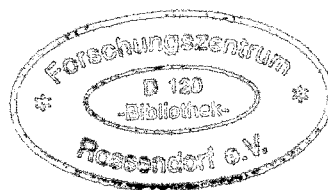


FZR-150  
September 1996

*Belegexemplar!*  
*kein Schriftverkehr*  
*vom AG gewünscht*  
*25.9.96 Ksh*

*E. Grosse and B. Kämpfer*

Internal Workshop on  
Kaon Production



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The **Internal Workshop on Kaon Production** took place on September 16, 1996 in the Research Center Rossendorf. This workshop was aimed at a survey on the experimental and theoretical status of kaon production in elementary hadron reactions and heavy-ion collisions. The experimental groups in the Institute for Nuclear and Hadron Physics reported on their activities in various collaborations at different accelerator facilities. Emphasis was put on our future abilities to achieve a substantial progress in the realm of strange particle production. From the theory side the previous results on kaon production and possible supports of the experimental research have been presented.

Please notice, the material presented here is in many cases very preliminary and is not suited for reference and should not be used in publications without explicit permission by the respective authors.

E. Grosse

B. Kämpfer

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### I. Elementary Processes $NN \rightarrow KYN$ , $NN \rightarrow K\bar{K}NN$

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- B. Kämpfer    Theory Survey
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- H. Müller      $K^-$  data from COSY
- P. Michel      $K^+$  data from COSY

### II. Kaon production in Proton-Nucleus and Heavy-Ion Collisions

- E. Grosse       $K^+$  experiments at SPES3
- E. Grosse       $K^\pm$  experiments at KaoS
- R. Kotte        $K^\pm, \Lambda$  experiments at FOPI
- K. Möller       $K^\pm$  experiments at COSY
- H. Müller       $K^\pm$  in heavy-ion collisions
- C. Schneider    $K^+$  experiments at ANKE
- H.W. Barz      Calculations of  $K^\pm$  spectra
- B. Kämpfer     Current studies of strange particle production

E. Grosse    Phenomenology

'elementary' process:  $NN \rightarrow NYK^+$   $\psi = \Lambda$

$pp \rightarrow K^+ X$   
Hogan et al.

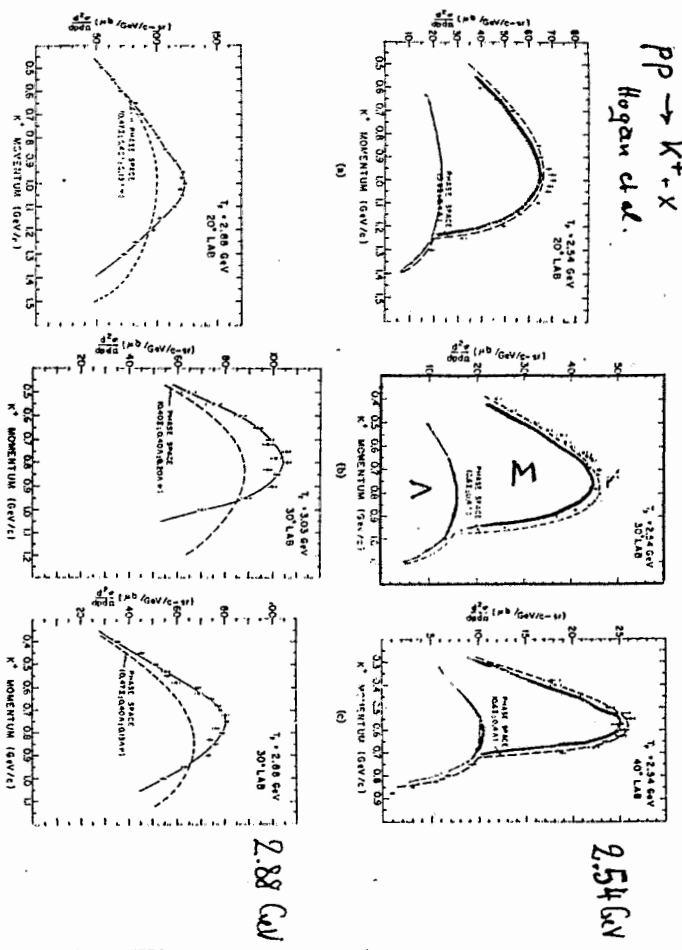
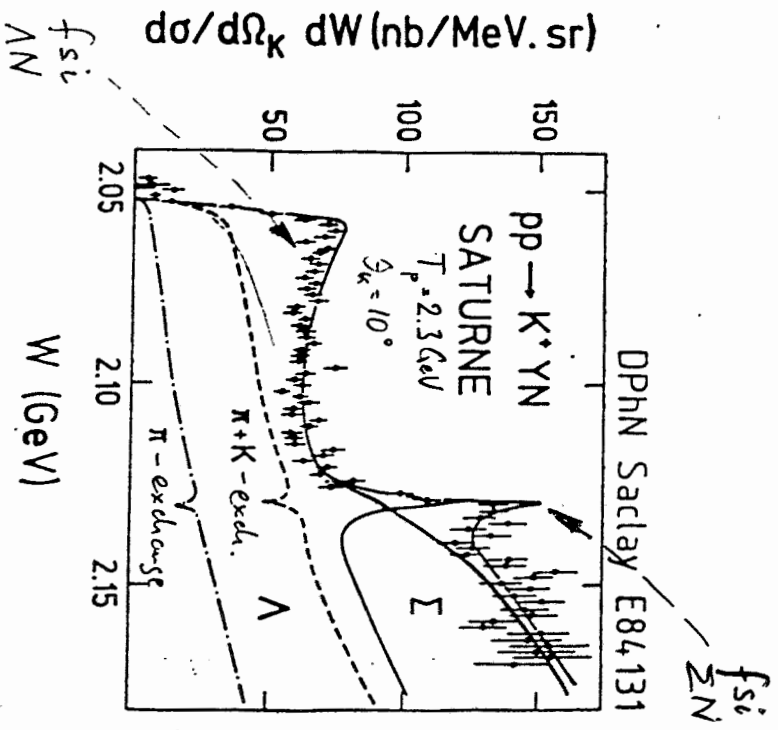


Fig. 4. Laboratory momentum spectra of  $K^+$  mesons produced in hydrogen at the lab angles and incident proton kinetic energies indicated. Errors include statistical errors as well as uncertainties introduced through corrections, but do not include the  $\sim 10\%$  uncertainty in the absolute calibration. Momentum resolution is  $\sim 2\%$ . The dashed lines represent phase space (see text) normalized to the area under the data.

threshold, $NN \rightarrow$	$\sqrt{s}$	$E_{K^+}$	$E_{Lab}$
$NN \rightarrow N \Lambda K^+$	2.548	1.582	
$NN \rightarrow N \Sigma K^+$	2.620	1.780	GeV
$NN \rightarrow N \Lambda^+ K^+$	2.864	2.494	



data: Siebert et al. (8)  
fit: Laget PLB 259, 2

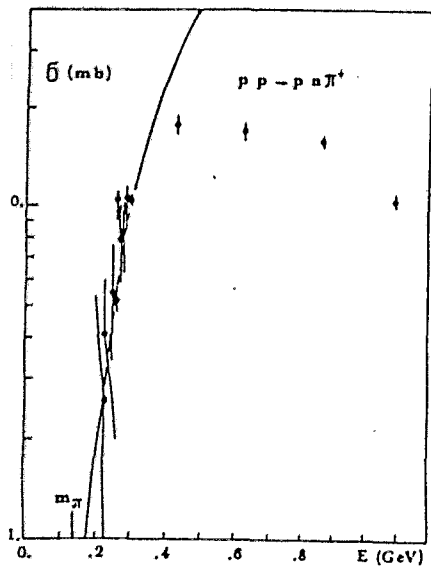


Fig. 2. The cross section of the reaction  $pp \rightarrow pn\pi^+$  versus initial kinetic energy in the CM frame. The data are taken from ref. [5]. The solid line is the prediction of eq. (6) normalized at  $E=0.3$  GeV.

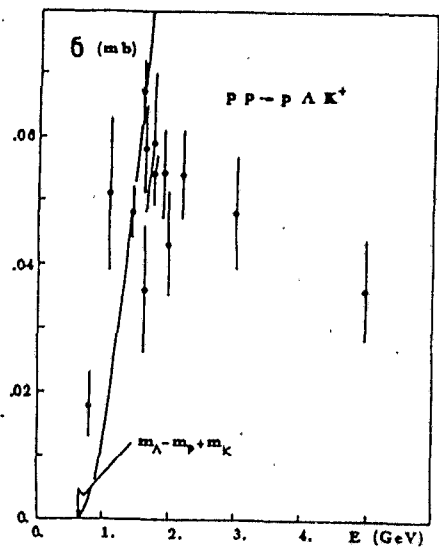


Fig. 3. The cross section of the reaction  $pp \rightarrow p\Lambda K^+$  versus initial kinetic energy in the CM frame. The data are taken from ref. [5]. The solid line is the prediction of eq. (10) normalized at  $E=1.5$  GeV.

# Strangeness suppression at high energies

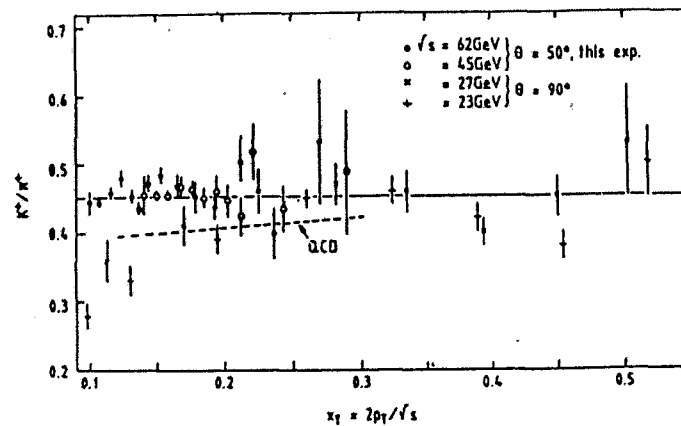


FIGURE 20  
Experimental ratio of  $K^+$  to  $\pi^+$  production in proton-proton interactions at large  $x_T = 2p_T/\sqrt{s}$ . The dashed line shows a model prediction using  $\lambda = 0.5$

$\lambda$ : strangeness suppression factor W. Hofmann NP (90)

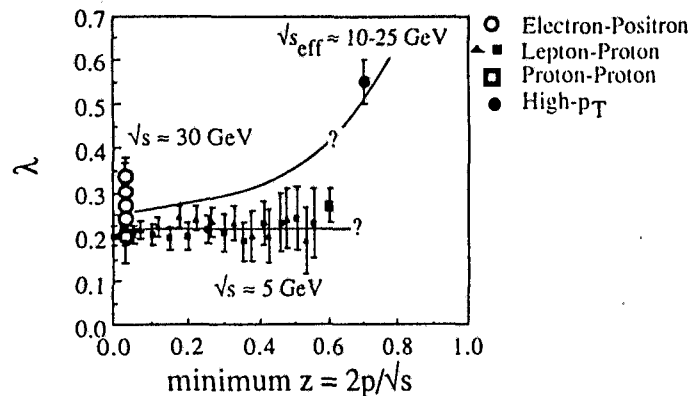
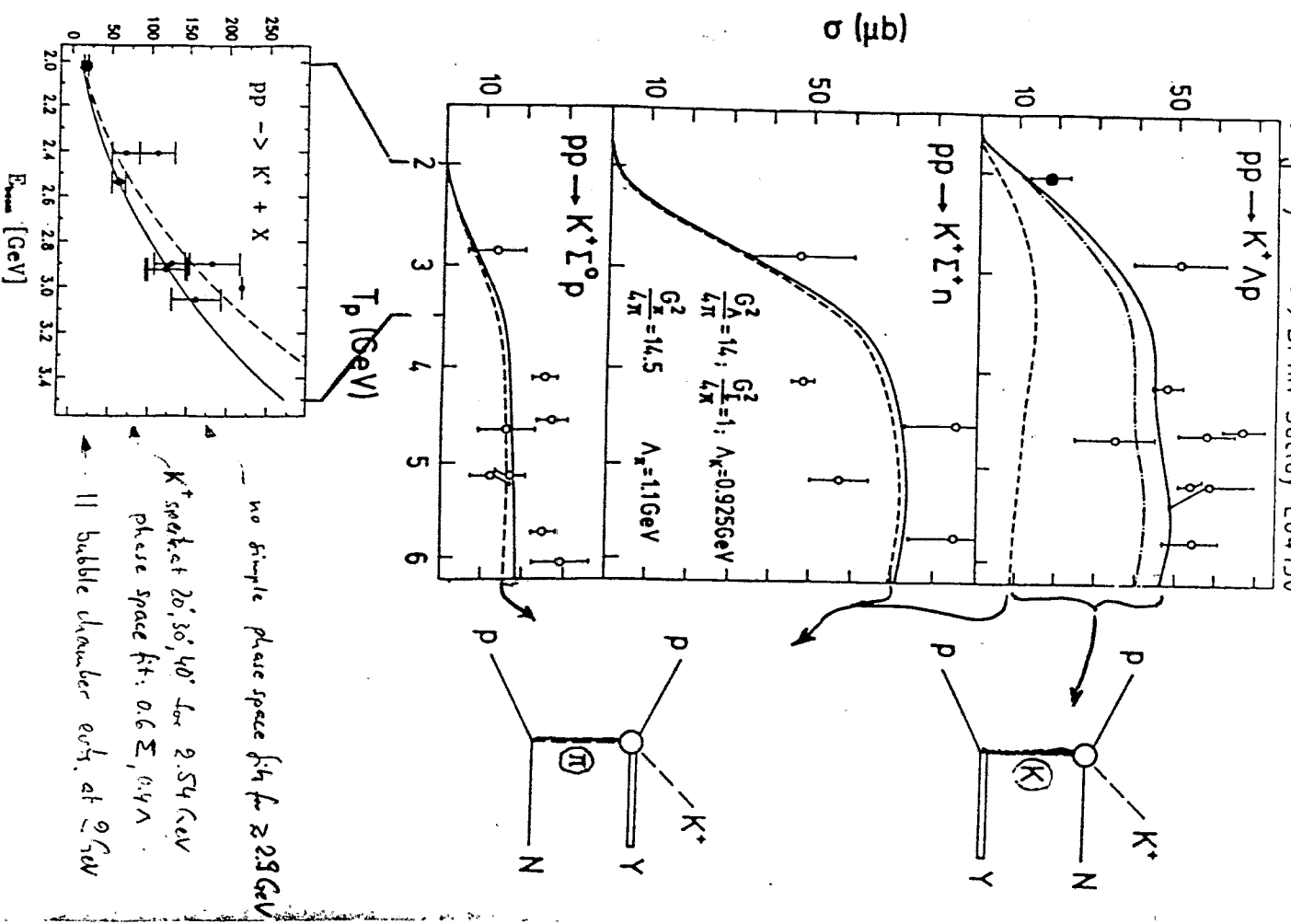
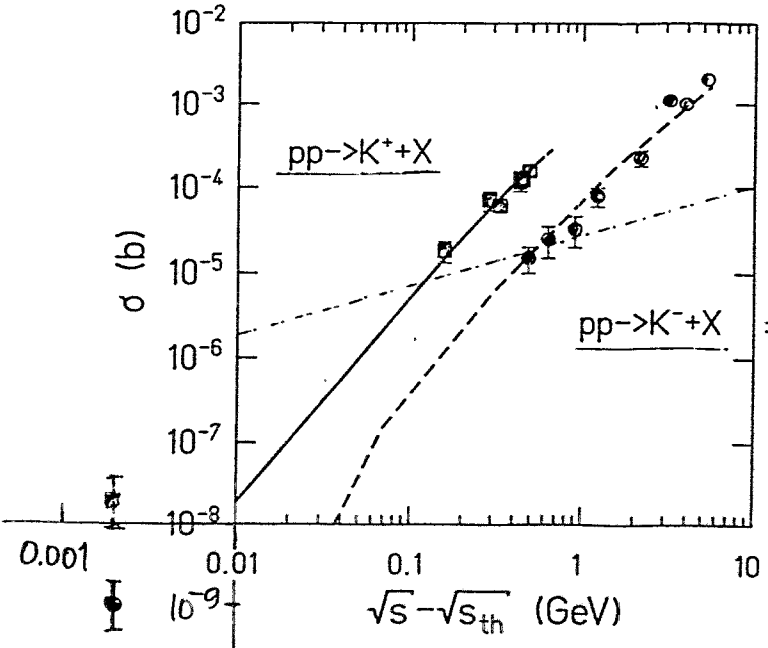


FIGURE 21  
Values of  $\lambda$  as derived from  $K/\pi$  ratios, as a function of the minimum  $z = p_{hadron}/p_{quark}$  above which hadrons are used in the analysis. Data are shown for  $e^+e^-$  annihilation (from several experiments), for neutrino-nucleon scattering, for low- $p_T$  pp reactions and for high- $p_T$  meson production in pp interactions.



Kaons from pp collisions

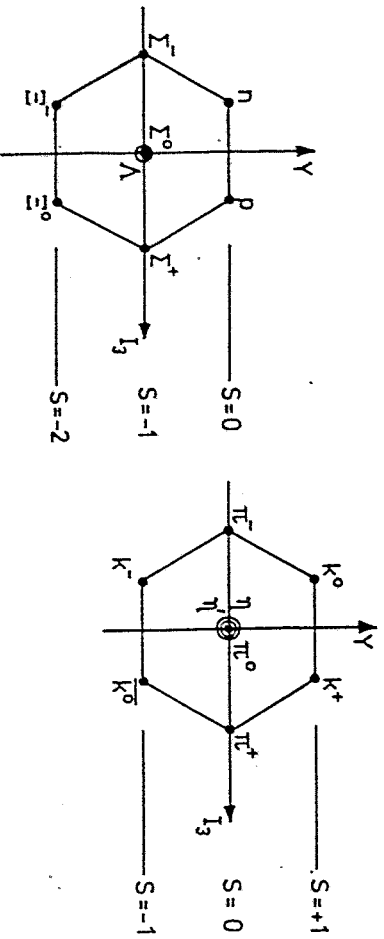


Data compilation:  
 CERN-HERA 84-01  
 Model calculation:  
 H.Müller, Z.Phys. A353 (1995)

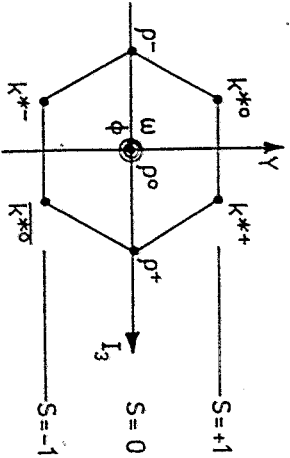
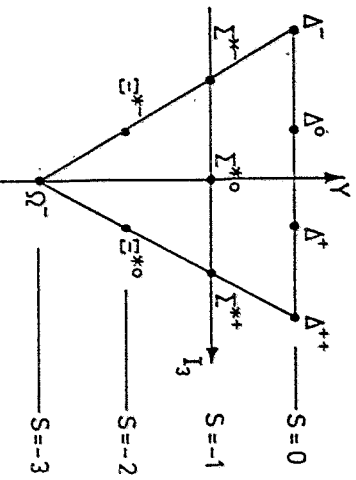
B. Kämpfer Theory Survey



# The Light Hadrons



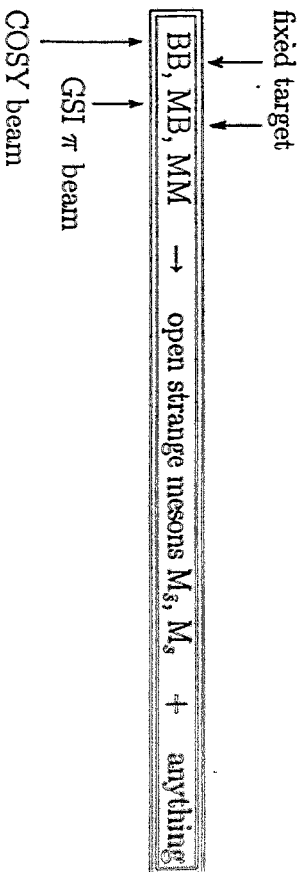
spin flip ↓



$$Y = B + S$$

## Let's Make Strangeness

### I. Elementary Cross Sections



	$u$	$d$	$u$	$d$	
$M_s = q\bar{s} = K^+, K^0$	$u$	$d$	$u$	$d$	$K$
$M_s = \bar{q}s = K^-, \bar{K}^0$	$u$	$d$	$u$	$d$	$\bar{K}$
	scalar		vector		

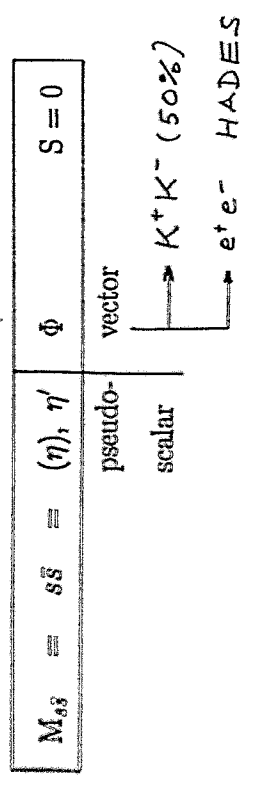
weak interactions with nucleons → long mean free path in nuclei

$K^+ = u\bar{s}$ ;  $K^+ N \leftrightarrow Z^*$  = high-lying

$K^- = \bar{u}s$ ;  $K^- N \leftrightarrow Y^*$  = analog to  $\pi N \leftrightarrow \Delta$

e.g.,  $\Lambda(1405) = \bar{K} N$  bound state or genuine  $3q$  state?

**BB, MB, MM** → hidden strange mesons  $M_{s\bar{s}}$  + anything



in strong interactions: strangeness is conserved

→ associated  $s\bar{s}$  creation

detection possibilities:

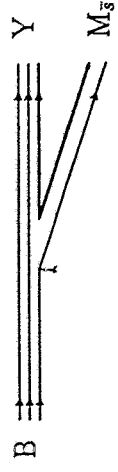
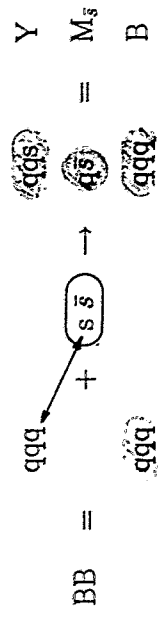
- $K^\pm \rightarrow$  spectrometer ( $cr = 371$  cm)
- or decays  $\pi^\pm \pi^0$  (21%),  $\mu^\pm \nu_\mu$  (68%) ←  $\Delta S = 1$
- $K_S^0 \rightarrow$  decays ( $cr = 2.6 / 1550$  cm)
  - $K_S^0 \rightarrow \pi^+ \pi^-$  (68%),  $\pi^0 \pi^0$  (31%)
  - $K_L^0 \rightarrow 3\pi^0$  (21%),  $\pi^+ \pi^- \pi^0$  (12%) ...

### Constituent Quark Combinatoric

$B = qq\bar{q}, M = q\bar{q}, Y = qq\bar{s}, M_s = q\bar{s}, M_{s\bar{s}} = \bar{q}s$

1)  $BB \rightarrow K + \text{anything}$

(i)  $BB \rightarrow KYB$



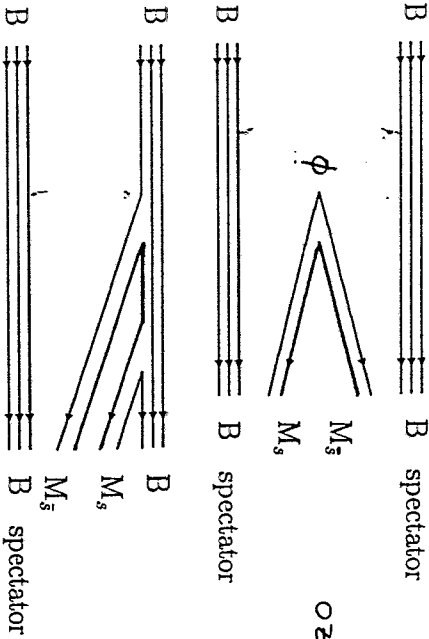
- e.g.  $NN \rightarrow KYN: p^+ p^+ \rightarrow K^+ \Lambda p^+, K^+ \Sigma^+ n, K^0 \Sigma^+ p^+$
- $p^+ n \rightarrow K^+ \Lambda n, K^+ \Sigma^- p^+, K^0 \Sigma^+ n$
- $n n \rightarrow K^+ \Sigma^- n, K^0 \Lambda n, K^0 \Sigma^0 n, K^0 \Sigma^- p^+$

= the easiest way for open anti-strange mesons  $K \alpha \bar{q} s$

open strange mesons would require anti-hyperon (too costly energetically)

(ii)  $BB \rightarrow K\bar{K}BB$

$$BB = qq\bar{q} + \text{circled } s\bar{s} + \text{circled } q\bar{q} \rightarrow \text{circled } s\bar{q} + \text{circled } q\bar{s} = M_s, M_{\bar{s}}$$



OZI forbidden

e.g.  $NN \rightarrow K\bar{K}NN: p^+ p^+ \rightarrow K^+ K^- p^+ p^+$

$p^+ n \rightarrow K^+ K^- p^+ n$

$n n \rightarrow K^+ K^- n n$

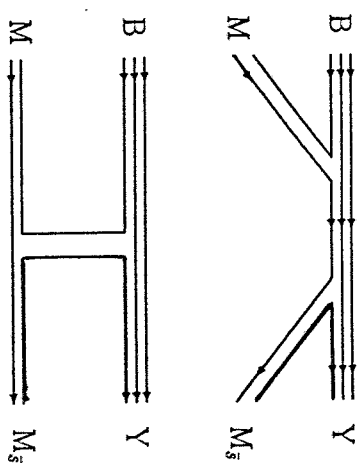
= the easiest way for open strange mesons

anti-leukons

2)  $MB \rightarrow K + \text{anything}$

(i)  $MB \rightarrow KY$

$$MB = qq\bar{q} + \text{circled } s\bar{s} \rightarrow \text{circled } q\bar{q} + \text{circled } q\bar{s} = Y$$



resonance diagram

s channel

pole diagram

t channel

e.g.  $\pi N \rightarrow KYN: \pi^- p \rightarrow K^0 \Lambda, K^+ \Sigma^-, K^0 \Sigma^0$

$\pi^0 p \rightarrow K^+ \Lambda, K^+ \Sigma^0, K^0 \Sigma^+$

$\pi^+ p \rightarrow K^+ \Sigma^+$

$\pi^- n \rightarrow K^0 \Sigma^-$

$\pi^0 n \rightarrow K^0 \Lambda, K^+ \Sigma^-, K^0 \Sigma^0$

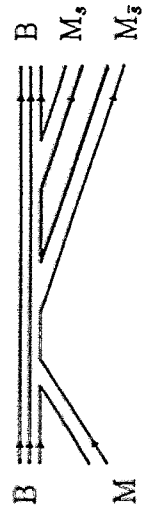
$\pi^+ n \rightarrow K^+ \Lambda, K^+ \Sigma^0, K^0 \Sigma^0$

only open anti-strange mesons

kaons

(ii) MB → K K̄ B

$$MB = qq\bar{q} + q\bar{q}s \rightarrow qq\bar{q} + q\bar{q}s = B \quad M_s \quad M_s$$

