol{r}') \times (\boldsymbol{r} - \boldsymbol{r}')}{|\boldsymbol{r} - \boldsymbol{r}'|^3} dV' \tag{5}$$

$$0 = \Delta \boldsymbol{B} \tag{6}$$

with $t$, $\boldsymbol{u}$, $p$, $\nu$, $\rho$, $\mu_0$, $\boldsymbol{r}$ and $V$ denoting the time, the velocity, the pressure, the kinematic viscosity, the density, the vacuum permeability, the coordinate and the cell volume, respectively. The Biot-Savart integral is only used to determine the magnetic field $\boldsymbol{B}$ on the boundaries. The fluid mesh has at least 200 cells on the diameter, which is fine enough according to [43].

If thermal effects shall be included, the Oberbeck-Boussinesq approximation [73] is used (for its validity, see [43, 74]). The following set of equations is solved

$$\frac{\partial \boldsymbol{u}}{\partial t} + \nabla \cdot (\boldsymbol{u}\boldsymbol{u}) = -\nabla p_d + \nu \Delta \boldsymbol{u} - \boldsymbol{g} \cdot \boldsymbol{r} \nabla \rho_k + \frac{\boldsymbol{J} \times \boldsymbol{B}}{\rho_0} \tag{7}$$

$$\nabla \cdot \boldsymbol{u} = 0 \tag{8}$$

$$\frac{\partial T}{\partial t} + \nabla \cdot (\boldsymbol{u} T) = \frac{\lambda}{\rho_0 c_p} \Delta T \tag{9}$$

with $\boldsymbol{u}$, $p$, $\nu$, $\boldsymbol{g}$, $\boldsymbol{r}$, $T$, $c_p$ $\boldsymbol{J}$ and $\sigma$ denoting velocity, pressure, kinematic viscosity, gravity, position vector, temperature, specific heat capacity, current density and

electric conductivity, respectively. The density $\rho = \rho_0\rho_k = \rho_0(1 - \beta(T - T_{\mathrm{ref}}))$ is calculated using the mean density $\rho_0$ at reference temperature $T_{\mathrm{ref}}$ and the coefficient of thermal expansion $\beta$; $\boldsymbol{J}$ and $\boldsymbol{B}$ are determined by the electro-vortex solver as described above. At least 250 cells on the diameter and strongly refined boundary layers are used.

## 3. Results

This section is arranged as follows: firstly, we compare the influence of a symmetric and asymmetric current supply on pure electro-vortex flow (fig. 4). Thereafter, we study the influence of the Earth magnetic field and of thermal stratification on both connection types (fig. 5 and 6). Further, we give estimates of the flow velocity depending on the cell current.

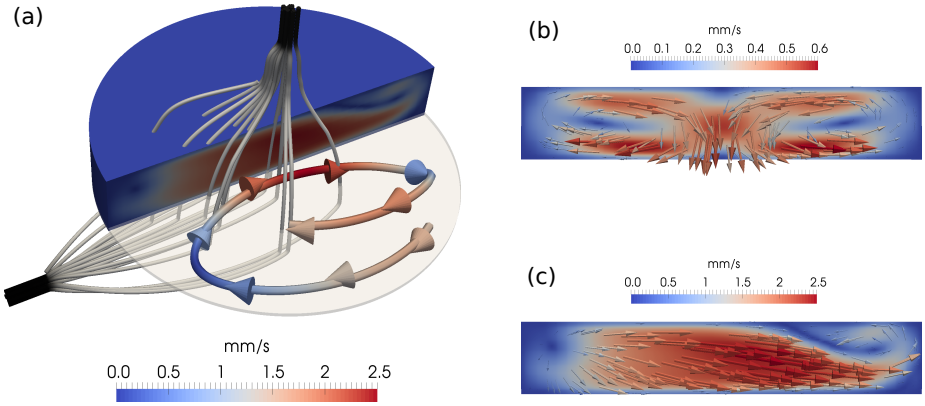


Figure 4: Current path and velocity streamlines for a current supply from the side (a). Velocity on a vertical plane for symmetric (b) and lateral current supply (c). The current is $I = 40\,\mathrm{A}$; the results show electro-vortex flow alone.

Fig. 4a illustrates the current path, streamlines and velocities for a lateral supply line. Electro-vortex flow is simulated alone; the applied current is 40 A. The flow profile is essentially horizontal forming two kidney-shaped vortices. The velocity reaches 2.5 mm/s. The *horizontal* jet (also shown in 4c) is uncommon for electro-vortex flow, but can easily be explained. As the current flows mainly horizontally through the copper plate, it induces a magnetic field in the

fluid. This field points towards the observer (in fig. 4a and c). The current in the liquid metal flows upwards (vertically) and interacts with the induced field. Consequently, the Lorentz force points to the right and drives the observed flow in "prolongation" of the current supply. For similar experiments, see [75, 76].