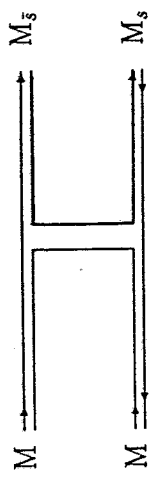
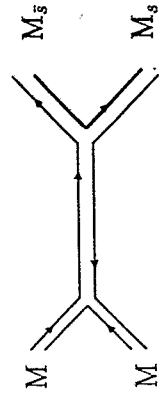


e.g.  $\pi N \rightarrow K \bar{K} N : \pi^0 p^+ \rightarrow K^+ K^- p^+$   
 $\pi^- p^+ \rightarrow K^+ K^- n$   
 $\pi^+ p^+ \rightarrow K^+ K^- p^+$

and the same for  $\pi n$

3) MM → M\_s M\_s

$$MM = (q\bar{q}) + (s\bar{s}) \rightarrow (q\bar{q}s\bar{s}) = M_s \quad M_s$$



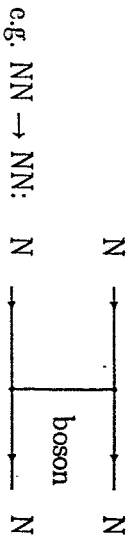
e.g.  $\pi\pi \rightarrow K \bar{K} : \pi^+ \pi^- \rightarrow K^+ K^-, K^0 \bar{K}^0$   
 $\pi^0 \pi^0 \rightarrow K^+ K^-, K^0 \bar{K}^0$   
 $\pi^- \pi^0 \rightarrow K^- K^0$   
 $\pi^+ \pi^0 \rightarrow K^+ \bar{K}^0$

at high energies also the heavier mesons contribute

# Theory

does not exist; only models & parametrizations

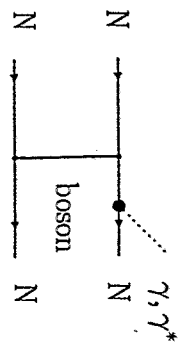
one possibility: utilize OBE model philosophy



e.g.  $NN \rightarrow NN$ :  $N \quad N$

advantage: well defined via Lagrangian + Feynman diagrammatics

+ extension possibilities  $\rightarrow$  bremsstrahlung & di-electrons:



disadvantages: - effective theory,

- only tree level

- parameter fiddling: masses, couplings, cut-offs

e.g. NN scattering: 4 bosons

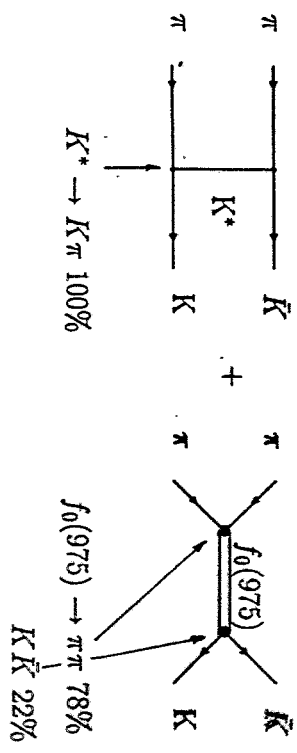
NN scattering + deuteron bound state: 6 bosons

- no simple initial/final state interaction corrections

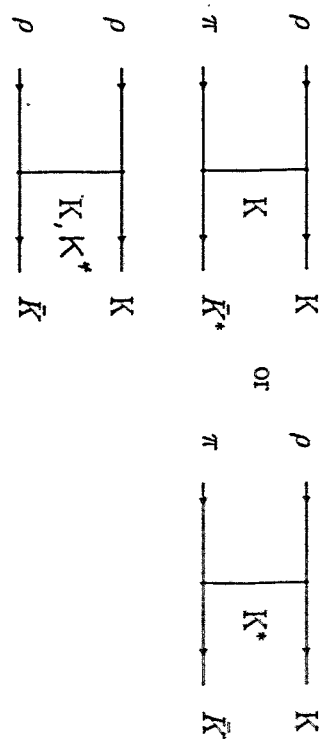
nevertheless: try the same here

# 1) $MM \rightarrow K \bar{K}$ is simplest

Brown/Ko/Wu/Li (1991):



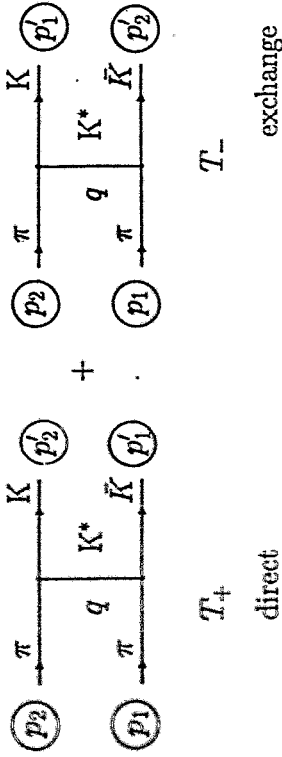
analog:



\*for simplicity we neglect\* ... diagrams  $\rightarrow$  incomplete calculation

Technicalities

example: only the pole diagram



$$|M|^2 = |T_+|^2 + |T_-|^2 + 2\text{Re}(T_+^* T_-)$$

↑  
interference term

N diagrams  $\rightarrow \frac{1}{2}N(N+1)$  terms  $\rightarrow$  explosion of computational efforts

$$\mathcal{L} = g (K_a^* \vec{\tau}_a K_b K_6 (\partial_\mu \vec{\pi}) - K^{*\mu} \vec{\tau} (\partial_\mu K) \vec{\pi}) \quad a, b = 1, 2$$

$\mathcal{L}$  = Lorentz invariant, parity invariant, particle-anti-particle symmetric,

iso-scalar

$K^*$  = vector  $\rightarrow K^{*\mu} \rightarrow$  derivative coupling is needed  
 $\rightarrow \partial_\mu \vec{\pi}$  and/or  $\partial_\mu K$

$\pi$  = iso-vector  $\rightarrow \vec{\pi}$  in iso-spin 3 space

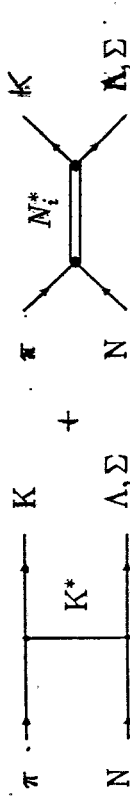
$K$  = iso-doublets  $\rightarrow (K^+, K^0), (K^-, \bar{K}^0), (K^{*+}, K^{*0}), (K^{*-}, \bar{K}^{*0})$ ,  
 with  $\vec{\tau} = 2 \times 2$  matrix contracted

formfactor at each vertex:  $F(q) = \frac{m^2 - \Lambda^2}{q^2 - \Lambda^2}$

2) MB  $\rightarrow$  KY

Brown/Ko/Wu/Li (1991): only rough estimates; no interference terms

Fessler & Huang, Tsuchida, ... (1994 - 1996): systematic approach



$\pi^+ p^+ \rightarrow K^+ \Sigma^+$	$\pi^- p^+ \rightarrow K^+ \Sigma^-$	$\pi^0 p^+ \rightarrow K^+ \Sigma^0$
$\pi^+ n \rightarrow K^+ \Sigma^0$		$\pi^0 n \rightarrow K^+ \Sigma^-$
$\pi^0 p^+ \rightarrow K^0 \Sigma^+$		$\pi^0 p^+ \rightarrow K^0 \Sigma^+$
$\pi^0 n \rightarrow K^0 \Sigma^0$	$\pi^- n \rightarrow K^0 \Sigma^-$	$\pi^0 n \rightarrow K^0 \Sigma^0$
$\pi^0 p^+ \rightarrow K^0 \Lambda$	$\pi^- p^+ \rightarrow K^0 \Lambda$	$\pi^0 p^+ \rightarrow K^+ \Lambda$
		$\pi^0 n \rightarrow K^0 \Sigma^+$

+ inclusion of  $\Delta \rightarrow$  Rarita-Schwinger fields

$\rightarrow \pi \Delta(1232) \rightarrow KY$

decays  $N^*$ ,  $\Delta \rightarrow MB, KY$

$N(1650)$	$P=-1, j=\frac{1}{2}$	$\pi N$	70%	1
		$K \Lambda$	7%	5
		$\pi \Delta$	5%	
$N(1710)$	$P=+1, j=\frac{1}{2}$	$\pi N$	15%	2
		$K \Lambda$	15%	6
		$K \Sigma$	6%	8
		$\pi \Delta$	17%	
$N(1720)$	$P=+1, j=\frac{3}{2}$	$\pi N$	15%	3
		$K \Lambda$	6%	7
		$K \Sigma$	3%	9
		$\pi \Delta$	10%	
$\Delta(1920)$	$P=+1, j=\frac{3}{2}$	$\pi N$	12%	4
		$K \Sigma$	2%	10

interaction Lagrangians for  $\pi NN^*$ :

$$\mathcal{L}_1 = -g_{\pi NN_{1650}} \left( \underbrace{\bar{N}_a^* \vec{\tau}_{ab} N_b}_{\text{Dirac's matrices}} \vec{\pi} + \bar{N}^* \vec{\tau} N^* \vec{\pi} \right), \quad a, b = 1, 2$$

$$\mathcal{L}_2 = -ig_{\pi NN_{1710}} \left( \bar{N}^* \gamma_5^* \vec{\tau} N \vec{\pi} + \bar{N} \gamma_5^* \vec{\tau} N^* \vec{\pi} \right)$$

$$\mathcal{L}_3 = \frac{1}{m_\pi} g_{\pi NN_{1720}} (\bar{N}^{*H} \vec{\tau} N(\partial_\mu \vec{\pi}) + \bar{N} \vec{\tau} N^{*H}(\partial_\mu \vec{\pi}))$$

$$\mathcal{L}_4 = \frac{1}{m_\pi} g_{\pi N \Delta_{1920}} (\bar{\Delta}^\mu \vec{I} N(\partial_\mu \vec{\pi}) + \bar{N} \vec{I}^\mu \Delta^\mu(\partial_\mu \vec{\pi}))$$

↓  
isospin transition operator

interaction Lagrangians for  $KY N^*$ :

$$\mathcal{L}_5 = -g_{K \Lambda N_{1650}} (\bar{N}_a^* \Lambda K_a + \bar{K} \Lambda N^*)$$

$$\mathcal{L}_6 = -ig_{K \Lambda N_{1710}} (\bar{N}^* \gamma_5^* \Lambda K + \bar{K} \Lambda \gamma_5^* N^*)$$

$$\mathcal{L}_7 = \frac{1}{m_K} g_{K \Lambda N_{1720}} (\bar{N}^{*H} \Lambda(\partial_\mu K) + (\partial_\mu \bar{K}) \Lambda N^* N^{*H})$$

$$\mathcal{L}_8 = -ig_{K \Sigma N_{1710}} (\bar{N}^* \gamma_5^* \vec{\tau} \Sigma K + \bar{K} \vec{\Sigma} \vec{\tau} \gamma_5^* N^*)$$

$$\mathcal{L}_9 = \frac{1}{m_K} g_{K \Sigma N_{1720}} (\bar{N}^{*H} \vec{\tau} \Sigma(\partial_\mu K) + (\partial_\mu \bar{K}) \vec{\Sigma} \vec{\tau} N^*)$$

$$\mathcal{L}_{10} = \frac{1}{m_K} g_{K \Sigma \Delta_{1720}} (\bar{\Delta}^\mu \vec{I} \Sigma(\partial_\mu K) + (\partial_\mu \bar{K}) \vec{\Sigma} \vec{I} \Delta^\mu)$$

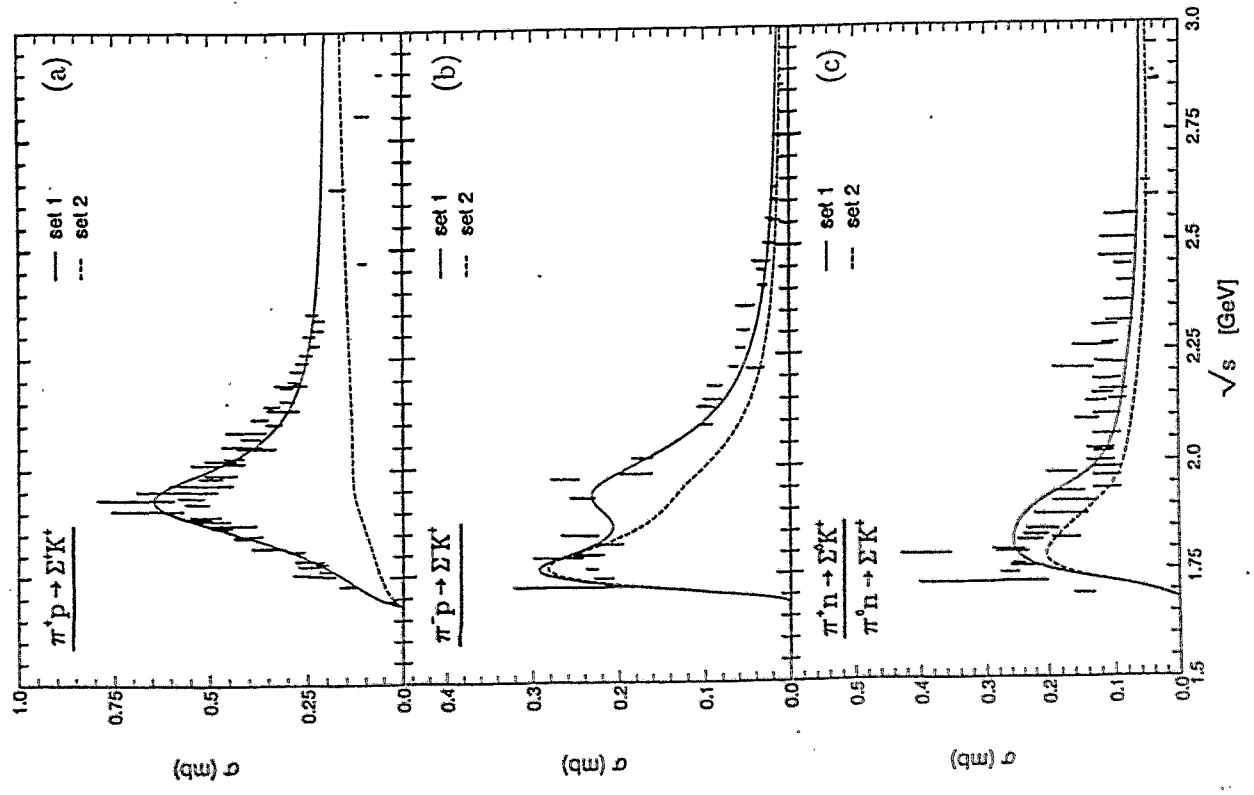
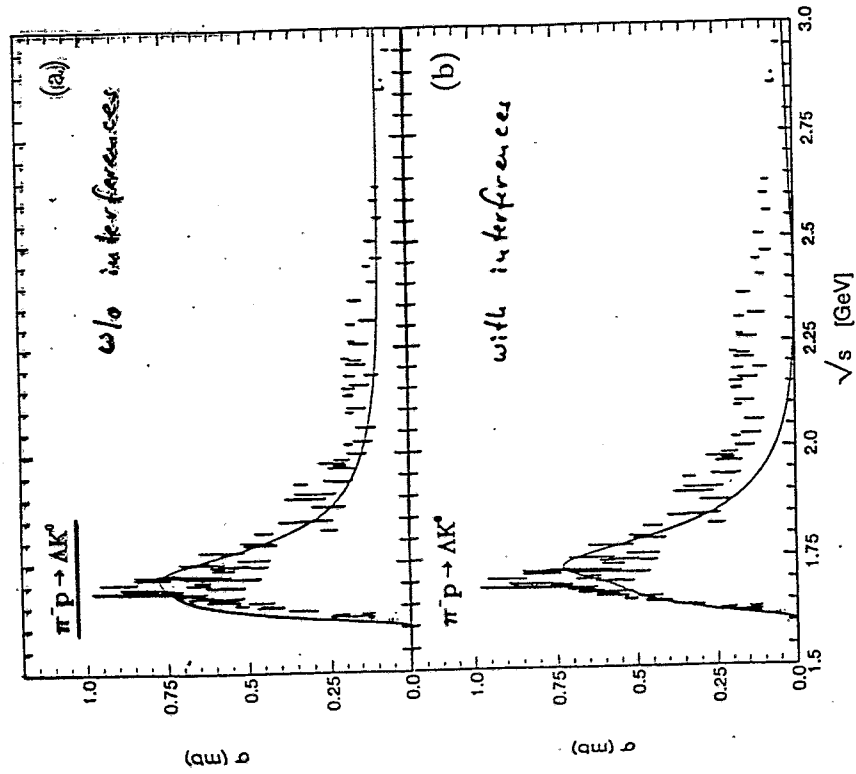
$QE D, QCD$  look simpler

also for couplings for  $K^*$

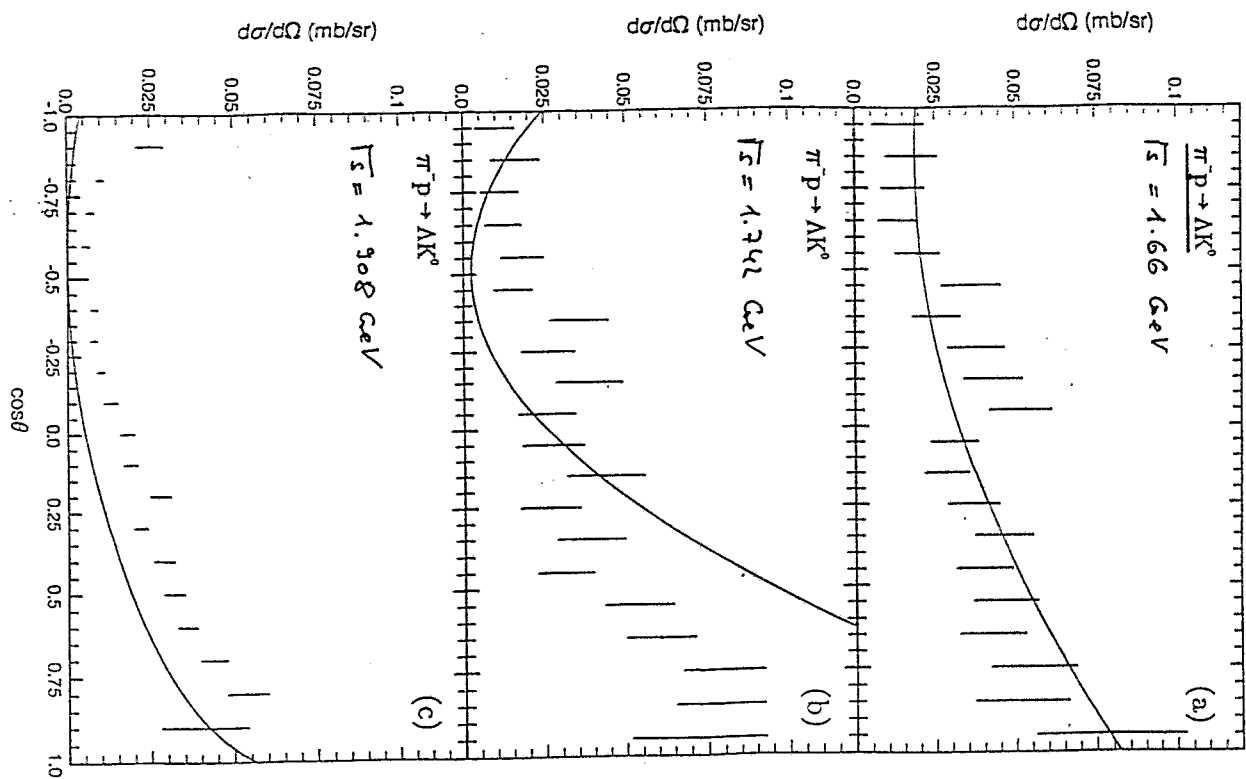
$\Sigma$  = iso-triplet:  $\vec{\Sigma} = (\Sigma^\pm, \Sigma^0)$

+ formfactors on each vertex

→ results of Faessler's group → figs.



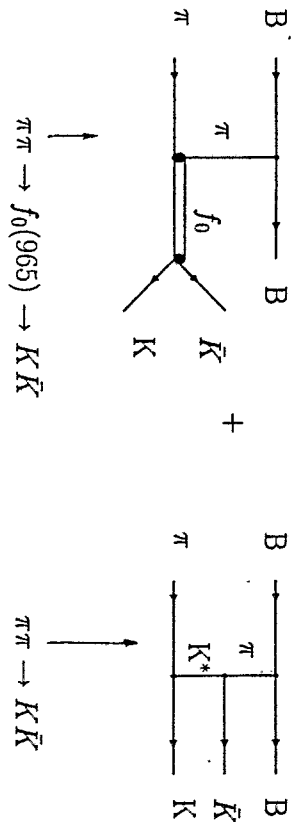




3)  $MB \rightarrow K \bar{K} B$

nothing exists

however: using the above vertices one can continue with



should one measure this at GSI  
with kaons ?

4) BB → KYB

(i) nothing complete exists

announcement of A. Faessler: continue with the above OBE model

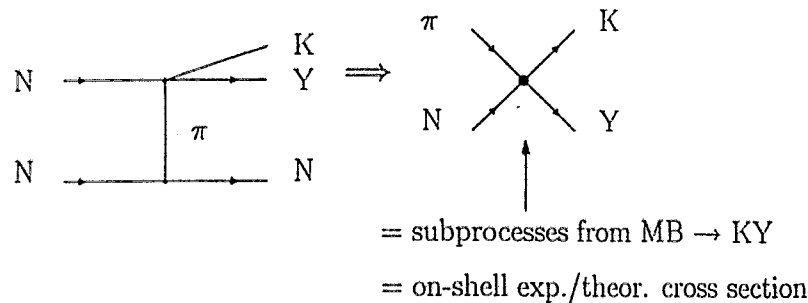
the above MB → KY diagrams = subprocesses here

should we start also such work? (e.g., Ph.D. work for M. Hentschel?)

(e.g., postdoc work of E.E. Kolomeitsev?)

(ii) earlier attempts:

	exchange	interference	$\Delta$	FSI
Ferrari (1960)	$\pi$ or K	+	-	-
Yao (1960)	$\pi$	-	-	-
Randrup/Ko (1980)	$\pi$	-	-	-
Wu/Ko (1989),	"	"	"	"
Brown/Ko/Wu/Xia (1991)	"	"	"	"
Deloff (1989)	$\pi, K$	?	-	+
Laget (1991)	$\pi, K$	-	+	-
Sibirskiy (1995)	$\pi, K$	-	+	-
Li/Ko (1996)	$\pi, K$	-	+	-

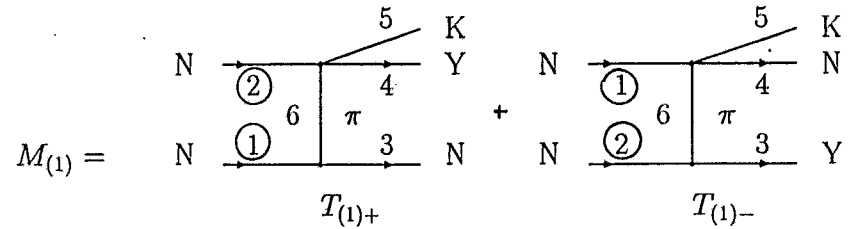


also for  $N \Delta \rightarrow KNY$

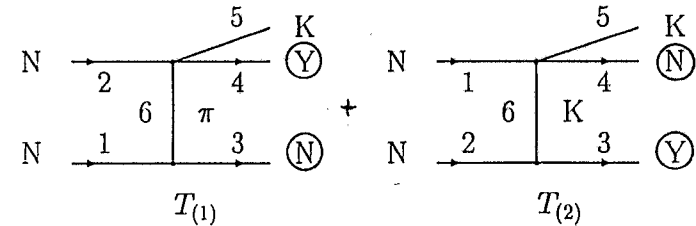
● without spinor dynamics

$$M \propto (\bar{u}_3 \Gamma_6 u_1) \mathcal{D}_\pi(6) (\bar{u}_4 \Gamma_6 u_2) K_5$$

● without interference terms



$$|M|^2 = T_{(1)+}^2 + T_{(1)-}^2 - \underbrace{2\text{Re}(T_{(1)+}^* T_{(1)-})}_{\text{neglected}}$$

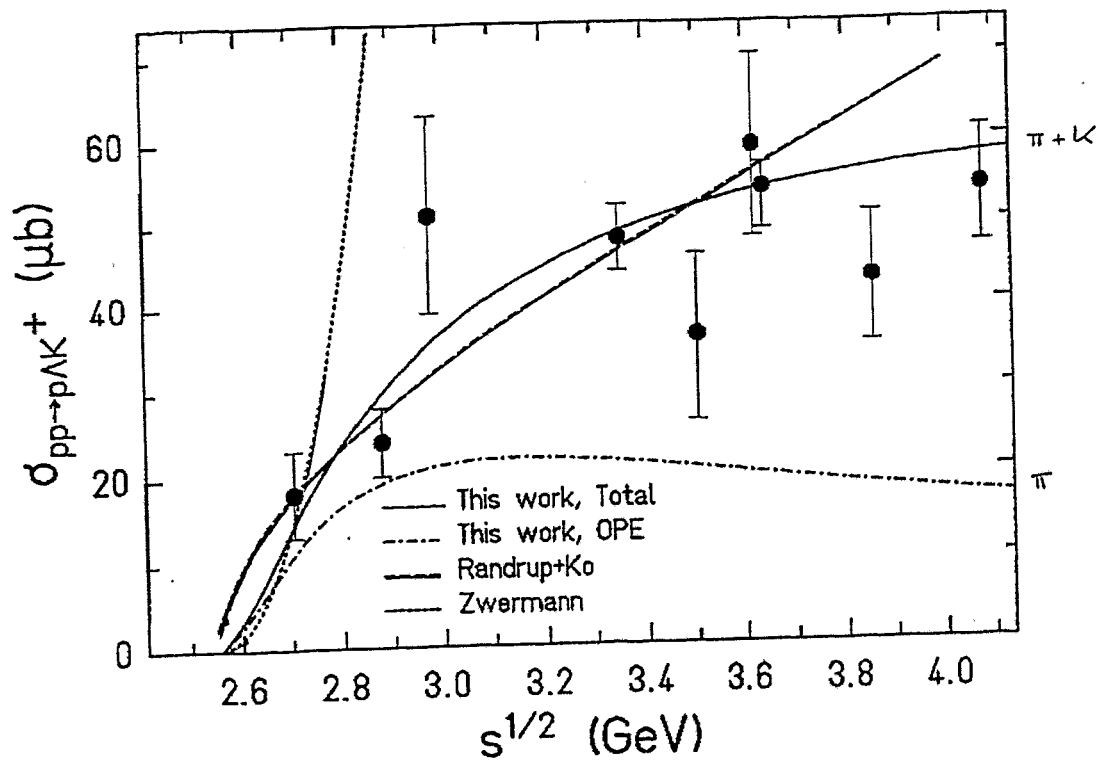


any  $T_{(1)}T_{(2)}$  interference is neglected (→ 10 terms)

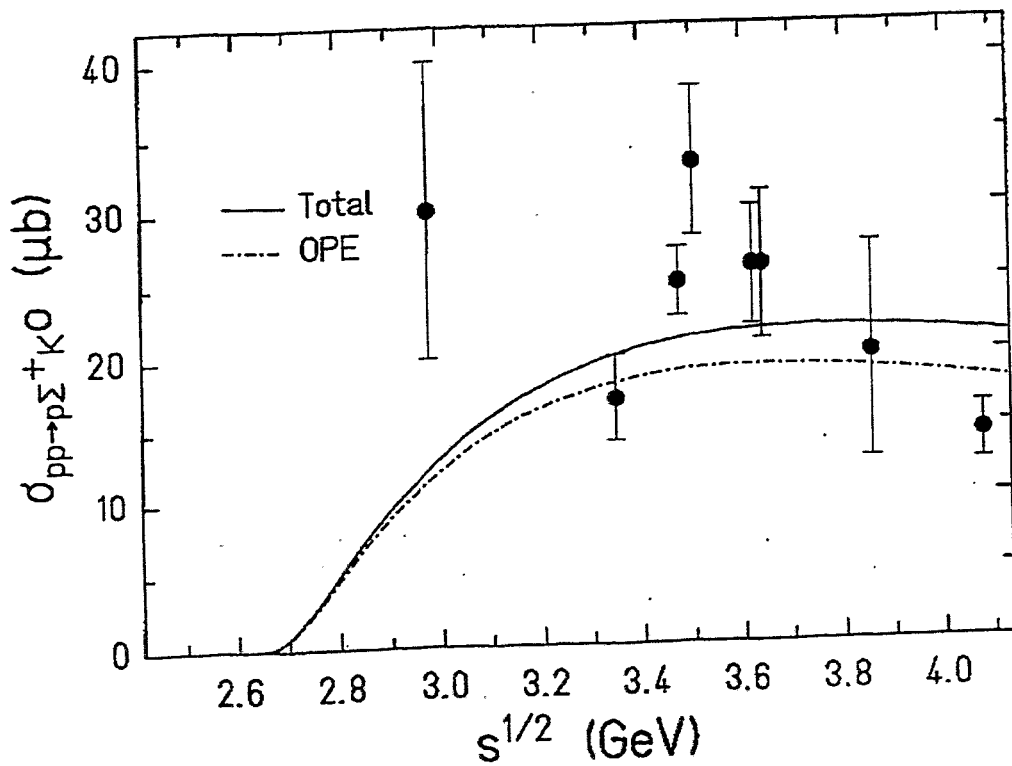
● subprocesses (1)  $\pi N \rightarrow KY$ , (2)  $KN \rightarrow KN$  are put by hand on mass shell

results of Li/Ko → figs.

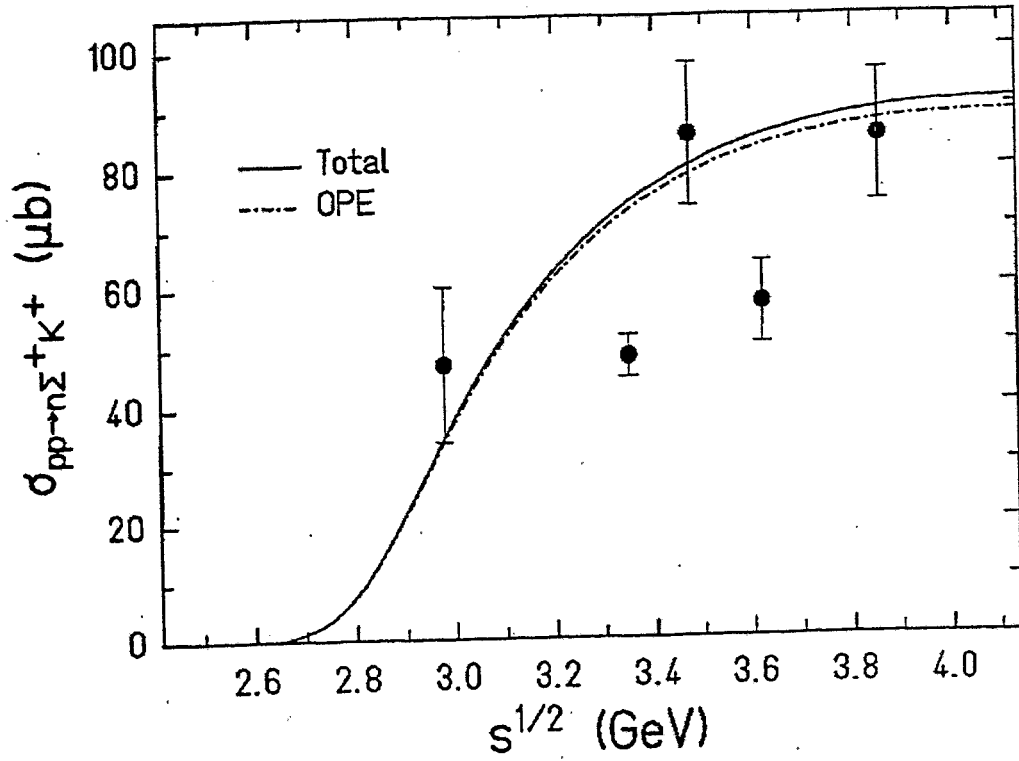
Li/K<sub>0</sub>



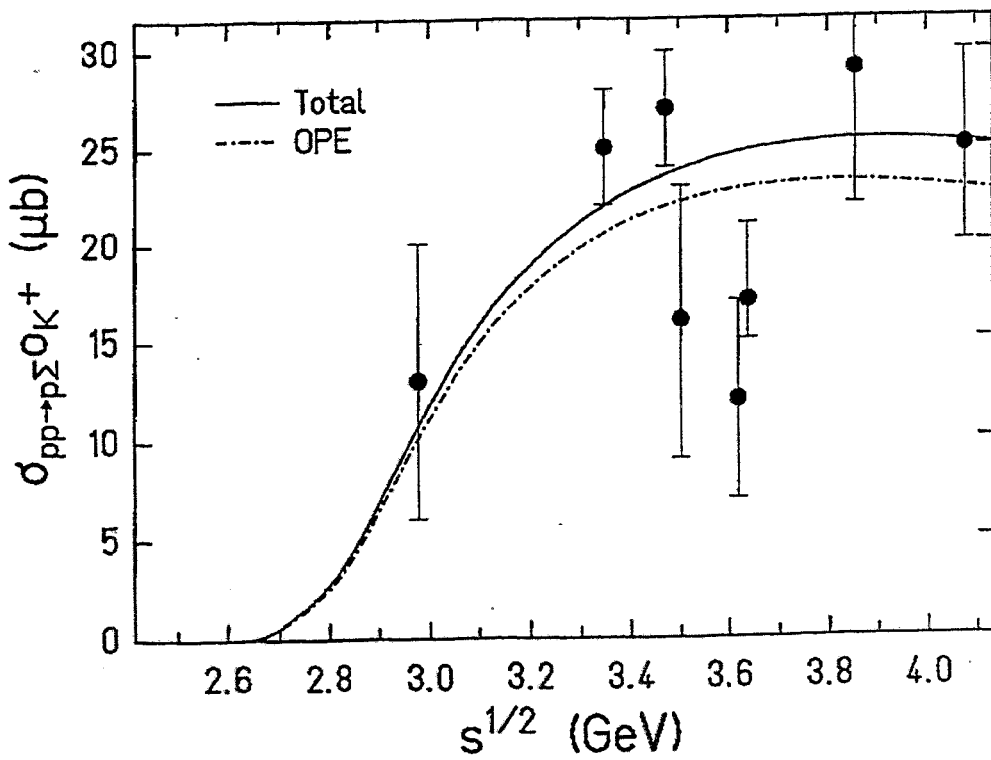
Li/K<sub>0</sub>



Li/ko



Li/ko



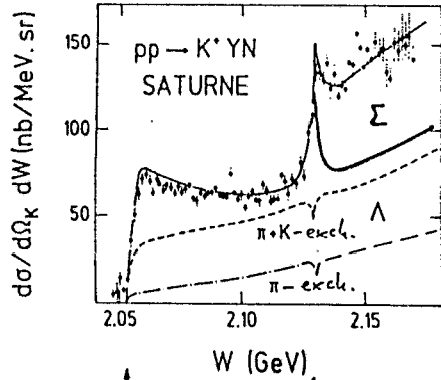
5) BB  $\rightarrow$  K  $\bar{K}$  BB

nothing exists

but one can continue with the above strategy

$\rightarrow$  rather extended work

$E_{lab}^{kin} = 2.3 \text{ GeV}$ ,  $\Theta_{k^+} = 10^\circ$   
missing mass spectrum



Laget (1991)  
FSI, coupl. chan.

thr.  $pp \rightarrow K^+ \Lambda p$   
2.053 GeV

cf. Deloff (1989)

thr.  $pp \rightarrow K^+ \Sigma N$   
2.131 GeV

$\Sigma^0, \Sigma^+$

$W = NY$  eff. mass

## Philosophy

earlier motivation (Bonn/Jülich group):

careful study of interactions on the hadronic level

→ separation of subnuclear (= quark-gluon) degrees of freedom

However:  $\chi$ PT + effective, low-energy models

→ express QCD entirely in terms of hadron observables

→ less space to "check" QCD

hadron interactions = low-energy QCD

to day: lattice QCD →  $M_{hadrons}$

future: lattice QCD →  $\sigma$ ?

let's accumulate as much as possible details

---

---

models are needed, e.g.  $\pi \Delta \rightarrow K \dots$

for HICs

W. Weise:  $s = \begin{cases} \text{heaviest light quark} & \underline{uds} \\ \text{lightest heavy quark} & \underline{scb} \end{cases}$

vacuum structure:  $\langle q\bar{q} \rangle$ ,  $\langle q\bar{s} \rangle$ ,  $\langle \bar{q}s \rangle$

H. Müller    The Rossendorf Collision Model

H. Müller     $K^-$  data from COSY

# A quark model for hadron production

- 1 Introduction
- 2 Rossendorf Collision (ROC) model
  - 2.1 Hadron-Hadron
  - 2.2 Nucleus-Nucleus
- 3 Comparison with experimental results
  - 3.1 Nucleon-Nucleon
  - 3.2 Proton-Nucleus
  - 3.3 Nucleus-Nucleus
- 4 Missing-mass spectra
- 5 Conclusions

## Basic assumptions

- Lorentz-invariant phase-space of  $n$  particles

$$dL_n(s) = \prod_{i=1}^n \frac{d^3 p_i}{2e_i} s^4 \left( p - \sum_{i=1}^n p_i \right)$$

- Probability of populating final channel  $\vec{\alpha}$

$$dW(s; \vec{\alpha}) \propto dL_n(s; \vec{\alpha}) A^2$$

- Differential cross section for channel  $\vec{\alpha}$

$$d\sigma(s; \vec{\alpha}) = \sigma_{in}(s) \frac{dW(s; \vec{\alpha})}{\sum_{\vec{\alpha}} \int dW(s; \vec{\alpha})}$$

Physical quantities are derived by summing up all channels  $\vec{\alpha}$  and integrating over the unobserved variables



# Matrix element

$$A^2(\vec{\alpha}_N) = A_{ex}^2(\vec{\alpha}_N) A_{sc}^2(\vec{\alpha}_N) A_{qs}^2(\vec{\alpha}_N) A_{st}^2(\vec{\alpha}_N)$$

Cluster excitation:

$$A_{ex}^2(\vec{\alpha}_N) = \prod_{I=1}^N \left( \frac{M_I}{\Theta_I} \right) K_1 \left( \frac{M_I}{\Theta_I} \right)$$

Scattering:

$$A_{sc}^2(\vec{\alpha}_N) = \exp(\beta(t_{a1} + t_{b2})) \times \prod_{I=3}^N \exp(- (Q_I/\bar{Q})^2)$$

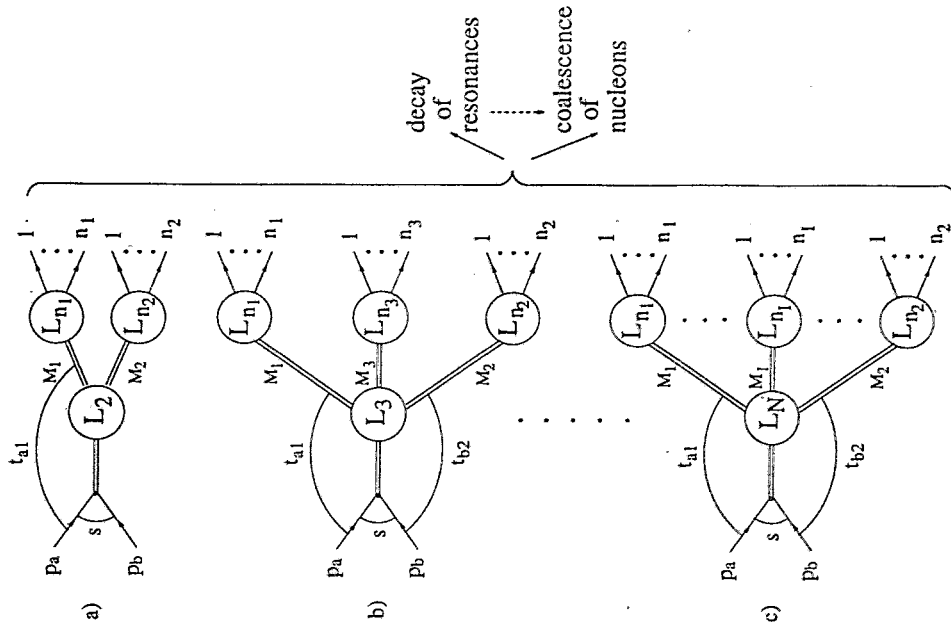
Quark statistics:

$$A_{qs}^2(\vec{\alpha}_N) \rightarrow \text{algorithm}$$

Statistics:

$$A_{st}^2(\vec{\alpha}_N) = \left\{ \prod_{I=1}^N g(\alpha_I) \left( \frac{V_I}{(2\pi)^3} \right)^{n_I-1} \times \left[ \prod_{i=1}^{n_I} (2\sigma_i + 1) 2m_i \right] \right\} \left( \frac{V_N}{(2\pi)^3} \right)^{N-1}$$

# Decomposition of phase-space Hadron-Hadron

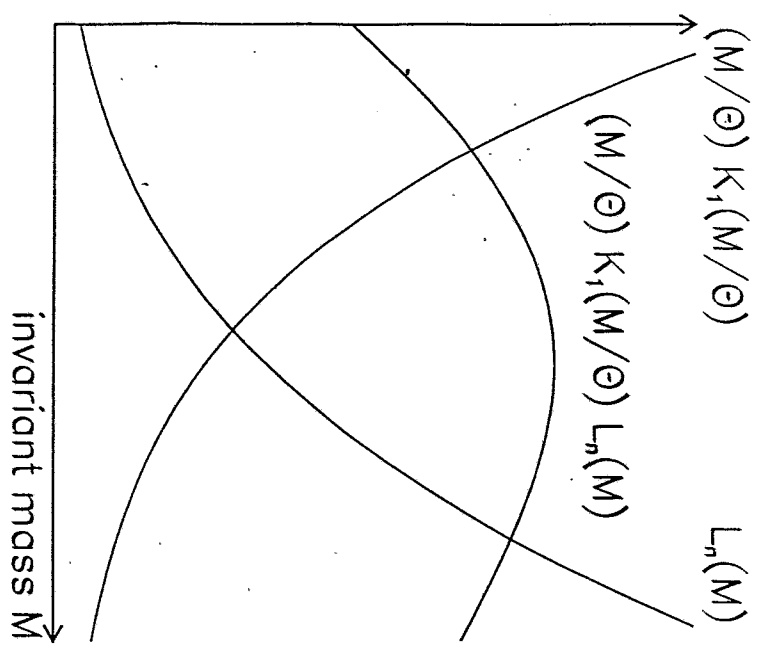


# Excitation

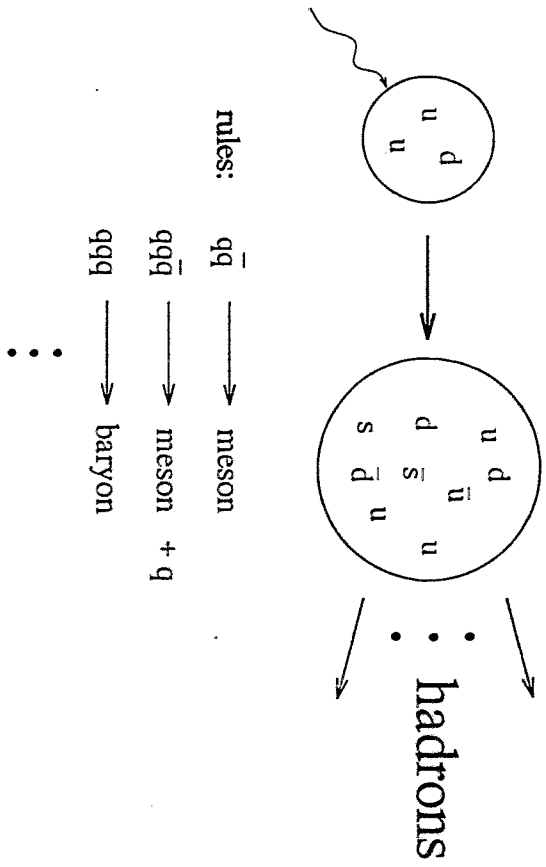
$$A_{ex}^2(\vec{\alpha}_N) = (M/\Theta) K_1(M/\Theta) \sqrt{M/\Theta} \exp(-M/\Theta)$$

$$\xrightarrow{M \rightarrow \infty} 1$$

$$\xrightarrow{M \rightarrow 0} 1$$



## Quark statistics



Hadrons consisting of the same quarks are sampled according to

$$\exp(-m/\Theta)$$

Number of states in the decay channel  $\alpha_I$   
of one cluster

$$dZ_I(\alpha_I) = g(\alpha_I) \left( \frac{V_I}{(2\pi)^3} \right)^{n_I-1} \left\{ \prod_{i=1}^{n_I} (2\alpha_i + 1) 2m_i \right\} dM_I \left( \frac{M_I}{\Theta_I} \right) K_1 \left( \frac{M_I}{\Theta_I} \right) dL_{n_I}(M_I; \alpha_I)$$

Number of "cluster states"

$$dZ_N(s) = \left( \frac{V_N}{(2\pi)^3} \right)^{N-1} \left\{ \prod_{i=1}^N (2M_i) \right\} \exp(\beta(t_{a1} + t_{b2})) \prod_{I=3}^N \exp(-(Q_I/\bar{Q})^2) dL_N(s; M_1, \dots, M_N)$$

Probability of populating channel  
 $\bar{\alpha}_N = (\alpha_1, \dots, \alpha_N)$

$$dW(s; \bar{\alpha}_N) \propto \left\{ \prod_{I=1}^N dZ_I(\alpha_I) \right\} dZ_N(s)$$

## Particle table

$N(S=0, I=1/2)$	10
$\Delta(S=0, I=3/2)$	4
$\Lambda(S=-1, I=0)$	6
$\Sigma(S=-1, I=1)$	2
$\Xi(S=-2, I=1/2)$	2

• Baryons

$^1S_0$	$\pi, K, \eta, \eta'$
$^3S_1$	$\rho, K^*, \omega, \Phi$
$^3P_0$	$a_0, K_0^*, f_0$
$^3P_1$	$a_1, K_1(1280), f_1$
$^3P_2$	$a_2, K_2^*, f_2, f_2'$
$^1P_1$	$b_1, K_1(1400), b_1, h_1$

• Mesons

# Parameters

## Nucleon-Nucleon

Temperature parameter:  $\Theta = 0.3 \text{ GeV}$

→ mean kinetic energy of hadrons in the cluster rest system

Radius parameter:  $R = 1.7 \text{ fm}$

→ mean multiplicity

Slope parameter:  $\beta = 3 \text{ GeV}^{-2}$

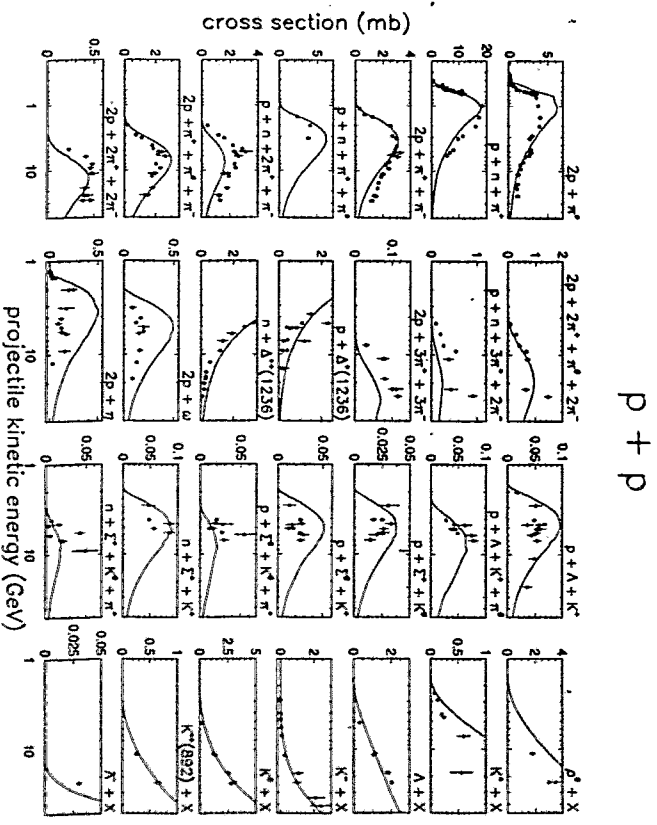
→ distribution of leading clusters

Momentum cut-off:  $\bar{Q} = 0.4 \text{ GeV}/c$

→ transverse dimension of phase-space

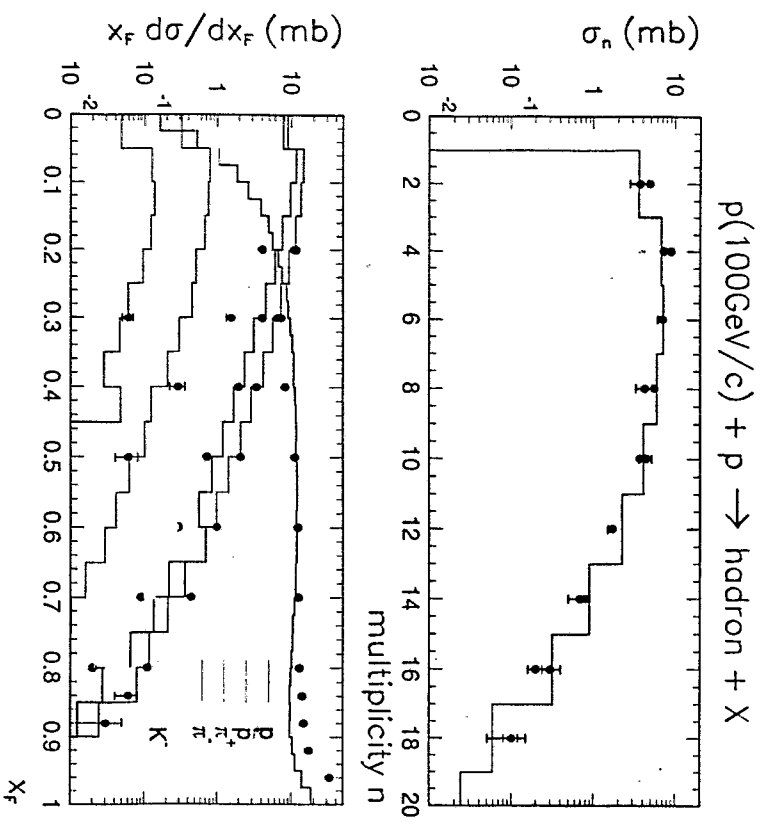
Suppression factor:  $\lambda = 0.15$

→ quarks are sampled according to  $u : d : s = 1 : 1 : \lambda$

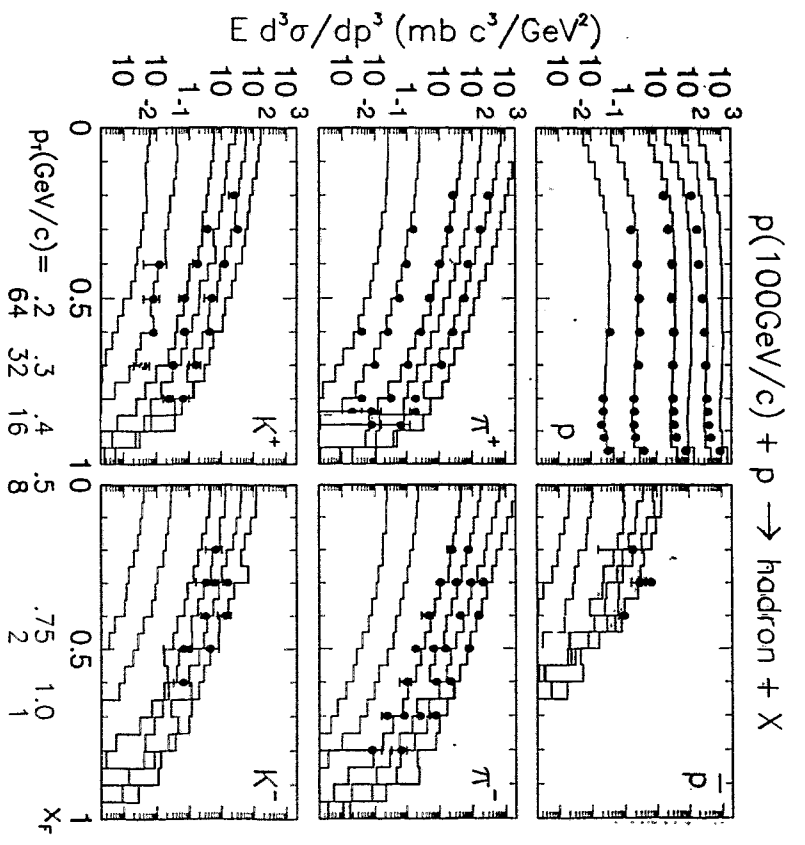


Energy dependence of the cross sections for various particle-production channels in  $pp$  collisions. Experimental data (blue points) are compared with ROC model results (red lines)