Fig. 4b shows the flow profile for a symmetric current supply, again for 40 A. A typical poloidal flow develops as it was often observed experimentally [47, 77–81]. Similar flow structures are very well known from vacuum arc remelting and electro-slag remelting [82–89]. However, depending on the exact geometry, the direction of the flow might be reversed [90–93]. In our simulation, the velocities reach 0.6 mm/s for the symmetrical setup. This is only 25 % of the flow velocity observed for a lateral current supply. Due to the shallow liquid metal layer, a poloidal flow will dissipate strongly in the boundary layer.

The simulated velocities are not directly comparable to the experiment. The latter was additionally heated from below (vertical temperature difference of approximately $\Delta T = 10\,\mathrm{K}$). As shown numerically by Beltrán, the experimentally observed flow is mainly caused by Rayleigh-Bénard convection. Also he used a volumetric expansion coefficient three times smaller than the real one [64, 94] (for the correct value see [43]), his velocity profile and magnitude (3 mm/s) matches very well to the experimental results (compare fig. 9 in [94] and fig. 4 in [64]). Electro-vortex flow will generally lead to velocities one order of magnitude smaller (Kelley and Sadoway [64] used currents of 23.3 A at most; our results are for 40 A). However, electro-vortex flow will surely influence the flow structure and may explain the increase in order of the flow which was observed experimentally.

In the next step we focus on the symmetric current supply (with the poloidal flow) only, and analyse the influence of a vertical magnetic background field. When we add the magnetic field of the Earth (measured in Dresden as $\boldsymbol{B} = (15 \cdot \boldsymbol{e}_x, 5 \cdot \boldsymbol{e}_y, 36 \cdot \boldsymbol{e}_z)\,\mu\mathrm{T}$) the original poloidal flow (fig. 5a) becomes strongly helical (fig. 5b). The appearance of such azimuthal swirl flow is well known from experiments [43, 77, 95] and can be easily explained. Radial cell currents and a vertical magnetic background field lead to azimuthal Lorentz forces [79, 84, 95].

Compared to a recent experiment by Ashour [43] with a point electrode on the top, we observe considerably stronger swirl (compare fig. 5b with fig. 5 in [43]). We attribute this difference to the location of the azimuthal forcing. Here, the force is well distributed in the whole volume; in [43] it is concentrated only in the centre of the liquid metal "sheet". We suppose the distributed azimuthal Lorentz force to better suppress the poloidal flow by forcing the streamlines into a dissipative Ekman layer [84]. Fig. 5c shows the volume averaged mean velocity of the poloidal and azimuthal flow – with and without the Earth magnetic field. If we add a vertical field, azimuthal swirl appears (compare the dashed curve). At the same time, the poloidal flow is strongly reduced (by a factor of 1/2). This fits nicely to Davidsons "poloidal suppression" model [84]. This is remarkable, because simulations with a point electrode (see [43]) did not show such a strong suppression.

Keeping the symmetric current supply, we now focus on the influence of the temperature stratification. During operation of an LMB, the cathode will be heated from above; the temperature stratification will be stable. At first glance, this configuration is similar to arc remelting. There, an electric arc heats the melt from above. However, the bath is cooled rather from the side than from below which leads to strong thermally driven flow [96], but we have a stable thermal stratification instead. Based on the temperature conduction model described in section 2 we apply a vertical temperature gradient of $\Delta T = 0.7\,\mathrm{K}$ (at 40 A). The stable thermal stratification slows down the electro-vortex flow (compare fig. 5d and e). While the general flow structure does not change, especially the velocity near the bottom wall decreases by a factor of 2/3. This result cannot be compared to the experiment, as Kelley and Sadoway heated from below (and we from above). A temperature gradient as in the experiment is not expected to appear during "normal" operation of an LMB; however, an additional heating or cooling for mass transfer enhancement (as proposed in [39, 40]) can easily lead to similar configurations.