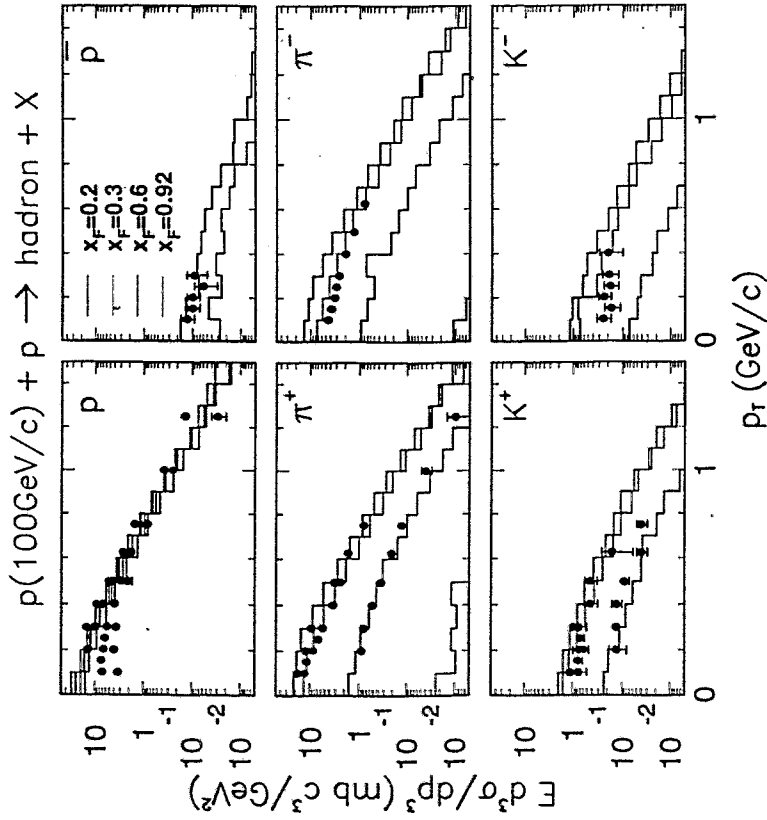




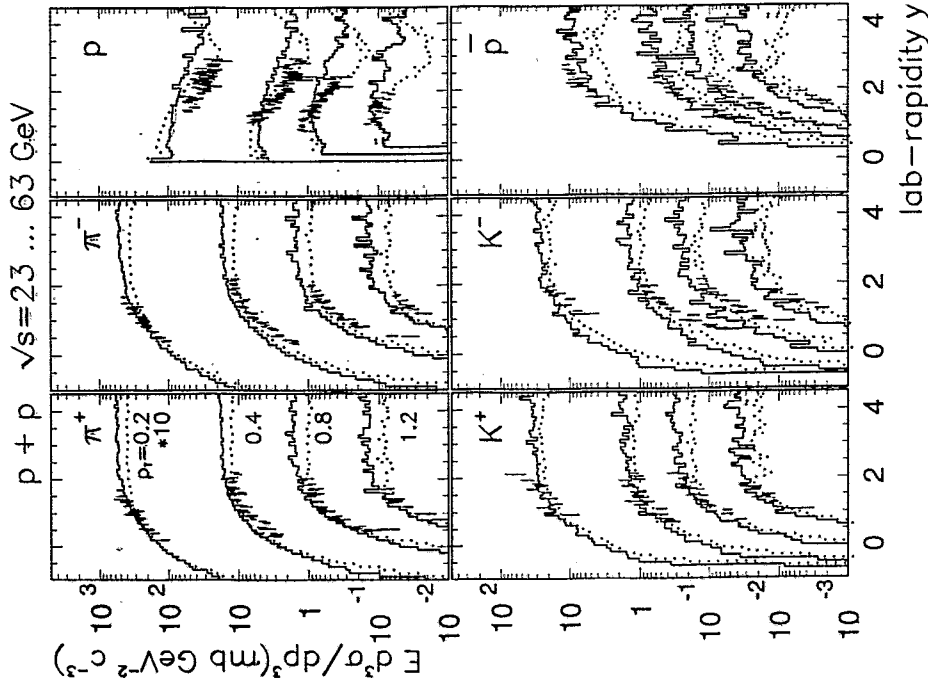
Multiplicity distribution and invariant cross section (integrated over transverse momentum) for hadron production as function of Feynman- $x$ . Points with error bars are experimental data, histograms are ROC model results



Invariant cross section for hadron production as function of Feynman- $x$  for various  $p_T$  values. Points with error bars are experimental data, histograms are ROC model results

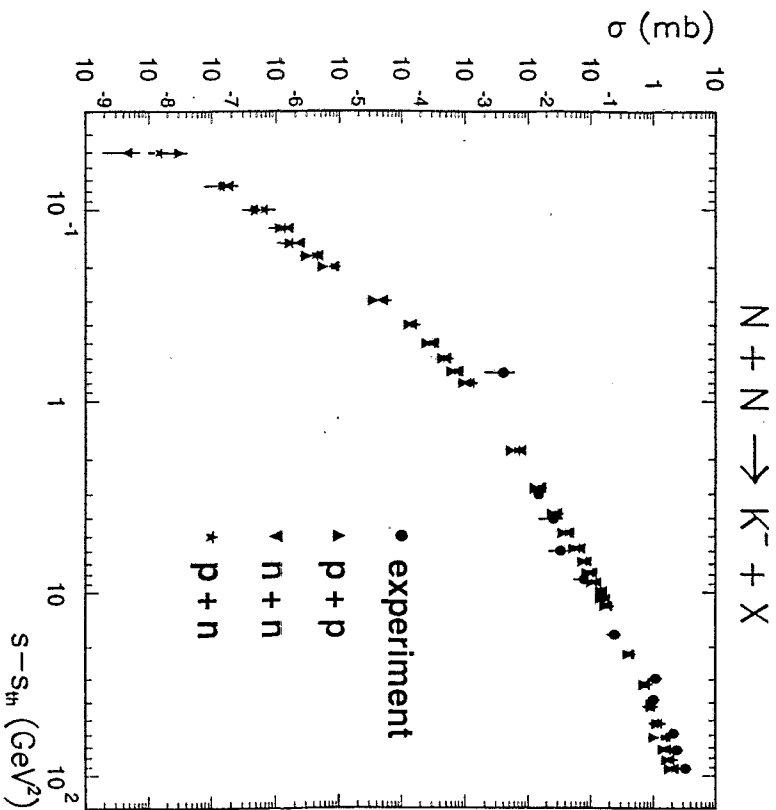


Invariant cross section for hadron production as function of transverse momentum at various  $x_F$  values. Points with error bars are experimental data, histograms are ROC model results

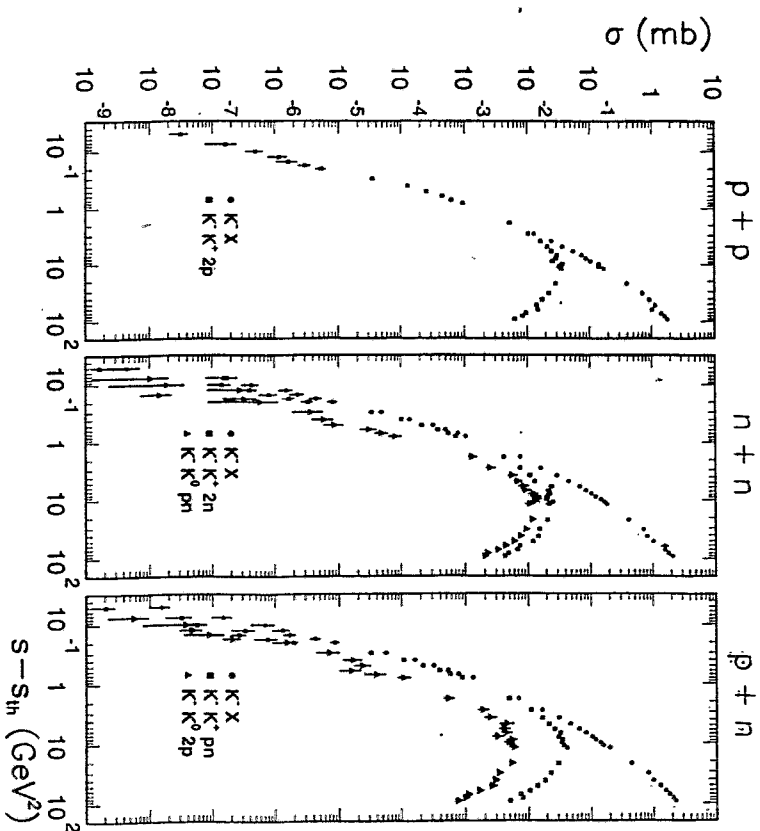


Invariant cross sections for the production of hadrons at different energies and indicated values of transverse momentum as a function of rapidity. Experimental data (colored points) are compared with ROC model results (black histograms: dotted  $\sqrt{s} = 23 \text{ GeV}$ , full  $\sqrt{s} = 63 \text{ GeV}$ )

# Isospin dependence of $K^-$ meson production in nucleon-nucleon interactions

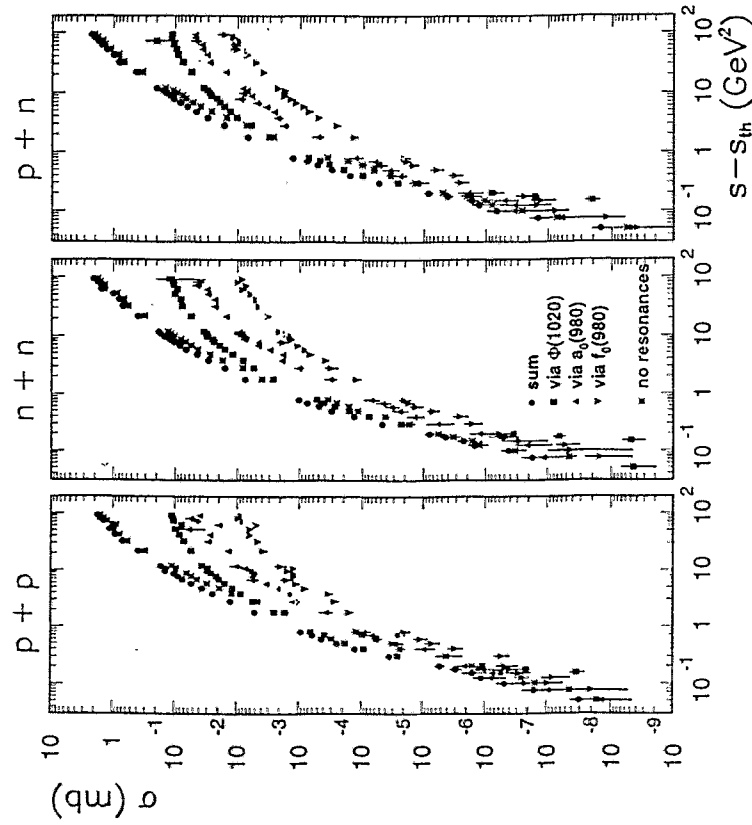


Cross section for inclusive  $K^-$  meson production in  $pp$ ,  $nn$  and  $pn$  interactions as a function of  $s - s_{th}$



Cross section for inclusive and exclusive  $K^-$  meson production in  $pp$ ,  $nn$  and  $pn$  interactions as a function of  $s - s_{th}$





Partial cross section for inclusive  $K^-$  meson production in  $pp$ ,  $nn$  and  $pn$  interactions via resonances as a function of  $s - s_{th}$

# ROC model

## Summary

- unified description of hadronic and nuclear reactions
- simultaneous description of all reaction channels for
  - any projectile-target combination
  - wide energy region
- implemented as Monte-Carlo generator
  - complete events
  - comparison with any experimental results
  - event generator for simulation of experiments

P. Michel  $K^+$  data from COSY

Assoziierte Strangeness-Produktion  
im p-p-Stoß ( $\neq NS$ )  
(COSY-TOF-Kollab. Uni Erlangen)

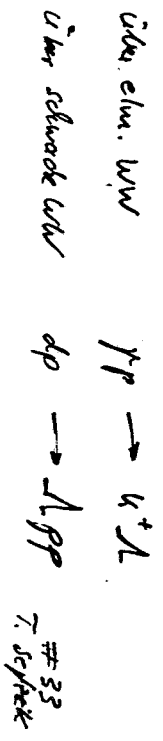
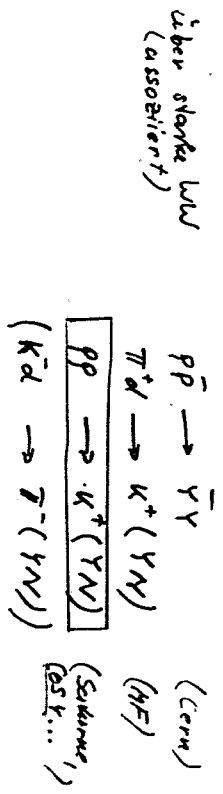
Warum? Konsistente Theorie der Baryon-Baryon-WW

$$\begin{pmatrix} u \\ d \end{pmatrix} \begin{pmatrix} s \\ s \end{pmatrix} \begin{pmatrix} t \\ b \end{pmatrix}$$

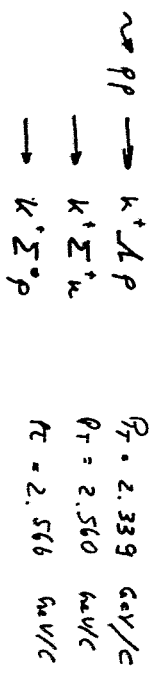
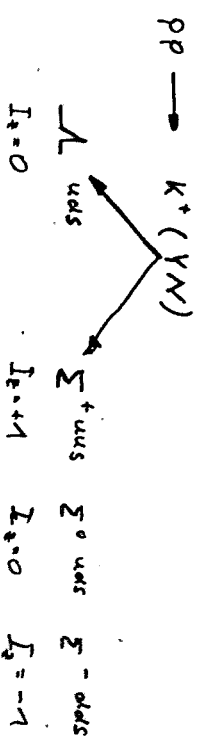
$$\begin{matrix} N \\ N \\ N \end{matrix}$$

- Erzeugungsmechanismus v. Strangeness (Erzeugung im NN-System als Input für Spangensproduz. im N-kern oder Kern-Kernsystem)
- NN-Wechselwirkung als Komponente der Baryon-Baryon-Wechselwirkung (über  $\neq SI$  bei kleineren Reaktive Energien)

Strangenessproduktion:

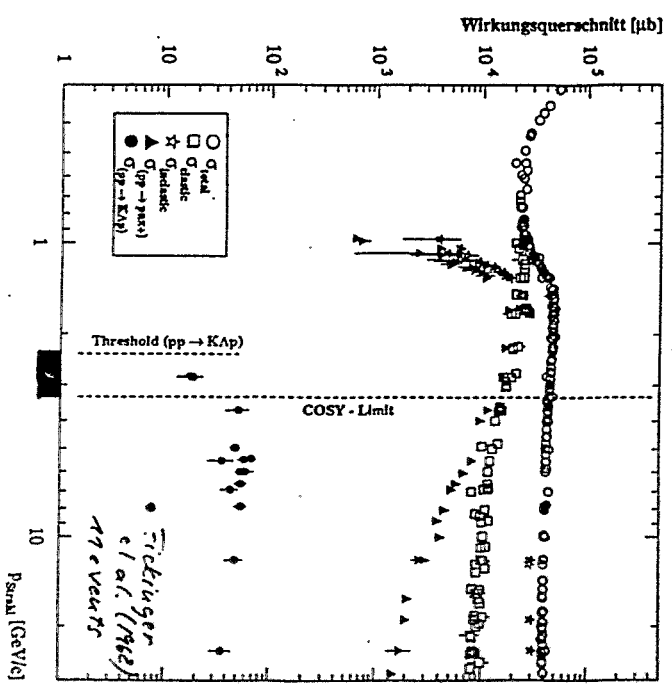


Was geht am COSY?  $R_{\text{max}} = 3.3 \text{ GeV/c}$



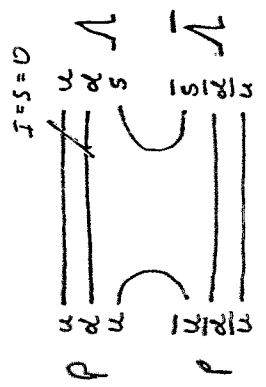
Welt daten vorrat 1985

- (2.2. Satzen 2.3-2.7) kein interne Kennzeichen mit  $K^+$  Nachweis im Kernersystemen keine  $\neq$ -Inform. über reik. Wechselwirkungen,  $\Lambda, \Sigma^+, \Sigma^0, \Sigma^-$  kann nicht gelöst



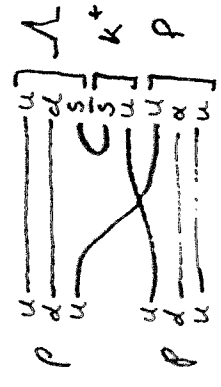
Theoretische Beschreibung

Quark-Gluonen-Modell



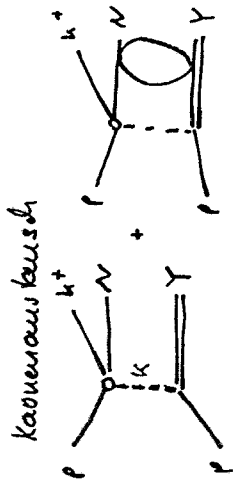
Quarks in  $u, s$ -Zustand  
 $\rightarrow$  (od) koppeln zu  $S = I = 0$   
 $\rightarrow$  Spinobservablen des  $\Lambda$  ( $\bar{\Lambda}$ ) aus Spin einzeln.  
 $v. s(\bar{s})$  unentwickelbar

$pp \rightarrow k^+ p \Lambda$

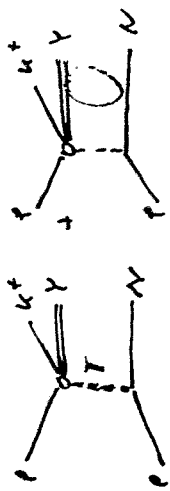


Messung aus Kaon-Modell

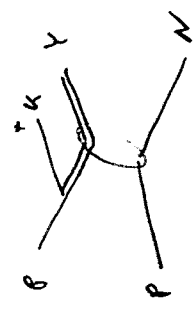
wichtigste Ordnung:



Pionenenaustausch



direkte Kaon-Emission

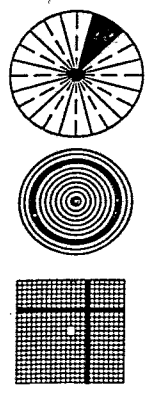
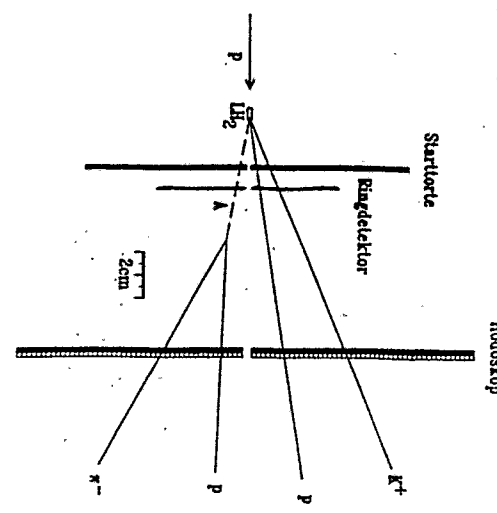
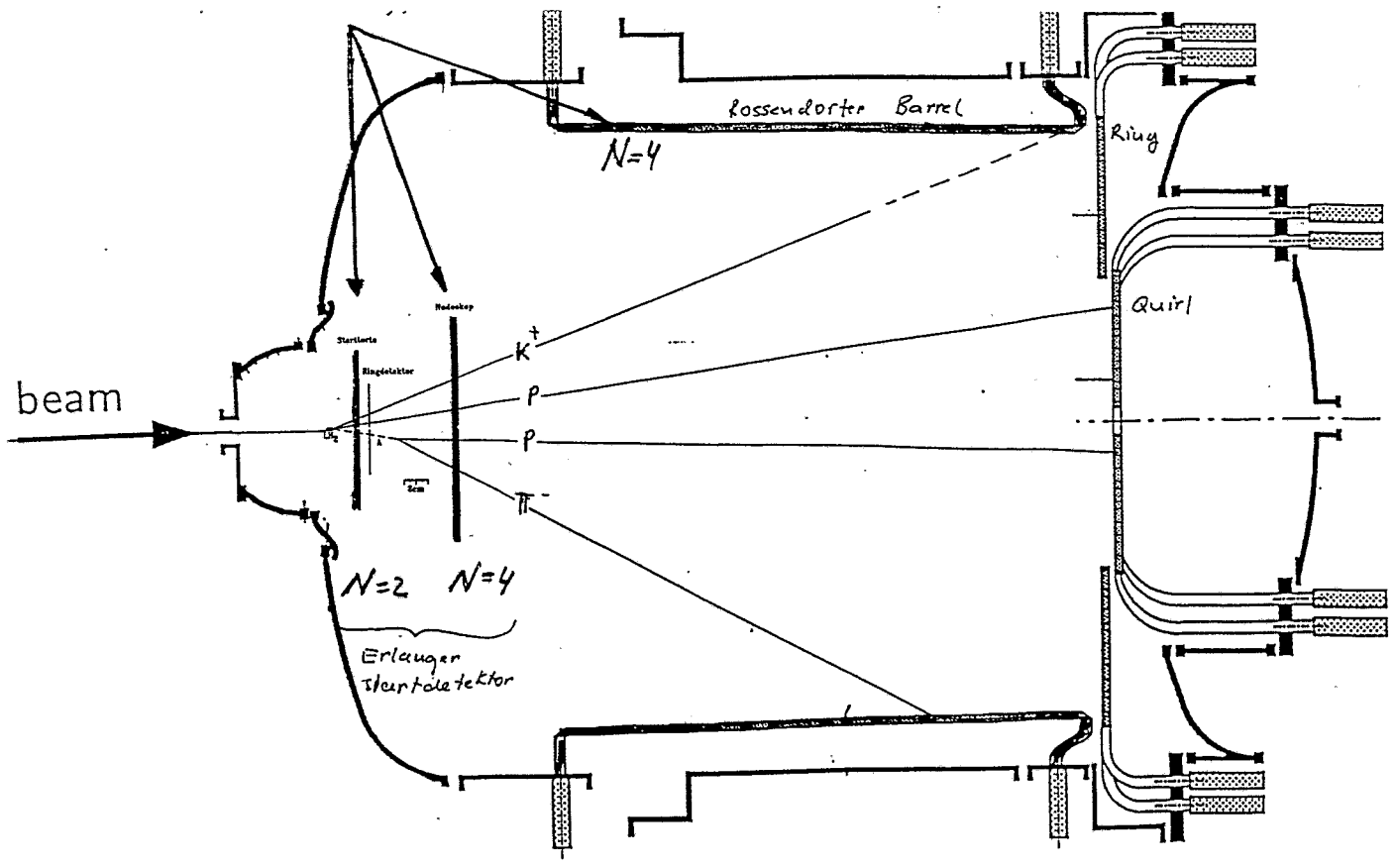


E-Experiment

1. Reaktionskinematik  $pp \rightarrow \dots$

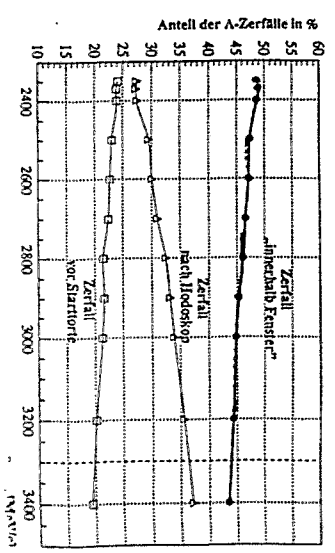
Kanal	$\sigma/\text{barn}$	sek. Zerfall	$N_{\text{ges.}}$	$N_{\text{ausg.}}$	$E_{\text{inc}} = \sum E_i^{\text{kin.}}$
pp	0.42	-	2	0	
$p\pi^+\pi^+$	0.34	$\pi^+ \rightarrow 2.8 \mu m \rightarrow \mu^+ \nu_\mu$	2	0	
$p\pi^0\pi^0$	0.08	$\pi^0 \rightarrow 25 \mu m \rightarrow 2\gamma$	2	0	
$p\pi^+\pi^0$	0.08	...	2	0	
$p\pi^0\pi^0$	0.047	...	2	0	
$p\pi^+\pi^+$	0.001	...	2	0	
$pp\pi^+\pi^-$	0.05	...	4	0	
$p\pi^+\pi^+\pi^0$	0.006	...	4	0	
$p\pi^+\pi^0\pi^0$	0.006	...	4	0	
$p\pi^+\pi^0\pi^+$	0.004	...	4	0	
$k^+ p \Lambda$	0.00027	$k^+ \rightarrow 3.7 \mu m \rightarrow \mu^+ \nu_\mu$ $\Lambda \rightarrow 7.19 \text{cm} \rightarrow p \pi^0 \quad 14\% \quad 36\%$	2	2	$E_{\text{inc}} = \sum E_i^{\text{kin.}}$
$k^+ \Sigma^+ n$		$k^+ \rightarrow$ $\Sigma^+ \rightarrow 2.4 \text{cm} \rightarrow p \pi^0$	2	0	
$k^0 \Sigma^+ p$		$\Sigma^+ \rightarrow$ $k^0 \rightarrow 2.7 \text{cm} \rightarrow \pi^+\pi^0$ $k^0 \rightarrow 16 \mu m \rightarrow$	2	2	$E_{\text{inc}} = \sum E_i^{\text{kin.}} + E_n$ (EV)
$k^+ \Sigma^0 p$		$k^+ \rightarrow$ $\Sigma^0 \rightarrow 20 \text{fm} \rightarrow p \Lambda$	2	2	$E_{\text{inc}} = \sum E_i^{\text{kin.}}$

online Trigger!  
 offline



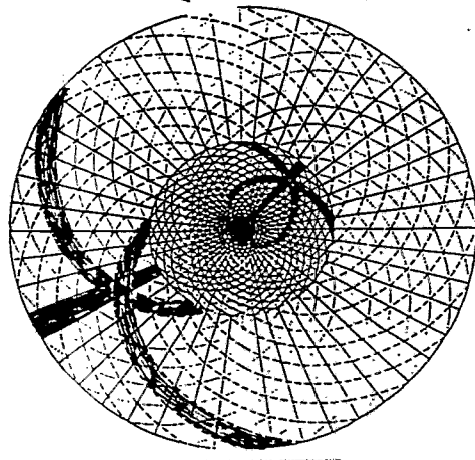
2 Lagen  
 a 12 Segmente  
 Stimulator  
 Si-r-Stellen  
 1mm NEN-04  
 520µm  
 2x2mm<sup>2</sup> BCF72  
 Durchmesser: 2mm  
 φ: 1mm  
 2mm Loch  
 Δt ~ 0.3µs (Lücken) Δt ~ 280µm Δx: 17 NEN-04  
 patch: 10µm  
 34 - 34 µm

- \* K1
- \* M
- \* Δt start
- \* Pi
- \* M
- \* ΔEi
- \* Xi, yi → Pi, Pi
- \* ΔEi



stopadelekt

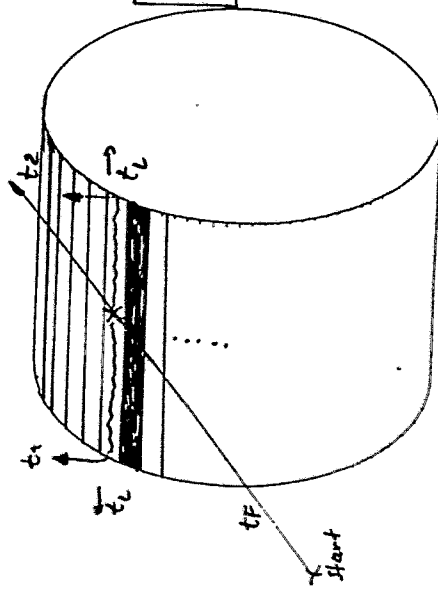
Endkappe:



Ring:  
 96 gerade  
 48 linke  
 48 rechte  
 ϕ: 116 cm - 300 cm

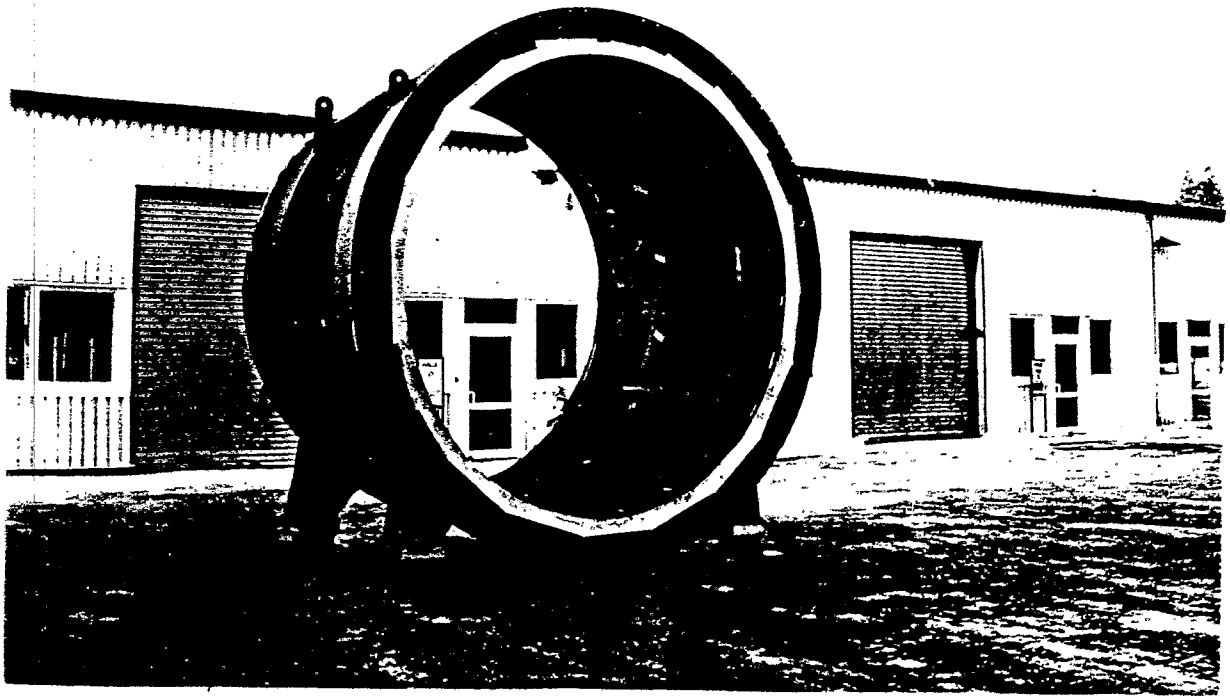
Quint:  
 48 gerade  
 24 linke  
 24 rechte  
 0,5 mm  
 ϕ Innendoch: 8 cm

Baumel:



96 Spinnvliesen NEMOA (Bicron)  
 3000 x 100 x 15 mm

\* M  
 \* ϕ  
 \* t1



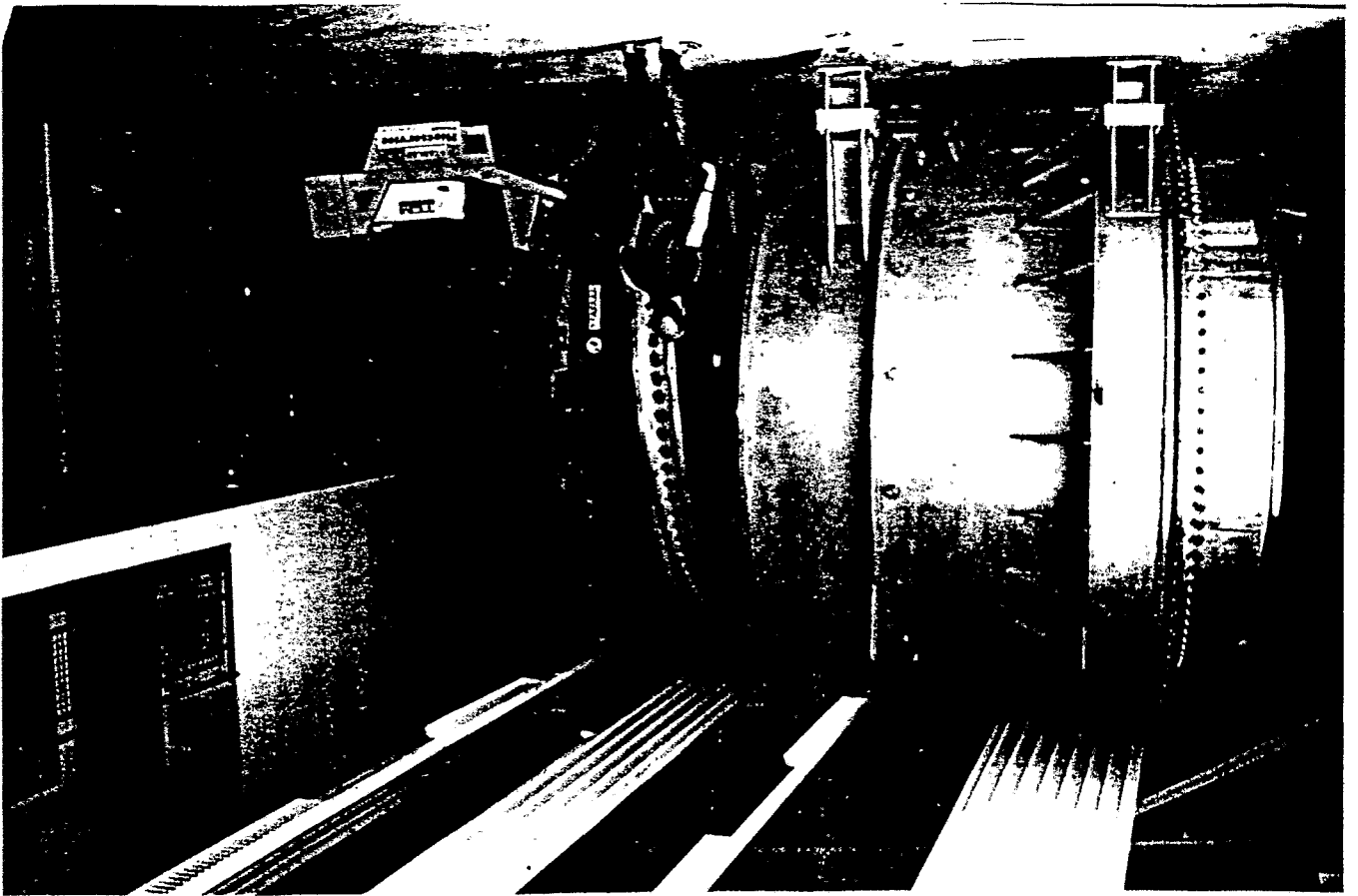
$$t_1 = t_F + t_2$$

$$t_2 = t_F + t_2$$

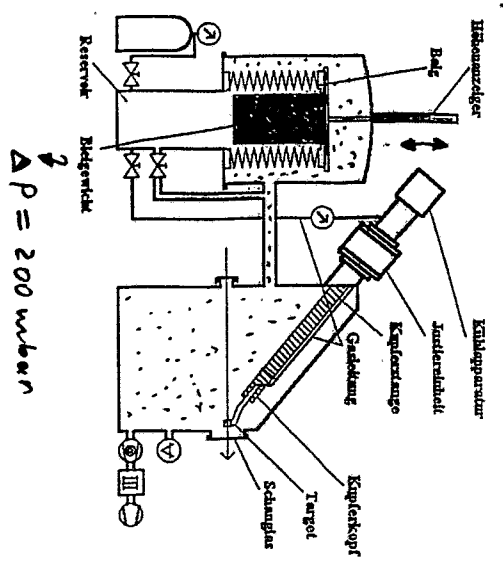
$$t_1 - t_2 \sim X$$

$$t_1 + t_2 \sim t_F$$

$$t_1 = \frac{X}{v_1}$$



LH<sub>2</sub>-Target



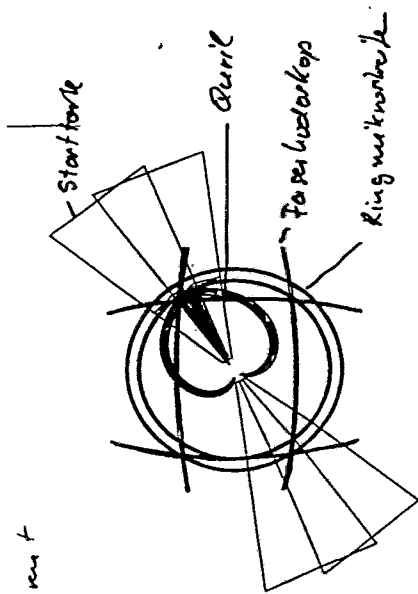
13-16 k

Eichtungs-Kühlschicht: 1 mm Kohlenstoff  
 Target  $\phi$  : 6 mm  
 Targetlänge : 4 mm  
 ? 1.2.10<sup>22</sup> p/cm<sup>2</sup>

Messprotokoll

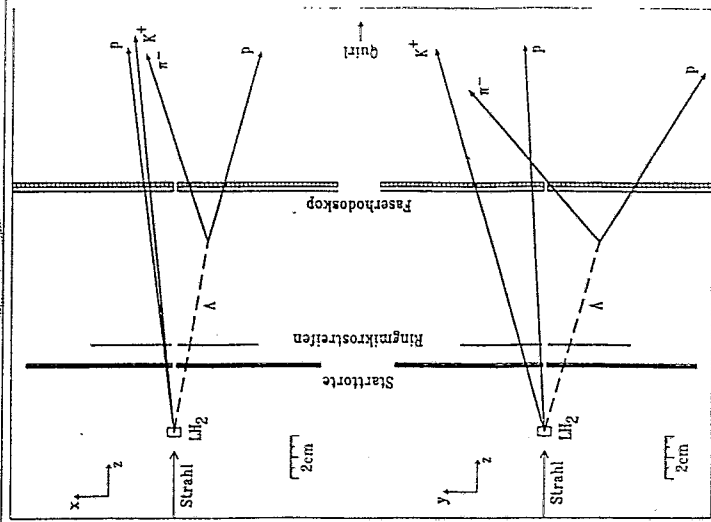
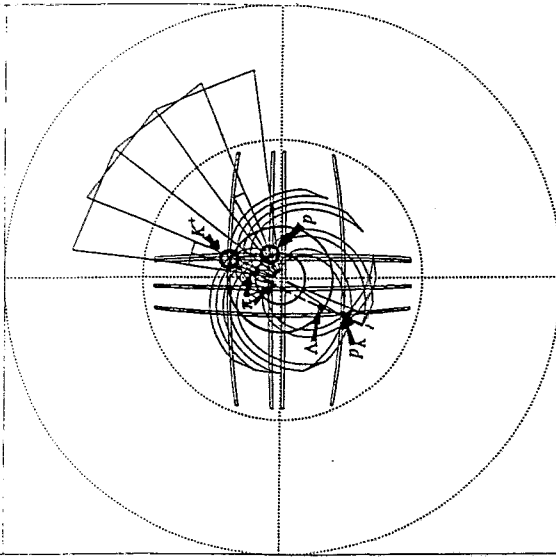
Messdatum: 4/96  
6/96

2-Spurenent



ALMSEPP 2.1  
Sun 1063  
Event 6511

ERL-KOENIG





Ereignisrekonstruktion:

### Vertex z-Position

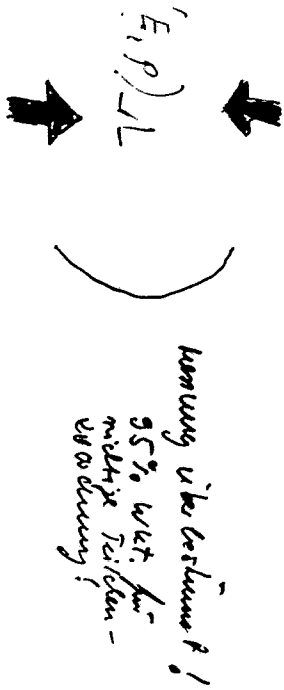
1.  $k^+, p^- \dots$  Ereigniswerte im Target

$k^+, p^-$  - Winkelgleichung  $\Delta t, \Delta E$

Impulserter  $L$  in Ebene  $(\vec{p}_A, \vec{\pi}_A)$

Test für richtige Zuordnung:

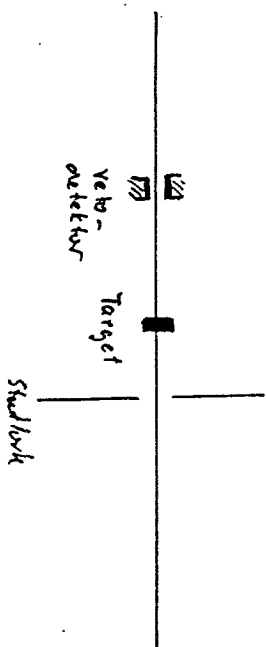
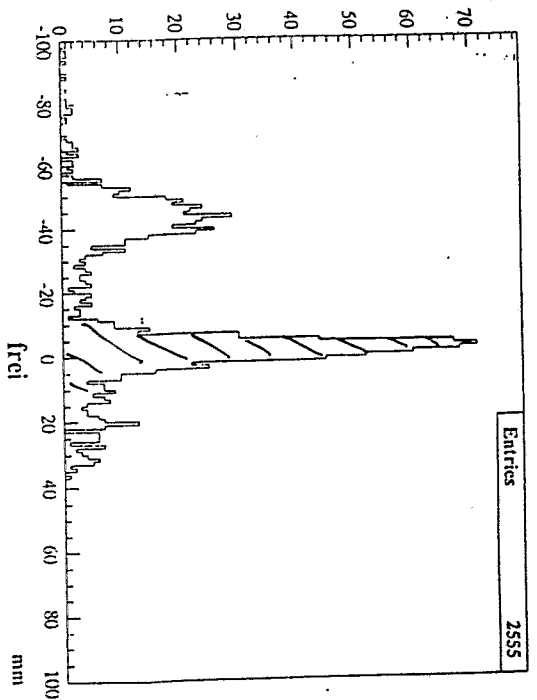
$$\chi^2 = \left( \frac{p_{\text{Stahl}}^2 + m_p^2 + m_p - E_p - E_x \right)^2 - \left( p_{\text{Stahl}} - \vec{p} - \vec{p}_A \right)^2$$



2.  $P_A, \vec{\pi}_A$

da Messung über bestimmt!

Ereignisrekonstruktion möglich für  $k^+$  - Zerfallswerte  
 (17% Rückgewinn!) !

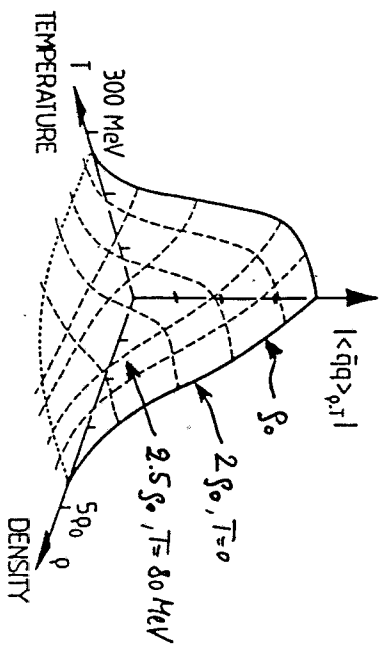


E. Grosse  $K^+$  experiments at SPES3

E. Grosse  $K^\pm$  experiments at KaoS

# Hadrons within the medium

Typical result of an NJL model calculation: (Lutz & Weise, 1992)



The  $\langle \bar{q}q \rangle$  condensate as a function of density  $\rho$  and temperature  $T$ .

Chiral symmetry is restored at large  $\rho$  (and  $T$ )

hadron masses go down:  $m_g^{\text{eff}}(\rho, T) \propto |\langle \bar{q}q \rangle_{\rho, T}|$

production near threshold goes up

$$m_K^{\text{eff}}(\rho) = m_K^2 - \frac{f_{\pi}^2}{f_{\pi}^2} \frac{K \cdot \pi}{\rho} + \dots$$

$$K \cdot \pi \text{ stability}$$

$$K \text{ decay}$$

LEITZ 4734  
Made in Germany

# SPES 3 at Saturne

Boivin, LeBorceu, Taksidoff, Willis et al

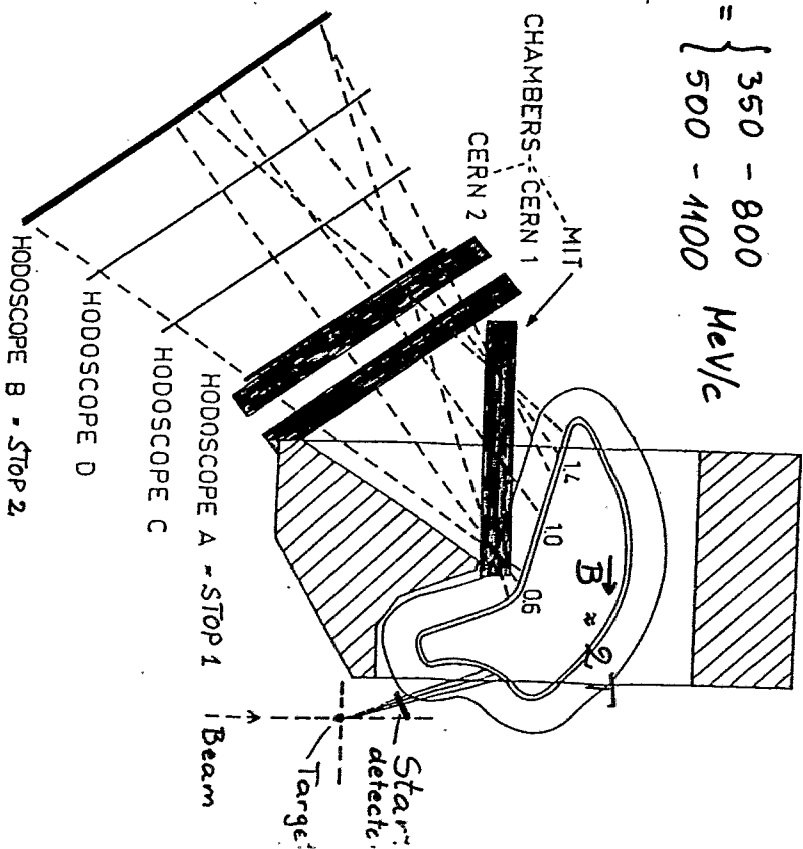
(LNS-IPN-collaboration)

$$\theta_{\text{lab}} = 40^\circ$$

$$\frac{\Delta p}{p} \cong 10^{-4}$$

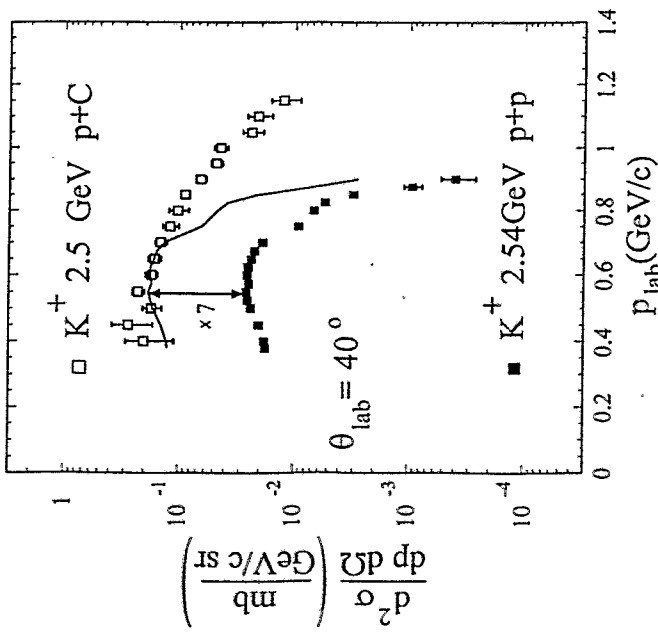
$$\Delta \Omega \cong 10 \text{ msr}$$

$$p = \begin{cases} 350 - 800 \\ 500 - 1100 \end{cases} \text{ MeV/c}$$



Particle identification:  $m = \frac{p}{\beta \gamma}$  (TOF)

Measured:  $p, \pi^+, K^+$

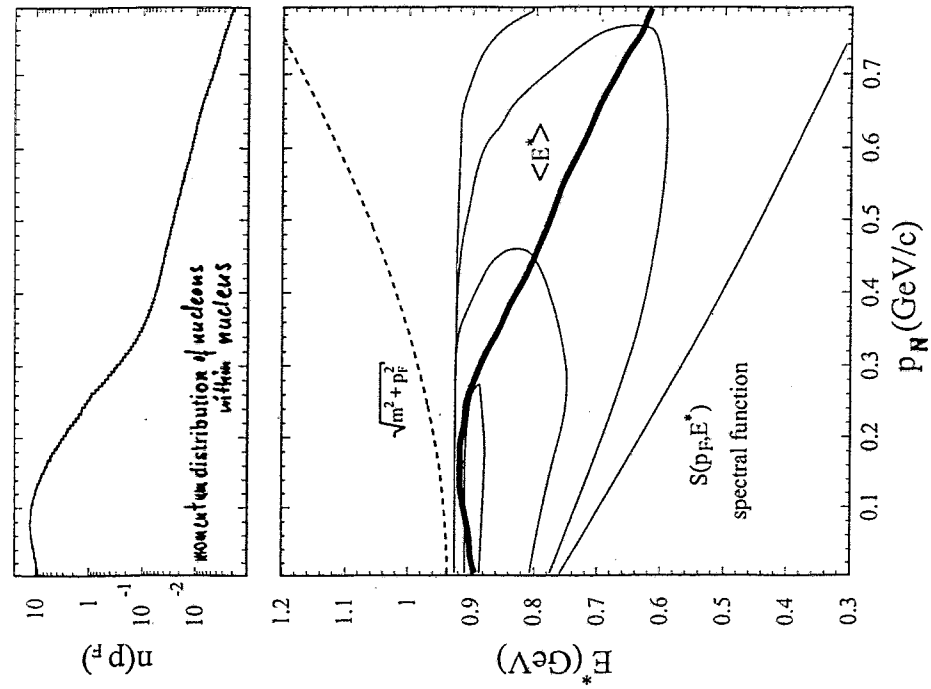


□ Debowski *et al.* (1995)

SPES-3 coll.: GSI + TH Darmstadt, IPN Orsay,  
LNS Saclay, UJ Cracow

■ Hogan *et al.* Phys. Rev. (1968)

$$\frac{\sigma_C^{inel}}{\sigma_p^{inel}} = 7.0$$



based on quasi-free electron scattering data

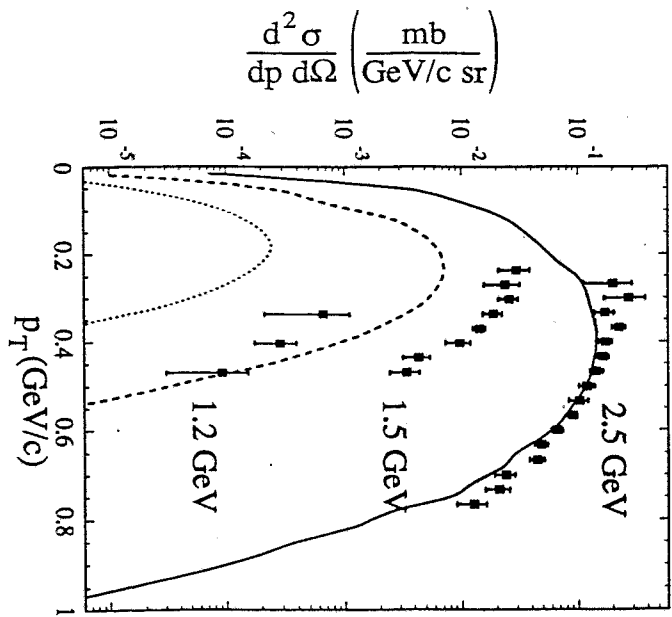
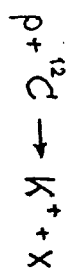
I.Sick, S.Fantoni, A.Fabrocini and O.Benhar (1994)

folding with elementary cross section  $\sigma_{elem}(NN \rightarrow NYK)$

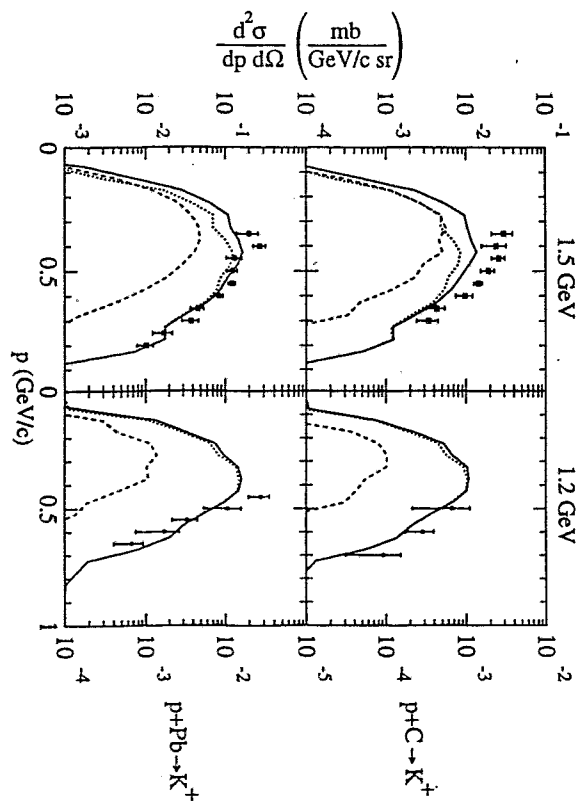
$$\sigma_{pA} = \frac{\sigma_A^{inel}}{\sigma_p^{inel}} \int S(p_N, E^*) \sigma_{elem}(s) d^3 p_N dE^*$$

$$s = (E_p + E)^2 - (\vec{p}_p + \vec{p}_N)^2$$



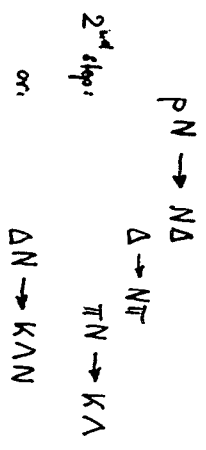


----- folding with spectral function

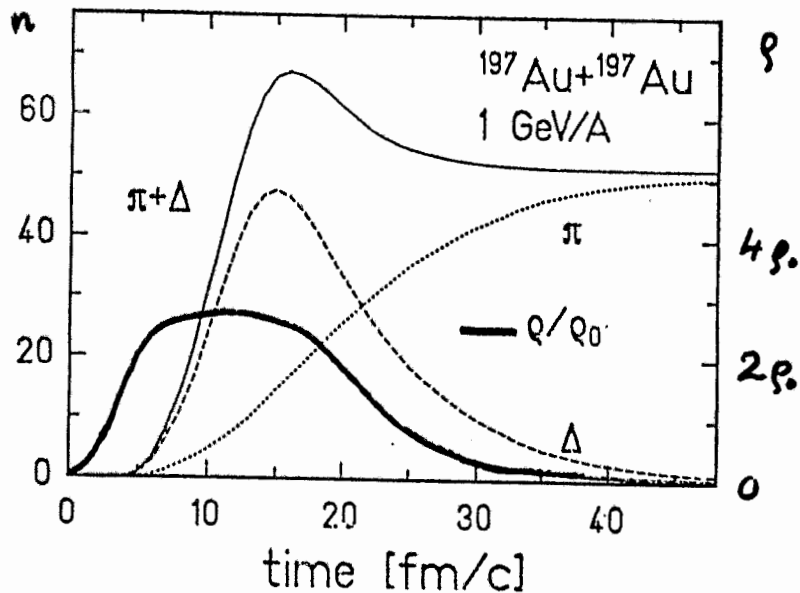
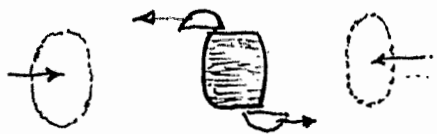