We use two quantities to estimate the mass transfer in the cathode: the volume averaged velocity as global measure, and the mean velocity gradient at

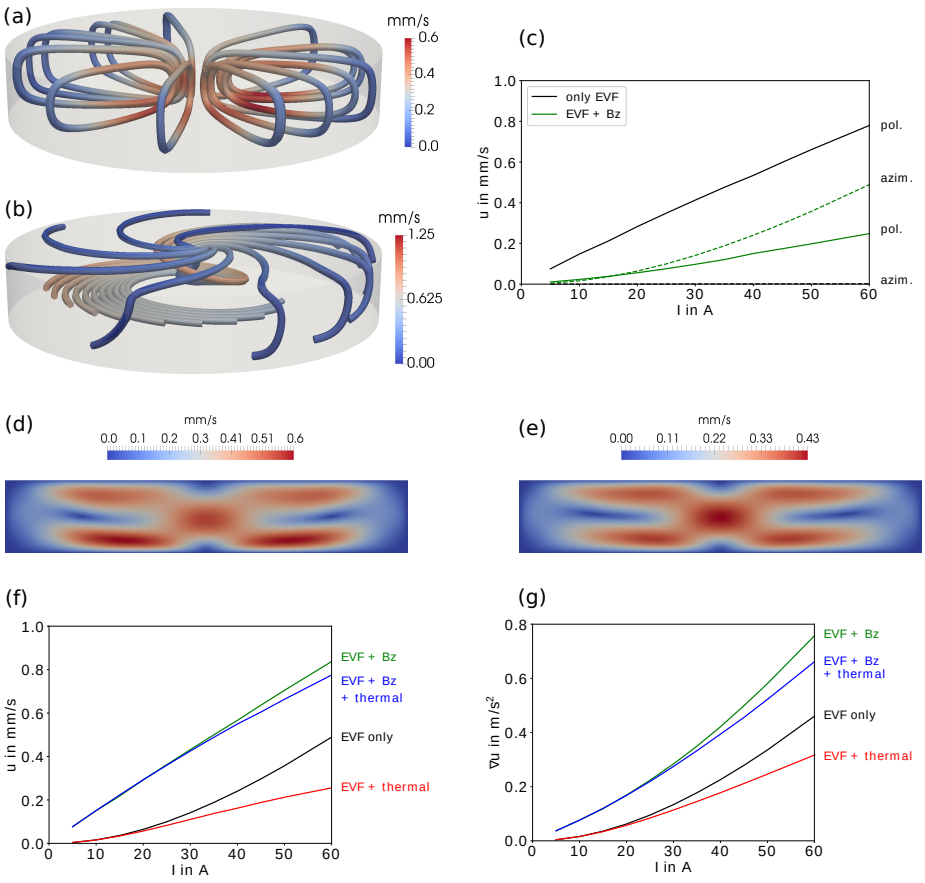


Figure 5: Streamlines and velocity without (a) and with the Earth magnetic field (b). Volume averaged mean velocities of the azimuthal and poloidal flow for both cases (c). Velocity on a vertical plane for symmetric current supply without temperature (d) and with a negative temperature gradient of 0.7 K (e). Volume averaged mean velocity (f) and mean velocity gradient (g) of electro-vortex flow alone, with an additional Earth magnetic field (Bz) and with a stabilising temperature gradient. $I = 40$ A.

the foam-cathode interface as local one. Fig. 5f and g show both quantities for electro-vortex flow alone, with the Earth magnetic field ("Bz") and with a stabilising thermal gradient. The azimuthal flow, caused by the Earth magnetic field, yields the highest velocities. A vertical temperature gradient does barely influence the horizontal flow. The poloidal electro-vortex flow ("EVF alone") is considerably slower – it is strongly dissipated at the bottom wall. The vertical

temperature gradient effectively breaks the downwards flow. Interestingly, a strong flow in the volume leads also to strong velocity gradients at the interface.

We now consider the lateral current supply, and study again the influence of temperature and the Earth magnetic field. The prevailing horizontal flow is hardly influenced by a stabilising vertical temperature gradient. The flow structure changes only slightly; the velocities with and without temperature gradient are almost the same (compare fig. 6c and d). Taking into account the Earth magnetic field changes the flow much more (compare fig. 6a and b). The horizontal current and vertical magnetic background field generate a Lorentz force which deflects the jet in clockwise direction. Presumably the stronger dissipation in the boundary layers decreases the velocity slightly. Most importantly, the Earth magnetic field does not lead to swirl flow in this configuration – the jet is only deflected. Fig. 6e and f show the mean velocity and the mean velocity gradient for pure electro-vortex flow, with the Earth magnetic field and with the stabilising temperature gradient. The differences are only marginal.

## 4. Summary & outlook

We have discussed, how electro-vortex flow (EVF) has the potential to enhance mass transfer in liquid metal batteries (LMBs). In a first step we discussed why such mass transfer enhancement is important. We emphasised that mostly (but not only) mixing of the cathode during discharge is highly beneficial. We studied the flow structure and magnitude of EVF numerically. Moreover, we discussed the influence of stray magnetic fields, the connection of the supply lines and a stable thermal stratification on electro-vortex flow.