----- folding

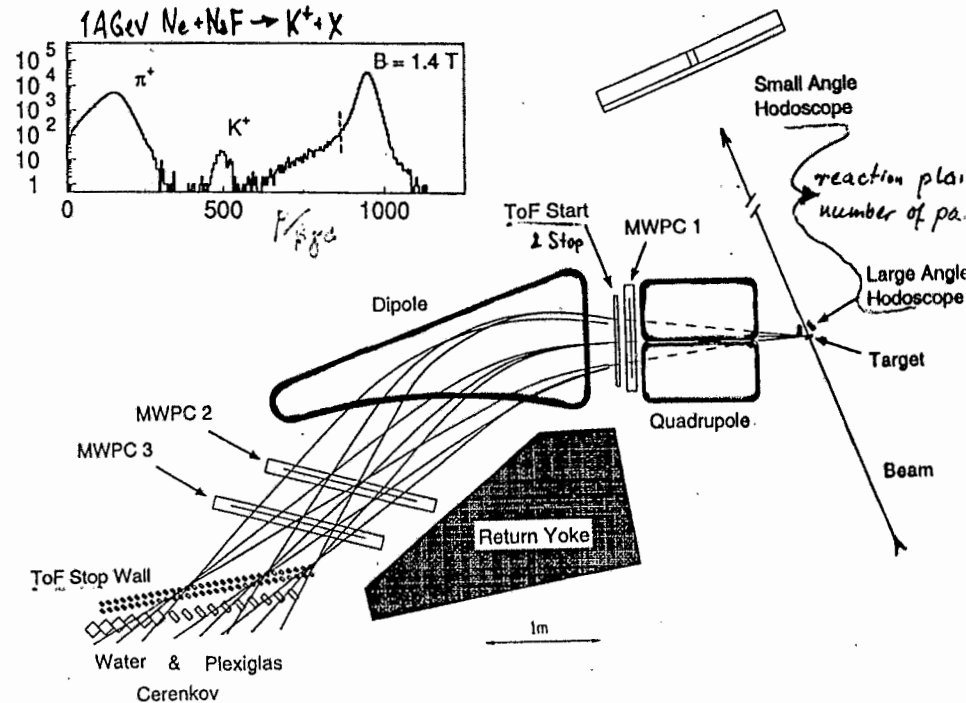
----- plus 2-step processes



2<sup>nd</sup> step:



## The KaoS Spectrometer at SIS



Transport model calculation (BUU) including  $NN \rightarrow NN$ ; Gy. Wolf et al. '93  
(Giessen & GSI)

In central collisions the projectile energy is converted into:

- compression  $\rightarrow$  expansion
- heat  $\rightarrow$  thermal motion  $\rightarrow$
- baryon excitation  $\rightarrow$  meson production

$$\sigma(NN \rightarrow \Delta) \sim 200 \text{ mb} \quad \text{for } \beta \sim 0.1 \text{ to } 0.2$$

$$\sigma_{\text{had}} \sim \sigma_{\text{had}} \sim \sigma_{\text{had}} \sim \sigma_{\text{had}}$$

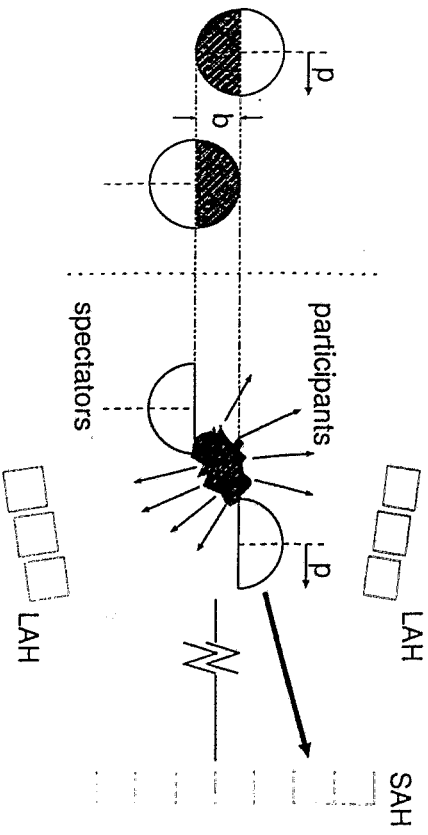
### KaoS Collaboration

R. Barth<sup>a</sup>, D. Brill<sup>c</sup>, M. Cieřlak<sup>a</sup>, M. Dębowski<sup>a</sup>,  
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F. Laue<sup>a</sup>, M. Mang<sup>a</sup>, Ch. Müntz<sup>b</sup>, H. Oeschler<sup>b</sup>,  
F. Pühlhofer<sup>d</sup>, E. Schwab<sup>a</sup>, P. Senger<sup>a</sup>, Y. Shin<sup>c</sup>,  
J. Speer<sup>d</sup>, R. Stock<sup>c</sup>, H. Ströbele<sup>c</sup>, Ch. Sturm<sup>b</sup>,  
K. Völkel<sup>d</sup>, A. Wagner<sup>b</sup>, W. Waluś<sup>c</sup>, M. Waters<sup>a</sup>,  
and I. K. Yoo<sup>d</sup>

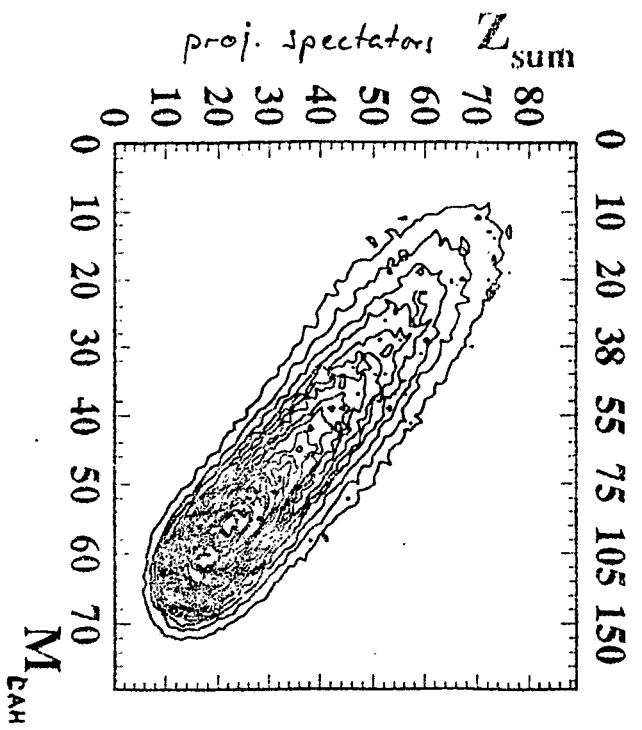
<sup>a</sup> GSI Darmstadt, <sup>b</sup> TH Darmstadt, <sup>c</sup> Univ. Frankfurt,

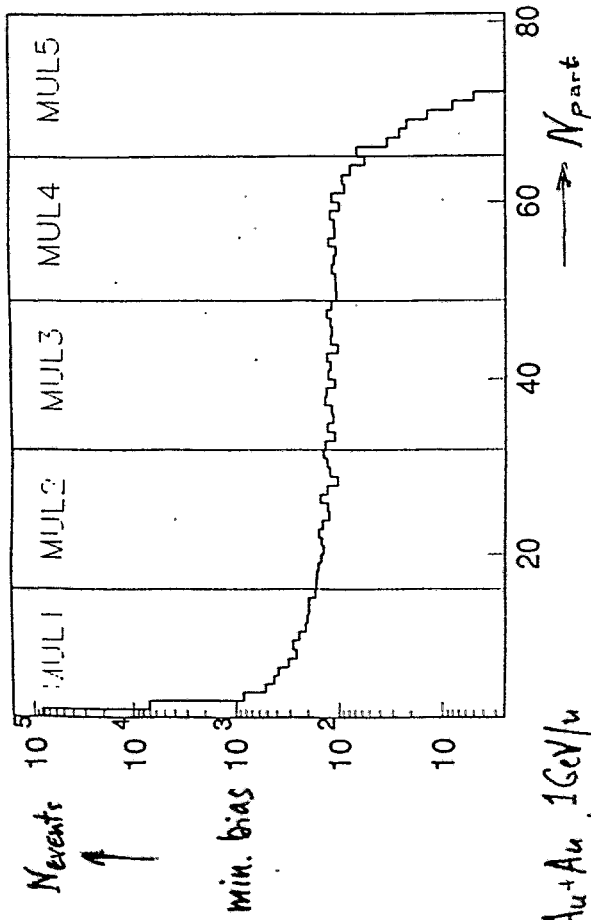
<sup>d</sup> Univ. Marburg, <sup>e</sup> Univ. Kraków

# Event Characterization

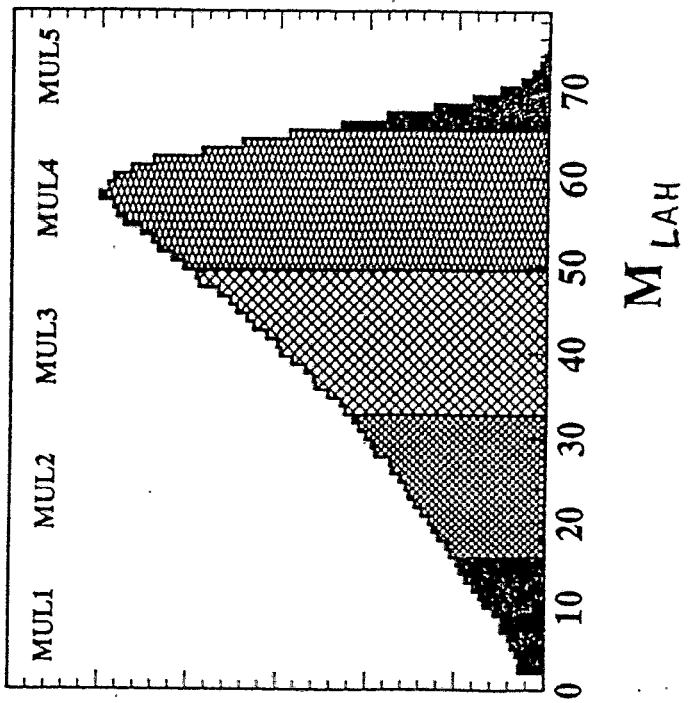


$$A_{PART} = 2 \cdot \frac{A}{Z} \cdot (Z - Z_{SAH}^{SUM})$$



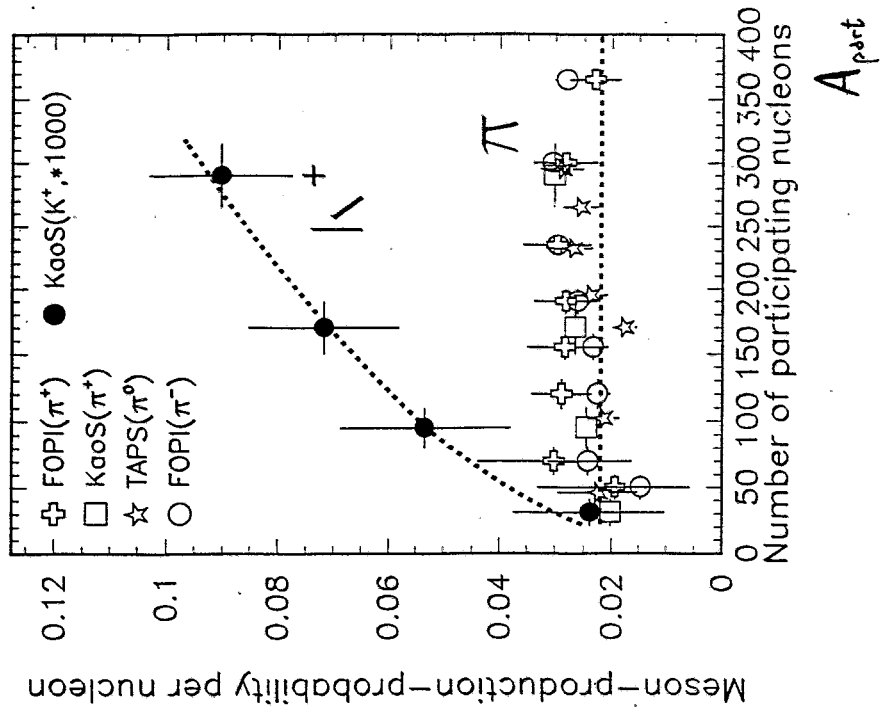


Au+Au, 1 GeV/u



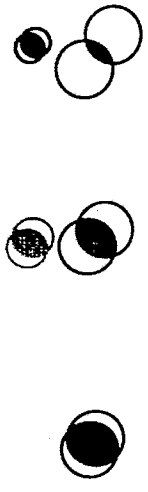
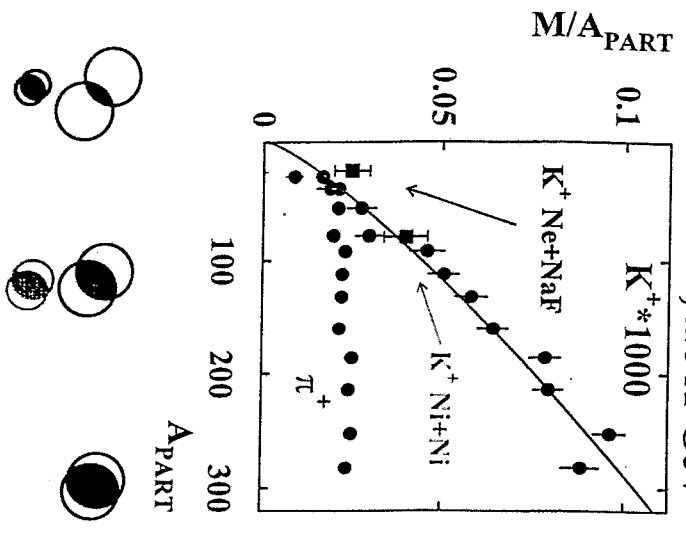
with  $\pi, K, \dots$

Au+Au, 1 A\*GeV





$^{197}\text{Au} + ^{197}\text{Au}, 1.0 \text{ A}\cdot\text{GeV}$



$$M^{K^+} = C \cdot A_{\text{part}}^\alpha \quad ; \quad \boxed{\alpha = 1.75 \pm 0.15}$$

QMD (Hartnack et al., Nucl. Phys. 580 (1994)):

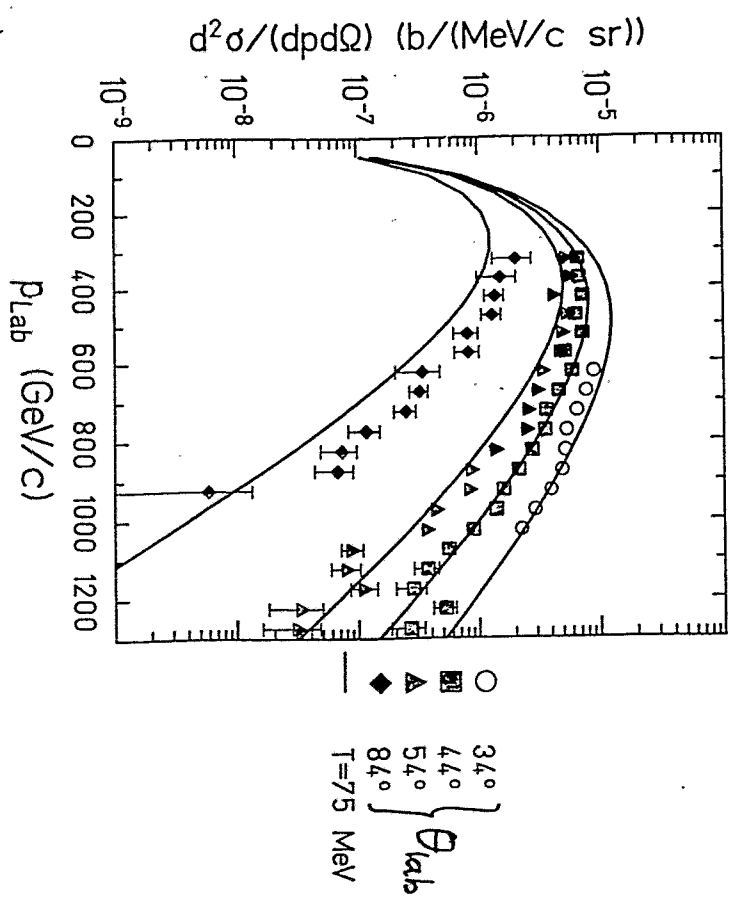
$$M^{K^+} = C \cdot A^\alpha \quad ; \quad \boxed{\alpha = 1.38 \text{ for stiff eos}}$$

$$\boxed{\alpha = 1.62 \text{ for soft eos}}$$

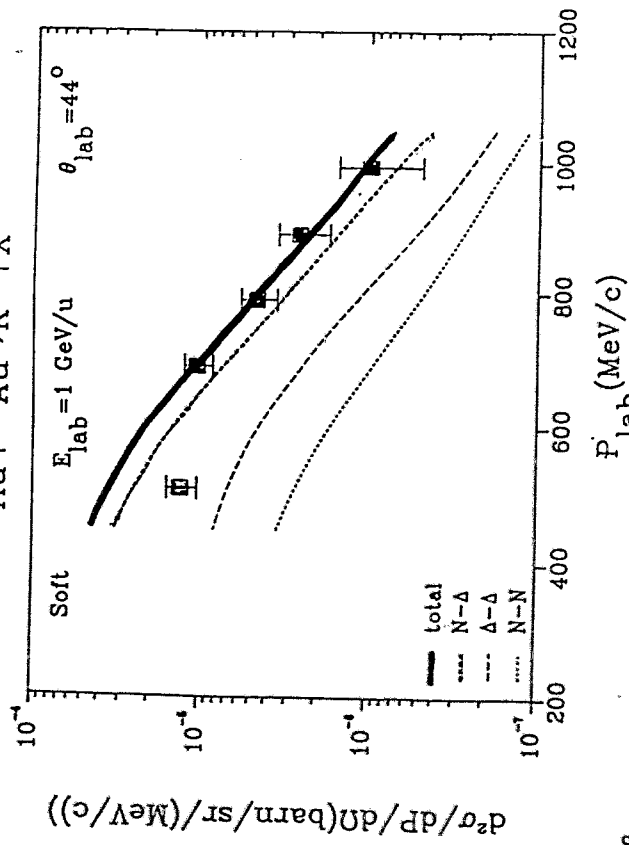
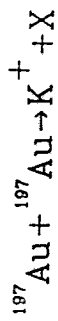
$K^+$  from Au+Au at 1.0 AGeV for different  $\Theta_{lab}$

→ comparison with  $d^3\sigma/dp^3 \propto \exp(-E/T)$

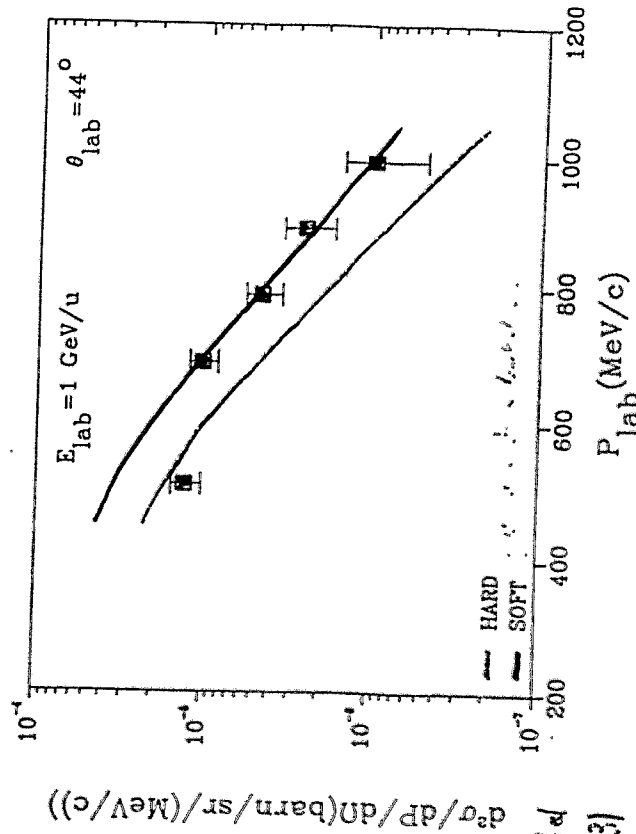
ISENBER, SATANGD, MESON96 1A1110FA, DATA



multi-step-processes



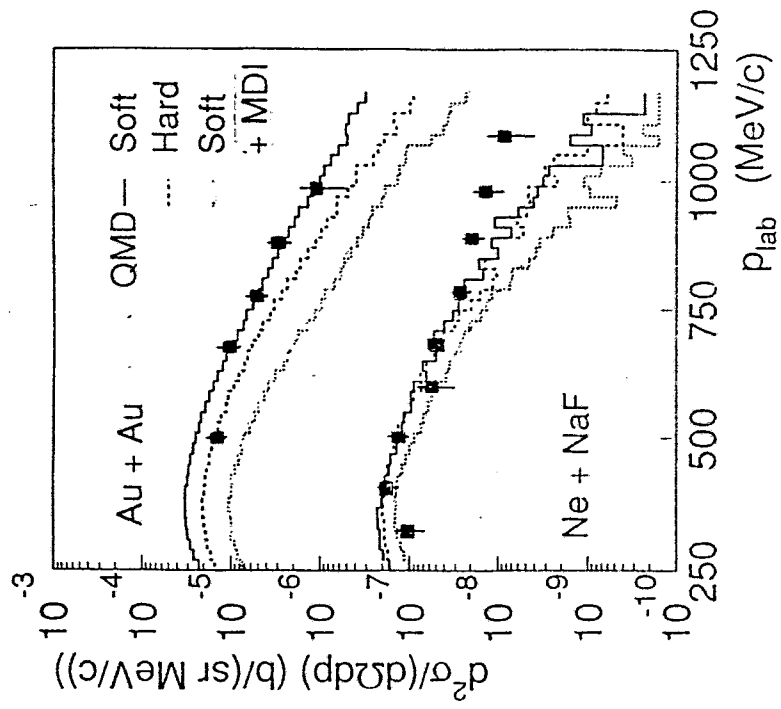
effect of eos



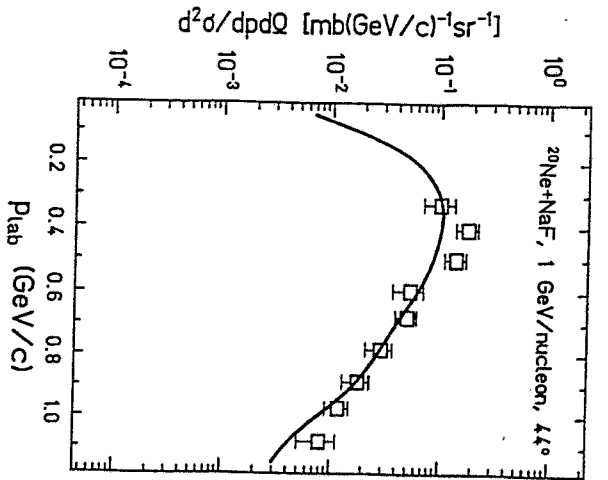
KoS data

QMD:

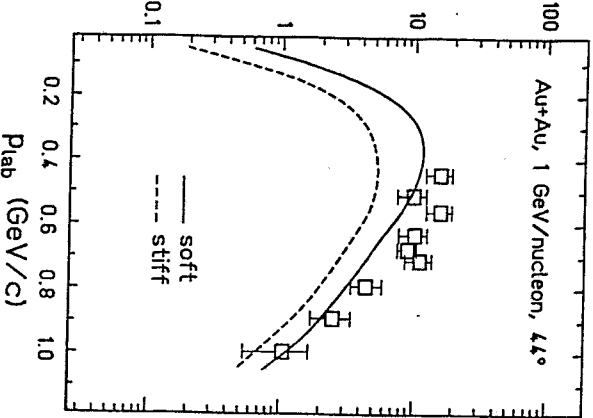
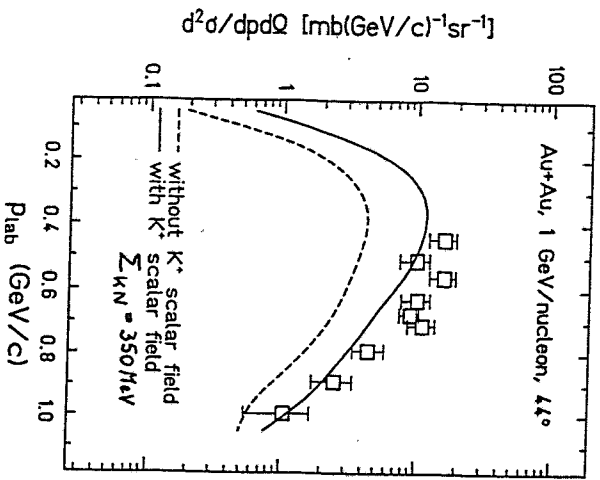
Huang, Foerster et al  
Phys. Lett. (1983)



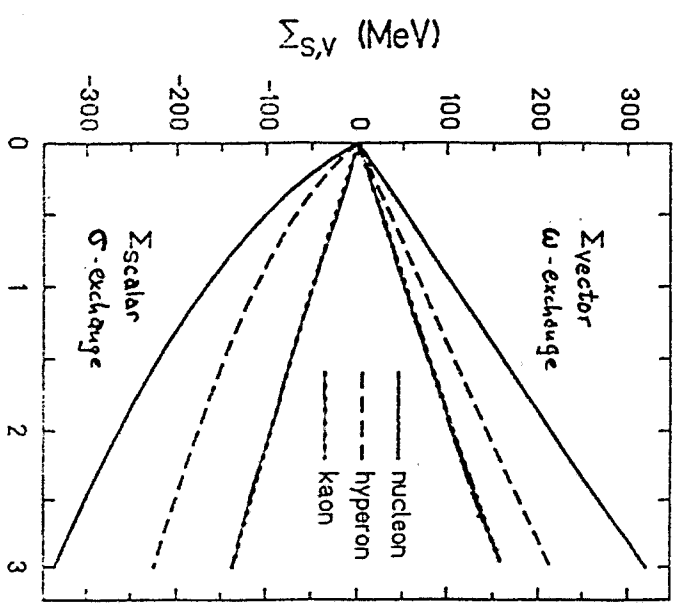
KoS data  
Hartnack & Frickelein  
non-relativistic QMD  
(1993)



midrapidity  
K<sup>+</sup> data  
from KAOS  
D. Hiskowiec et al.



In-medium fields acting on hadrons



σ : attractive  
ω : repulsive  
attractive for antiparticles ?

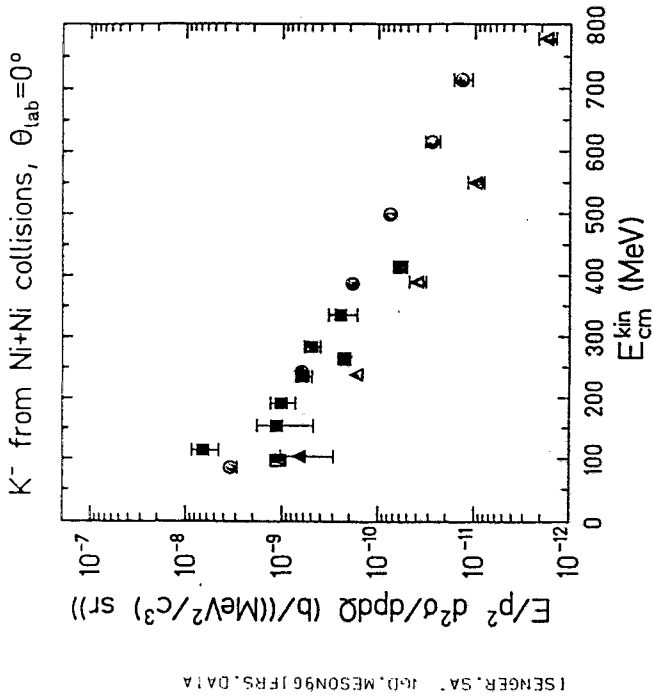
$$V_{opt} = \Sigma_S + \Sigma_V \approx -50 \text{ MeV}$$

G.Q.L. & C.H.Ko

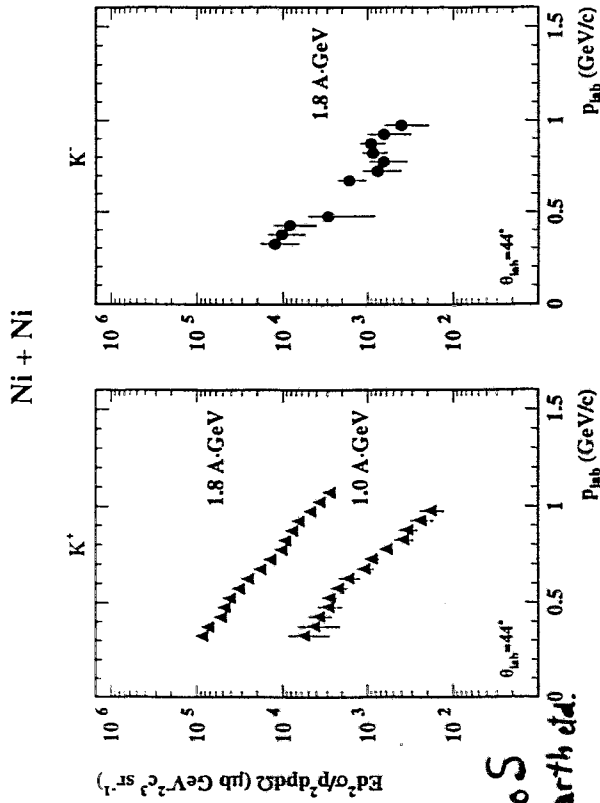
calc. by C.H.Ko, G.Q.L. et al.  
Phys. Lett. B 349 (1995) 405  
Nucl. Phys. A575(1994) 765

11/11/95 (11/11/95)

FRS data at  $0^\circ$  (A. Gillitzer et al.)

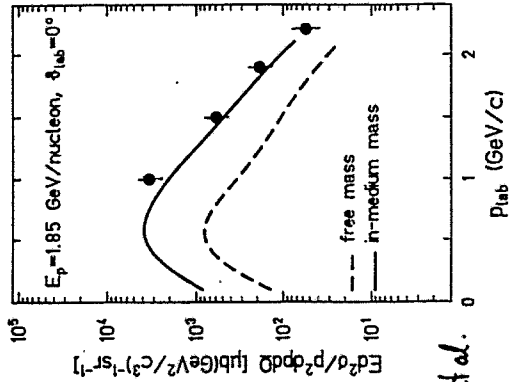


ISENGER, SA. IGD, MESON96 IFRS, DATA



KaoS

R. Barth et al.

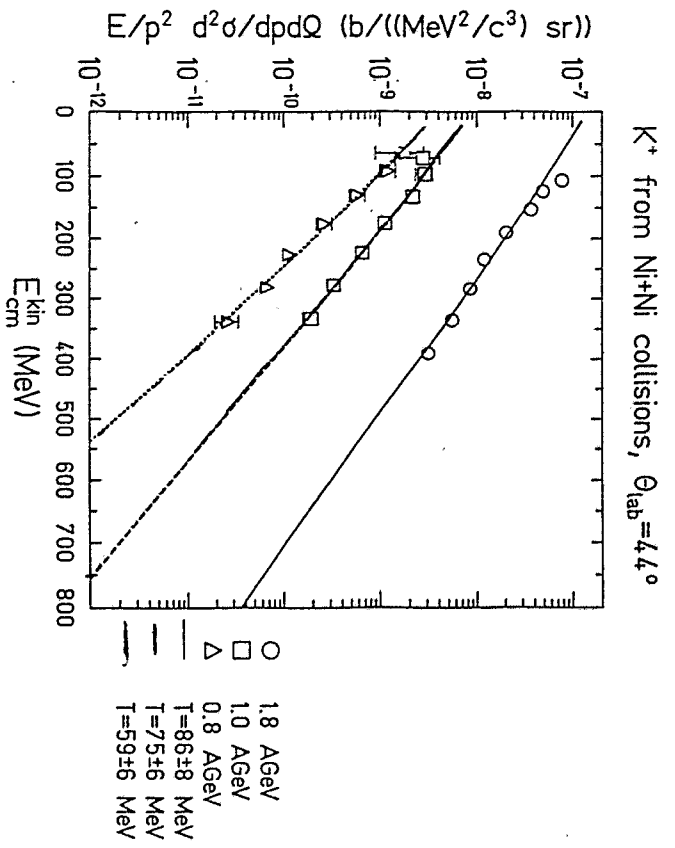


TU München - GSI collab.

A. Gillitzer et al.

data taken at SIS-FRS

calc. by G.O.Li, C.M.Ko et al.



Equivalent energies for  $K^+$  and  $K^-$  production

- $N+N \rightarrow K^+ \Lambda N$  at 1.0 GeV:
- $\sqrt{s} - \sqrt{s}_{thres} = 2.32$  GeV - 2.55 GeV = -0.23 GeV
- $N+N \rightarrow K^+ K^- NN$  at 1.8 GeV:
- $\sqrt{s} - \sqrt{s}_{thres} = 2.63$  GeV - 2.86 GeV = -0.23 GeV

R. Kotte  $K^\pm, \Lambda$  experiments at FOPI

## Study of Hot and Dense Hadronic Matter

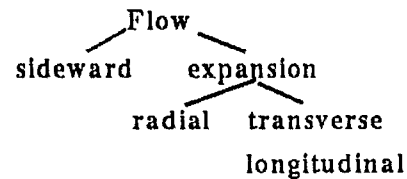
at SIS Energies (0.1-2A GeV)

Outline and Conclusion:

DATA: FOPI, FRS, KaoS, TAPS

Hadronic matter at  $\rho < 3\rho_0$ ,  $T < 100$  MeV

Particle Production  
( $\pi, \eta, K, \Delta, \Lambda, \bar{p}, \Phi$ )



chemical composition

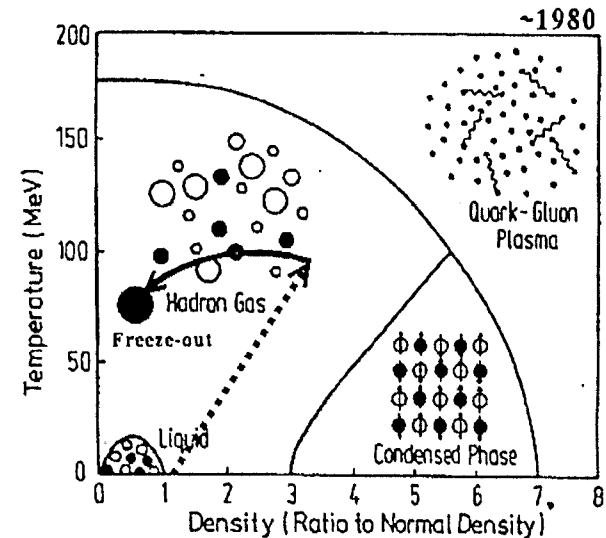
stopping  
dynamics  
kinetic equilibrium

Large Flow Effects

Consistent Picture not achieved yet (strangeness)

Interesting Measurable Speculations  
(chiral symmetry)

## Kernmaterie - Phasendiagramm



Hadronengas:

$p, n, \Delta, N^*, \Lambda, \pi, K, \rho, \omega, \Phi, \dots$

! nicht perturbativer Bereich der QCD

Auswirkungen grundlegender Symmetrien?  
Gleichgewichtskonzepte anwendbar?

Endzustand aller  
(ultra)relativistischen Schwerionenreaktionen

## Experimente zur Strangeness Produktion

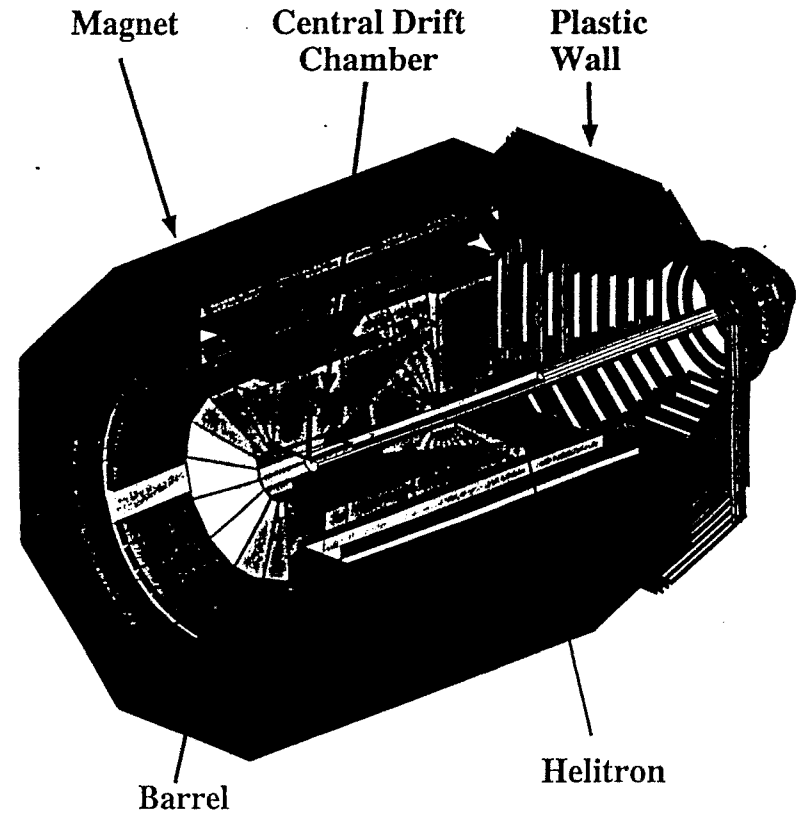
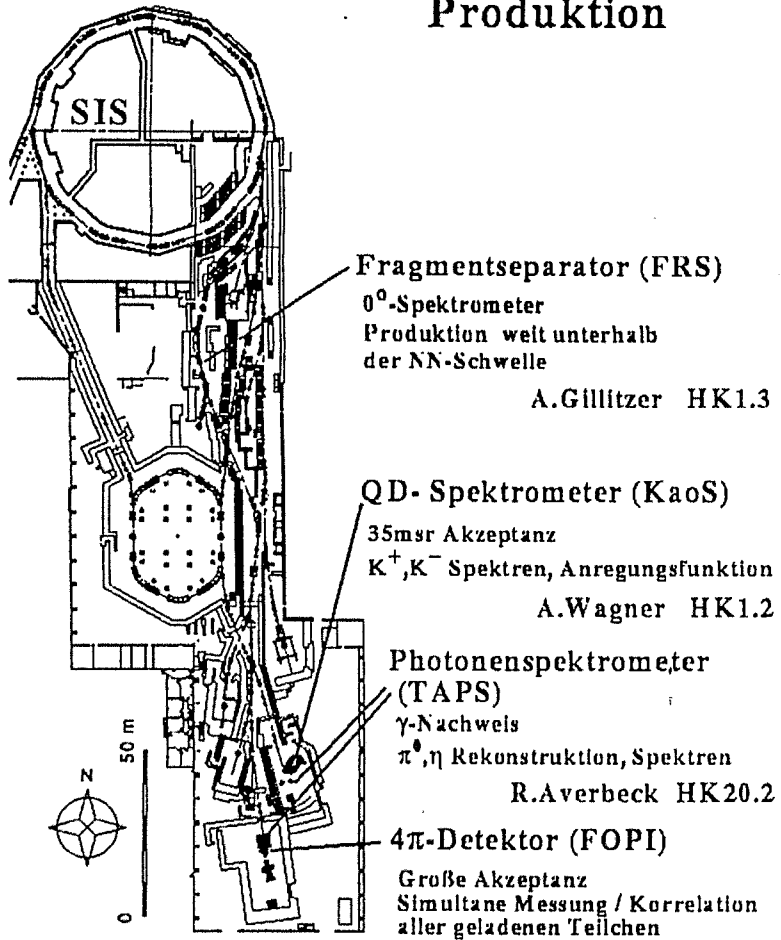
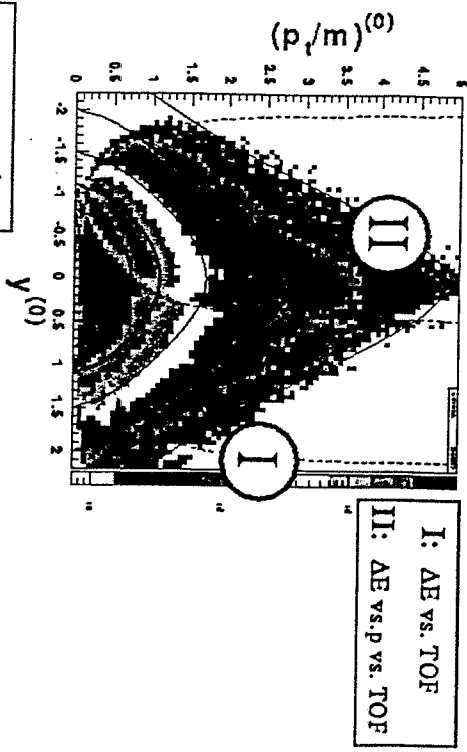


Figure 1: The 4 $\pi$  detector FOPI at GSI. For reference, the 3 arrows at the coordinate system origin are 50 cm long.



# Akzeptanz

## Häufigkeitsverteilung von Z=1 Teilchen im Geschwindigkeitstrahm

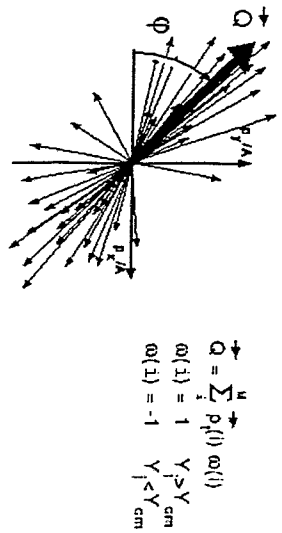


$$y = \tanh^{-1} \beta_{\parallel}$$

$$p_t/m = \gamma \beta_{\perp}$$

$$X^{(0)} := X/X_{\text{projectil}} \text{ im CMS}$$

vollständige azimutale Abdeckung!  
Bestimmung des Stoßparametervektors (Reaktionsebene):



mass determination is restricted only by the finite detector resolution.

After a linearization of the momentum versus velocity data was performed for  $Z = \pm 1$  particles with  $P_{\perp AB} \leq 0.6 \text{ GeV}/c$ , the mass spectra shown in Fig. 1 were produced. For the positively charged particles a large peak is located near  $0.5 \text{ GeV}/c^2$  which is associated to the  $K^+$  meson. At high momenta this peak vanishes below the background which is due to the finite detector resolution, whereas at lower momenta the background is dominated by mismatched Barrel and CDC data. The mass spectrum of negatively charged particles ( $P_{\perp AB} < 0.6 \text{ GeV}/c$ ) reveals, in addition to the  $\pi^-$  contribution, an intriguing structure near  $0.5 \text{ GeV}/c^2$  albeit with low statistics. Not only are the location and width of this structure in agreement with the expected values for anti-kaon production, the yield relative to the  $K^+$  is comparable to previous measurements near this energy [4].

The acceptance for kaons in the transverse momentum versus laboratory rapidity plane is shown in Fig. 2. The data analyzed here are within the horizontally hatched region displayed for the Barrel, but with a further restriction imposed that the maximum laboratory momentum be  $0.5 \text{ GeV}/c$ . For reference, the arrow marks mid-rapidity for a colliding system at  $1.93 \text{ A-GeV}$ . The kaon yield is concentrated mostly in the range of rapidity between the target and mid-rapidity. At  $1.93 \text{ A-GeV}$   $K^+$  mesons can be produced in first chance nucleon-nucleon collisions with a maximum momentum up to the kinematic limit ( $P_{\perp}^{\text{max}} = 0.32 \text{ GeV}/c$ ) which is denoted by the dot-dashed curve. Since al-

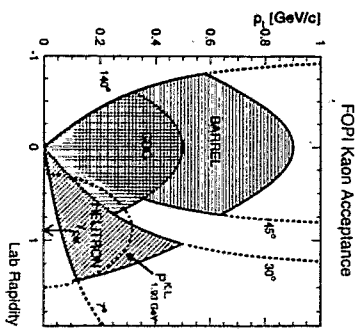
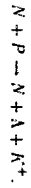


Figure 2. Kaon acceptance of the FOP1 detector system. The data evaluated here are from within the horizontally hatched area marked for the Barrel. For reference, mid-rapidity of systems at  $1.93 \text{ A-GeV}$  is denoted by the arrow.

most the full detector acceptance is beyond this limit, even at beam energies slightly above the free nucleon-nucleon threshold FOP1 is primarily sensitive to kaons produced by collective production processes.

The reaction channel to produce a  $K^+$  with the lowest threshold ( $1.6 \text{ GeV}$ ) includes a hyperon in order to conserve strangeness:



Since the  $A$  is neutral and decays with a lifetime  $\tau_0 \approx 7.9 \text{ cm}$  it can not be directly measured by FOP1. However, the products of its main decay channel ( $A \rightarrow p\pi^+$ , branching ratio 64%) can be readily detected by the CDC. The  $A$  is identified by calculating the invariant mass ( $M_{\text{inv}}$ ) of all  $p\pi^+$  pairs that intersect to form a secondary vertex away from the main event vertex as shown by the open points in Fig. 3. In this figure a very pronounced peak from the  $A$  is visible above the mixed event background which is marked by the dashed histogram.

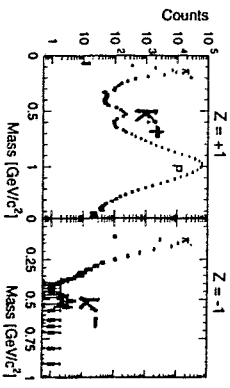


Figure 1. Reconstructed mass using the matched CDC-Barrel data for  $P_{\perp AB} < 0.6 \text{ GeV}/c$  for (left) positively charged particles and (right) negatively charged particles.

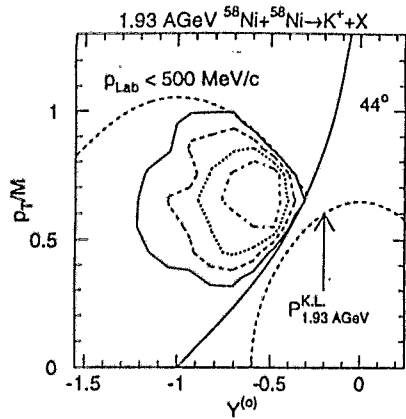


Figure 4. Transverse momentum  $p_T$  versus scaled rapidity  $Y^{(0)}=Y/Y_{CM}-1$  for  $K^+$  particles measured in Ni+Ni collisions at 1.93 AGeV.

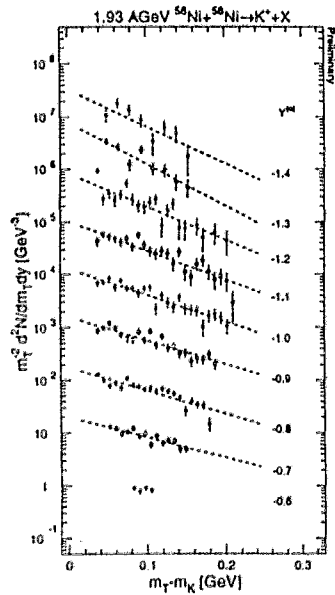


Figure 5. Measured  $K^+$   $m_T$  spectra for various slices in normalized rapidity.

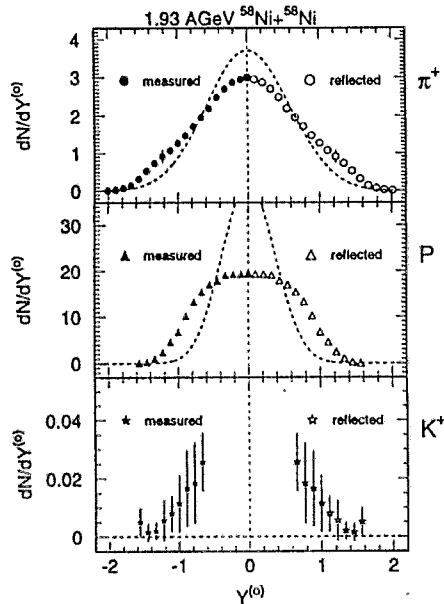
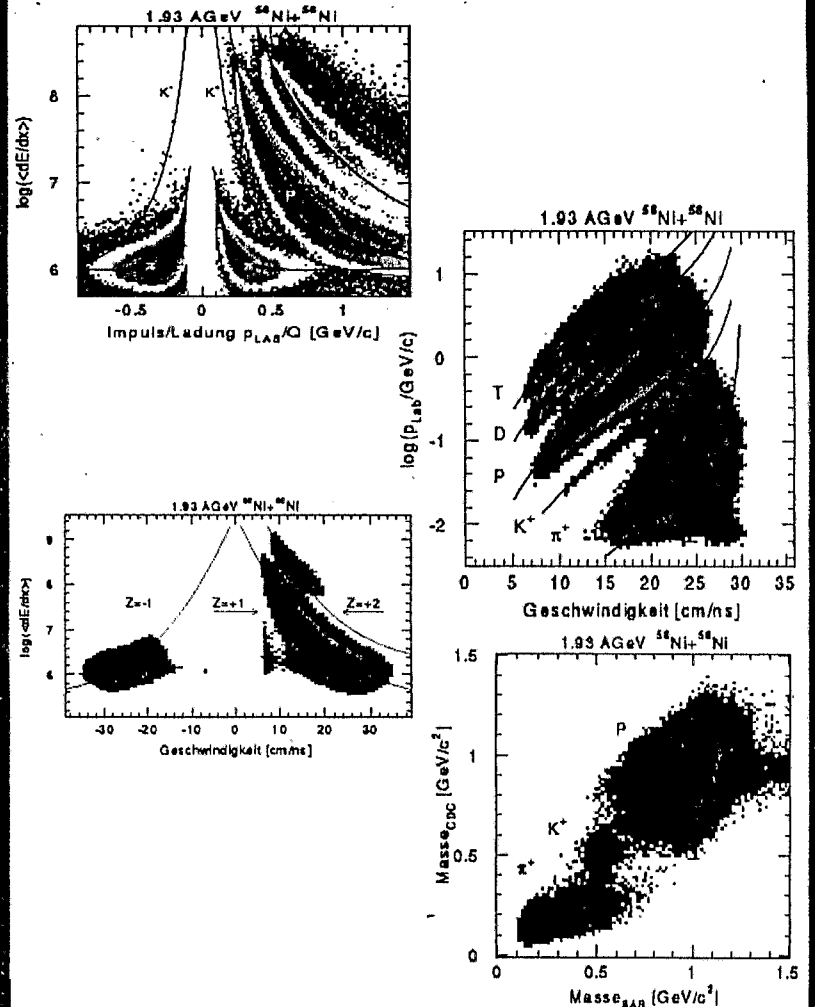


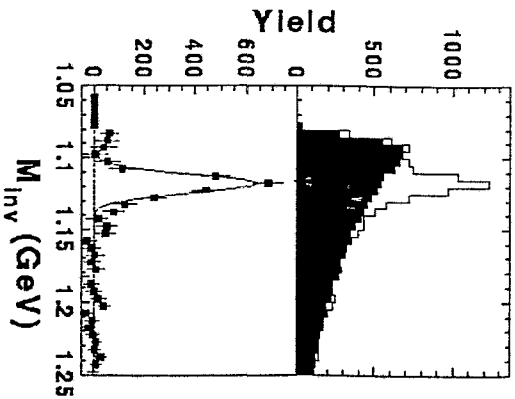
Figure 6. Measured yields of  $K^+$ , proton and  $\pi^+$  as functions of normalized rapidity.