A lateral current supply to the cathode will generate a *horizontal* flow. In contrast, a central current supply below the cathode will induce a *vertical* jet. Looking only on this flow-direction, would expect a vertical flow to be better suited for enhancing mass transfer. It will remove reaction products directly from the cathode-electrolyte interface. However, the vertical (or better: poloidal) flow has three disadvantages: (1) it's mean velocity is much smaller

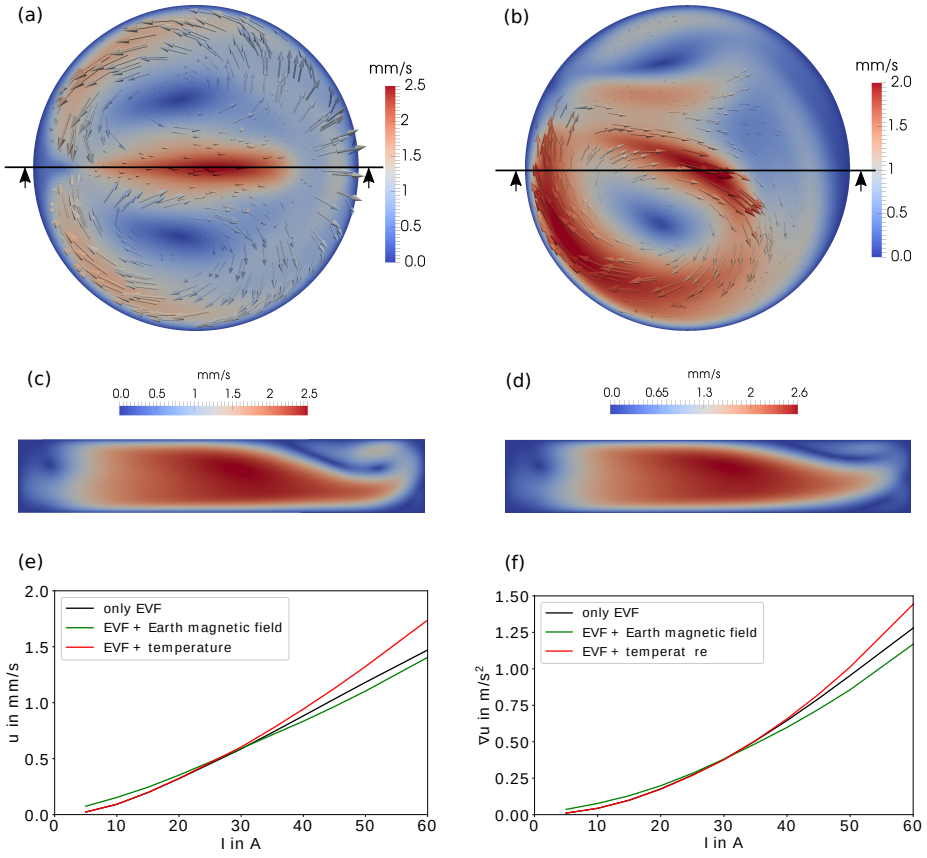


Figure 6: Electro-vortex flow for a lateral supply wire without (a) and with the Earth magnetic field (b). Flow in the cross section of the jet without (c) and with a stabilising thermal gradient (d). The current for (a)-(d) is 40 A. Volume averaged mean velocity (e) and mean velocity gradient (f) for electro-vortex flow alone, with the additional Earth magnetic field (Bz) and with a stabilising temperature gradient.

compared to the horizontal flow, (2) it is dampened by the stable temperature stratification and (3) it will turn to a swirling flow under presence of the Earth magnetic field. In contrast, the horizontal jet will not be dampened considerably by a temperature stratification nor be strongly influenced by the Earth magnetic field. We believe therefore the lateral supply line to be better suited for enhancing mass transfer. Concerning the swirl flow we could (at least partially) confirm Davidsons model of poloidal suppression.

Our models are strongly simplified: we ignore induced currents and magnetic fields; we ignore internal heating; the simulation of thermal convection and EVF is fully decoupled. A next step would be therefore the development of a fully coupled EVF-thermal convection model as well as it's coupling with a real mass transfer (e.g. Li in Bi) model. Of course, velocity and concentration measurements in a real 3-layer LMB would be a large step forward. Performing Kelley's experiment with an inverse temperature gradient (better at room temperature) could allow a further experimental study of the interaction between EVF and thermal convection.

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