## Teilchen Identifizierung



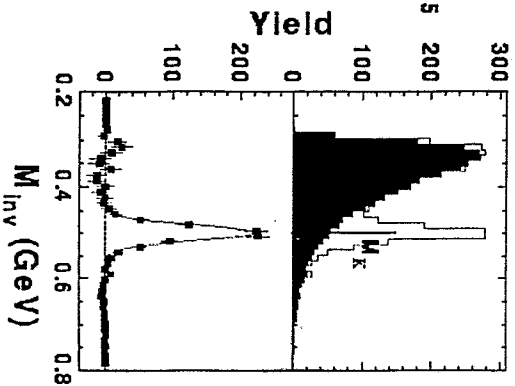
# Rekonstruktion seltsamer Teilchen

$$M_{inv} = \sqrt{(\sqrt{p_1^2 + m_1^2} + \sqrt{p_2^2 + m_2^2})^2 - (\vec{p}_1 + \vec{p}_2)^2}$$



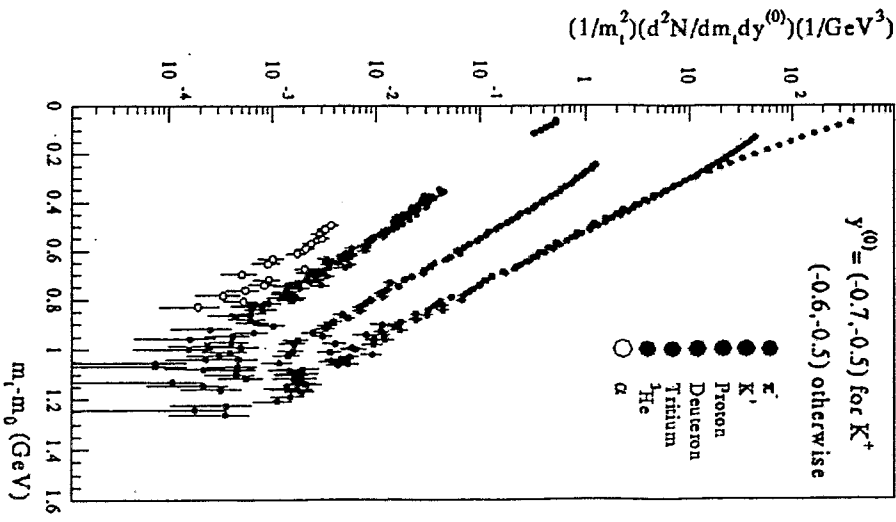
$K_S^0 \rightarrow \pi^+ \pi^-$  (68.6%)  
 $m = 498 \text{ MeV}$   
 $ct = 2.68 \text{ cm}$

$\Lambda \rightarrow \pi^- p$  (64.2%)  
 $m = 1116 \text{ MeV}$   
 $ct = 7.89 \text{ cm}$



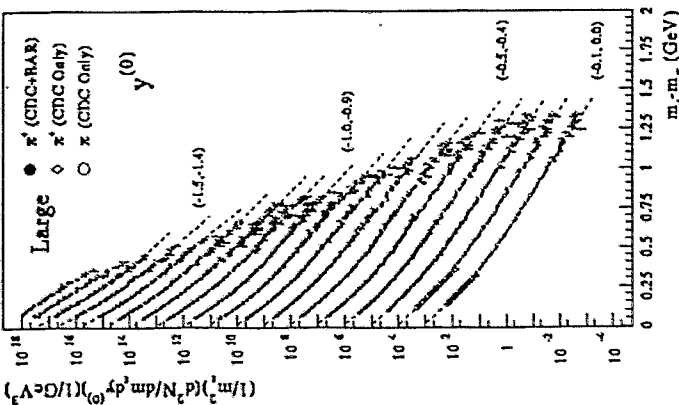
# Transverse Mass Spectra (all)

1.93 AGeV  $^{58}\text{Ni} + \text{Ni}(420 \text{ mb})$ , FOPI Preliminary)



# Spektren ( $\pi, K^+$ )

1.93 AGeV  $^{58}\text{Ni}+^{58}\text{Ni}$ (420mb, FOPI Preliminary)



Transversale Masse

$$m_T = \sqrt{p_T^2 + m^2}$$

Boltzmann Spektrum

$$d^2 N / dp^3 \propto \pi n_T^{-2} d^2 N / d^3 p_T dy$$

# Relativistische Kinematik

$$E = m_T \cosh(y)$$

totale Energie

$$E d^3 \sigma / dp^3 = \frac{1}{2\pi n_T} d^2 \sigma / d^2 m_T dy \text{ invarianter W.-Querschnitt}$$

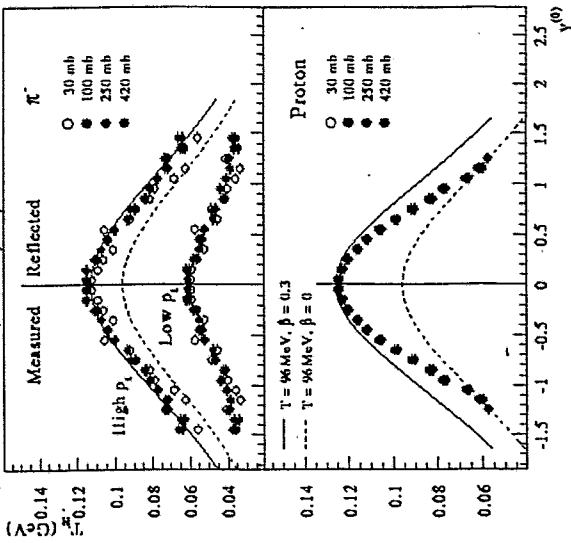
Boltzmann Verteilung

$$d^3 \sigma / dp^3 \propto e^{-E/T} = \frac{1}{2\pi \cosh(y) m_T} e^{-m_T \cosh(y)/T} \propto \frac{1}{m_T^2} e^{-m_T/T_B}$$

$$\rightarrow T_B = \frac{T}{\cosh(y)}$$

Abfallparameter

1.93 AGeV  $^{58}\text{Ni}+^{58}\text{Ni}$  (Centrality Dependence, FOPI Preliminary)

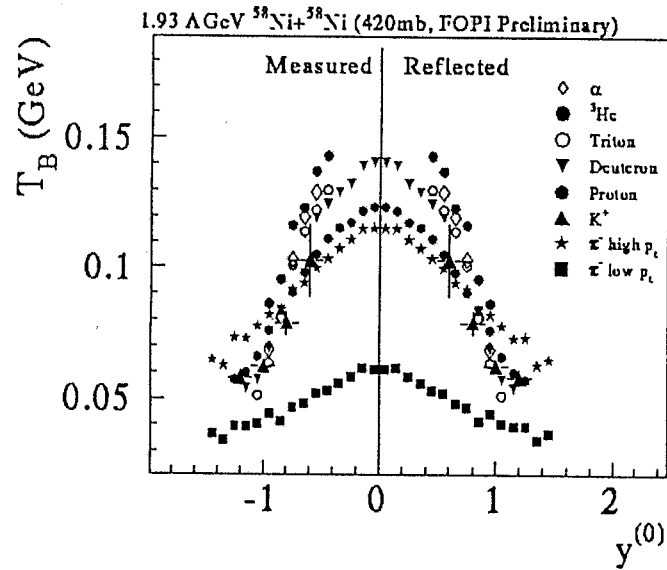


keine  
Zentralitäts-  
abhängigkeit!

Pionen: zwei Komponenten  
 $\pi^+ = \pi^-$

Kaons: einfach exponentiell

## Vergleich der Abfallparameter



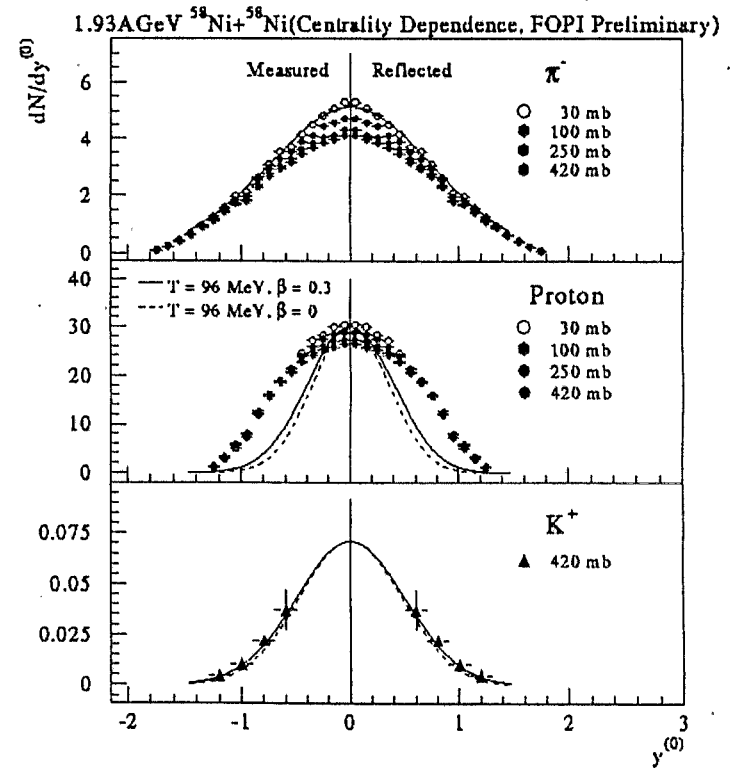
Exponentielle Spektren

Systematische Variation mit der Rapidität

Abfallparameter für Kaonen und Protonen sind ähnlich

Bei  $y^{(0)}=0$ : Ordnung nach der Ejektilmasse

## Rapiditätsdichteverteilungen



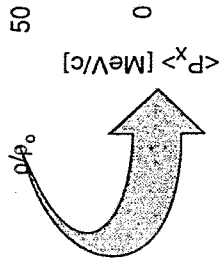
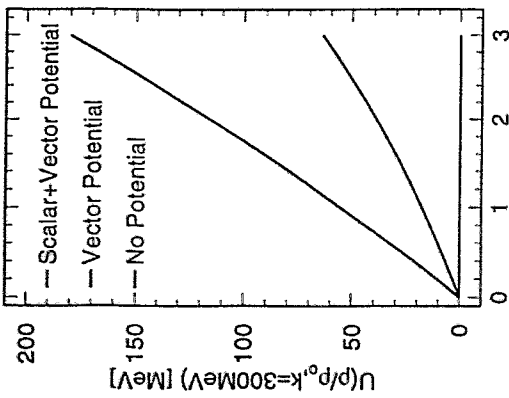
Protonendaten zeigen anisotropes Verhalten (prolat)

Rapiditätsdichteverteilungen der Mesonen sind durch eine isotrope Emissionsverteilung parametrisierbar

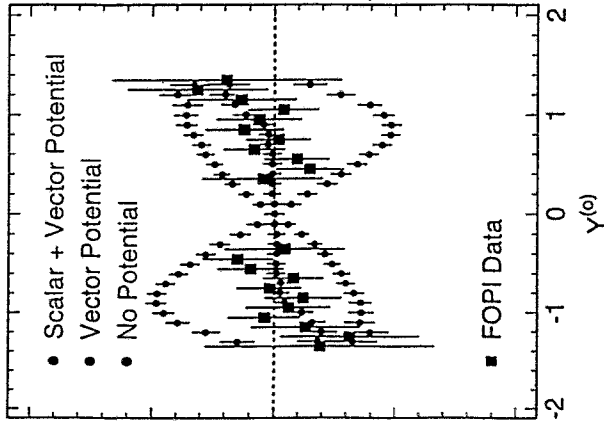
# Gerichteter $K^+$ - Fluß

eine Sonde für das Kaon-Potential  
in Kernmaterie ?

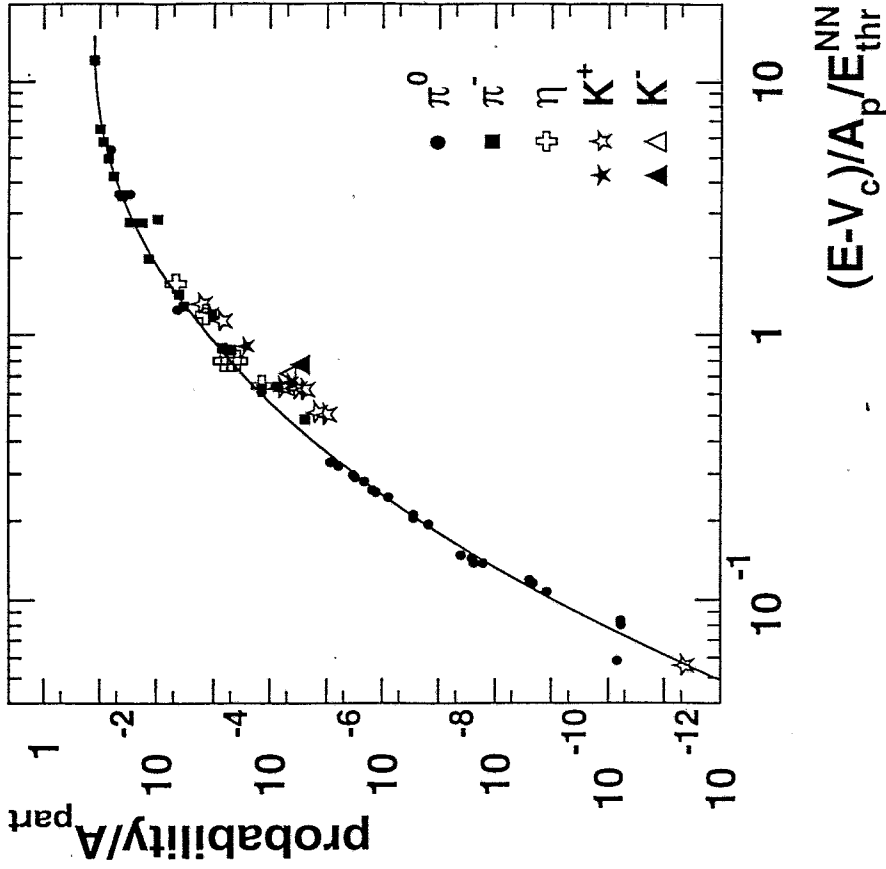
G.QLI, C.M.Ko, B.Li,  
PRL 74 (1995) 235  
NPA 594 (1995) 460



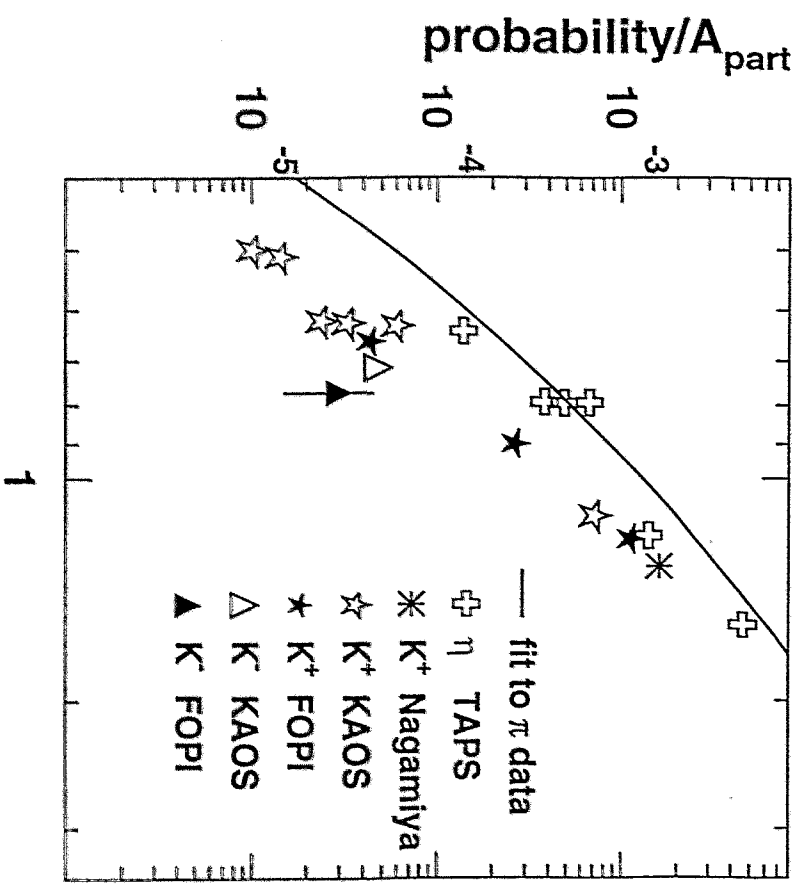
Kaonen bewegen sich  
in einem Potential  
Skalares Potential ist  
zur Beschreibung der  
Daten notwendig



meson-production probability (V.Metag)



strange meson-production probability



$$(E-V)/A_p/E_{thr}^{NN}$$

K. Møller  $K^{\pm}$  experiments at COSY



## COSY-Proposals mit Strangeness-"Content"

COSY-Energiebereich: 40 MeV - 2.5 GeV ( $p = 270 \text{ MeV}/c - 3.3 \text{ GeV}/c$ )

Proposal Nr.	Thema
1	Spectroscopy of Light Hyper-Nuclei with BIG KARL (Ernst, Bonn)
2	$\Lambda$ -Production at Rest by Means of the ${}^4\text{He}(p, {}^4\text{HeK}^+)\Lambda$ Reaction at 1 GeV (Ernst, Bonn)
6	A Precision Study of Near Threshold Two Meson Production via the Reaction $p+d \rightarrow {}^3\text{He}+\pi^++\pi^-$ and $p+d \rightarrow {}^3\text{He}+K^++K^-$ (Jahn, Bonn)
11	Threshold Meson Production at the Internal COSY-Beam in the Range of Scalar Mesons involving Strangeness (Oelert, Jülich)
12	Study of $\eta$ and $\eta'$ Production and Interaction (Roderburg, Jülich)
13	Production of Very Heavy $\Lambda$ -Hypernuclei at Energies Below the Nucleon-Nucleon Threshold (Schult, Jülich)
15	Associated Strangeness Production in pp-Reactions (Eyrich, Erlangen)
18	Study of the Subthreshold $K^+$ Production with a $0^\circ$ -Facility at TP2 in COSY (Sistemich, Jülich)
21	Study of subthreshold $K^-$ -production (Müller, Rossendorf)
32	Measurement of the lifetime of the Hypertriton ${}^3_\Lambda\text{H}$ (Nann, Indiana Univ.)

### COSY-Proposal 6:

**A Precision Study of Near Threshold Two Meson Production Via the Reaktion  $p+d \rightarrow {}^3\text{He}+\pi^++\pi^-$  and  $p+d \rightarrow {}^3\text{He}+K^++K^-$**

**Detektor:** BIG KARL, MOMO

**Physikalische Motivation:** •  $p+d \rightarrow {}^3\text{He}+\pi^++\pi^-$  ( $E_p=432-510 \text{ MeV}$ )

•  $p+d \rightarrow {}^3\text{He}+K^++K^-$  ( $E_p=1.73 - 1.83 \text{ GeV}$ )

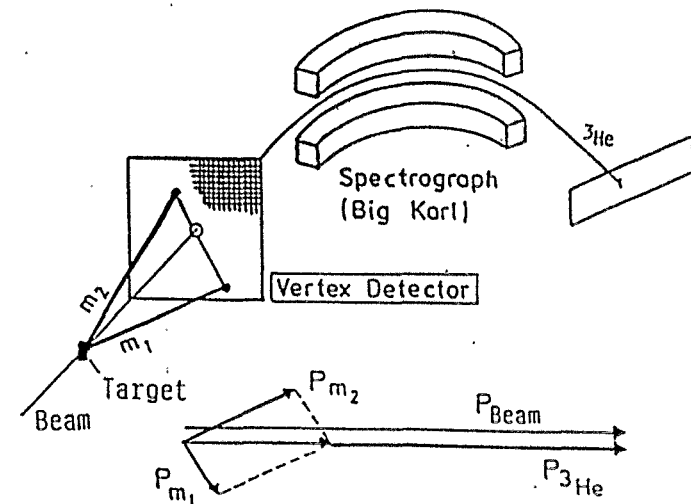
• precision data on low energy ( $T < 50 \text{ MeV}$ ) meson-meson interaction (Phase behaviour, resonances in meson-meson-scattering)

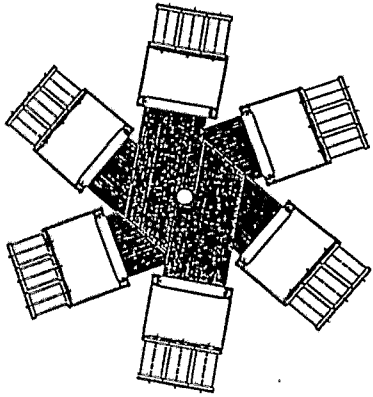
• ABC-effect,  $K\bar{K}$  molecules?

• radiative  $\Phi(1020)$  decay?  
→ strange quark content of  $f_0(975)$

• glueball in the 1 GeV missing mass region?  
(determination of the  $K^*K/\pi^+\pi^-$  ratio)

### Experimentaufbau:





**COSY-Proposal 12:**

**Study of  $\eta$  and  $\eta'$  Production and Interaction**

**Detektor: TOF**

- Physikalische Motivation:**
- measurement of cross section of  $pp \rightarrow pp\eta$
  - measurement of cross section of  $pp \rightarrow pp\eta'$
  - $pd \rightarrow ppK\Lambda, 3pKK, {}^3\text{He}\eta, {}^3\text{He}\eta'$   
 → constraints on the quark and gluonic content of  $\eta$  and  $\eta'$

$$\eta = \eta_8 \cdot \cos \theta_p - \eta_1 \cdot \sin \theta_p$$

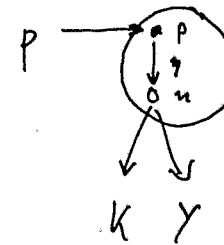
$$\eta' = \eta_8 \cdot \sin \theta_p + \eta_1 \cdot \cos \theta_p$$

$$\eta + \eta' = 2 \cdot K^*$$

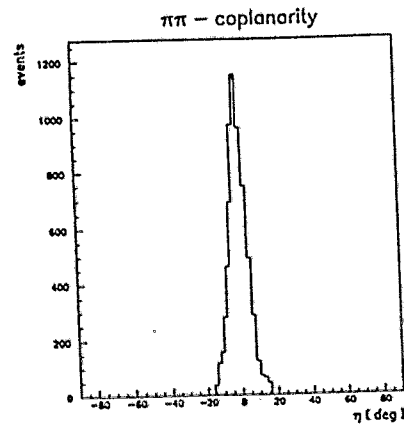
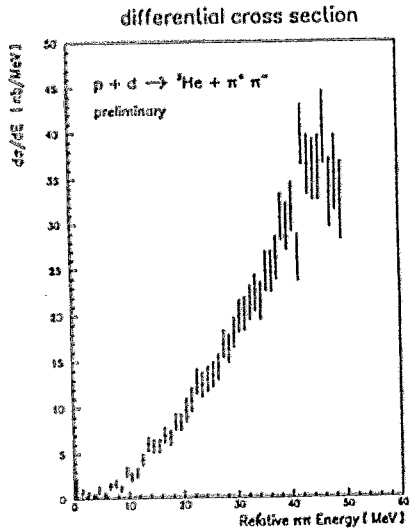
$$(1506 \leftrightarrow 895) \text{ (MeV/c}^2\text{)}$$

$$\phi + \omega = 2 \cdot K$$

$$(1801 \leftrightarrow 1784) \text{ (MeV/c}^2\text{)}$$



- 1.)  $pp \rightarrow pp\gamma$  ( $\frac{1}{4}$ )
- 2.)  $\gamma(\prime) + n \rightarrow k\gamma$   
 $\quad\quad\quad \quad\quad\quad \bar{k}N$



**Fig. 4:** Relative energy spectrum of two - pion events from the reaction  $pd \rightarrow {}^3\text{He} \pi^+ \pi^-$  at 1150 MeV/c incident proton beam momentum

**Fig. 3:** Coplanarity of the  $\pi^+\pi^-$  -events

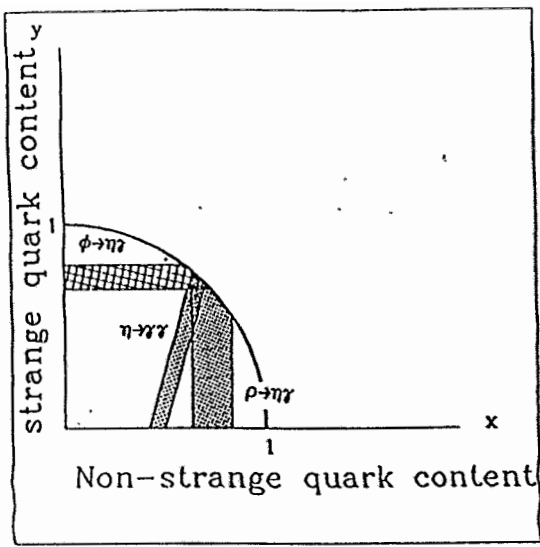


Fig. 1  $\eta$  quark content [4].  $x$  and  $y$  are defined in the formula:  
 $|\eta\rangle = x \cdot 1/\sqrt{2} |uu+dd\rangle + y \cdot |ss\rangle$

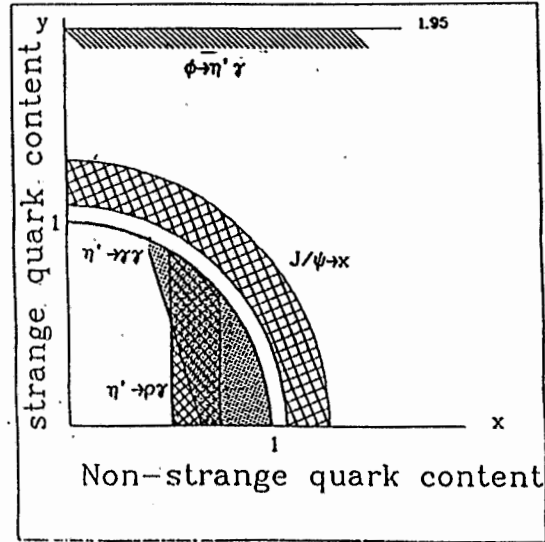


Fig. 2  $\eta'$  quark content [4]. (Updated for  $\phi \rightarrow \eta' \gamma$  [5] and for  $J/\psi \rightarrow$  vector + pseudoscalar meson [6])

Reaction	$pp \rightarrow pp\eta$	$pp \rightarrow pp\eta'$	$pd \rightarrow 3pKK$	$pd \rightarrow ppK\Lambda$	$pd \rightarrow 3He \eta$	$pd \rightarrow 3He \eta'$
Threshold (GeV/c)	1.886	3.208	2.521	1.850	1.573	2.434
Momentum of scattered protons ( $3He$ ) (GeV/c) at threshold	0.77	1.06	0.62	0.50	1.32	1.18
at threshold +50 MeV/c	.61-.98	.94-1.23	.42-.86	.31-.72	1.19-1.52	1.63-2.18
at threshold +100 MeV/c	.55-1.08	.81-1.40	.35-.97	.24-.83	1.15-1.62	1.56-2.18
Maximum lab.-angle of scattered protons ( $3He$ ) at threshold + 50 MeV/c	10.5	7.6	16.7	21.0	6.3	5.7
at threshold + 100 MeV/c	14.7	10.2	23.7	30.0	8.9	8.0

Mögliche Prozesse zur Strangeness-Untersuchung an COSY-TOF

Reaktion	Schwelleenergie $\sqrt{s}$ in GeV	Impuls GeV/c	kinetische Energie GeV
$pp \rightarrow K^+ \Lambda p$	2.548	2.339	1.582
$K^+ \Sigma^+ n$	2.622	2.560	1.789
$K^+ \Sigma^+ p$	2.624	2.566	1.793
$K^+ \Sigma^+ p$	2.625	2.569	1.796
$p d \rightarrow K^+ \Lambda d$	3.485	1.839	1.127
$p^4He \rightarrow K^+ \Lambda^4He$	5.338	1.581	0.900
$p^{12}C \rightarrow K^+ \Lambda^{12}C$	12.787	1.400	0.747
$pp \rightarrow K_s^+ K_s^0 pp$	2.875	3.327	2.518

Tabelle 2.1: Schwellenimpulse für die protoninduzierten Reaktionskanäle der assoziierten Strangeness-Produktion am Proton und an leichten Kernen im Impulsbereich von COSY

- $pp \rightarrow \Sigma^+ K_s^0 p$
- $pp \rightarrow K^+ K^- pp$
- $pp \rightarrow K_s^+ K_s^0 pp$

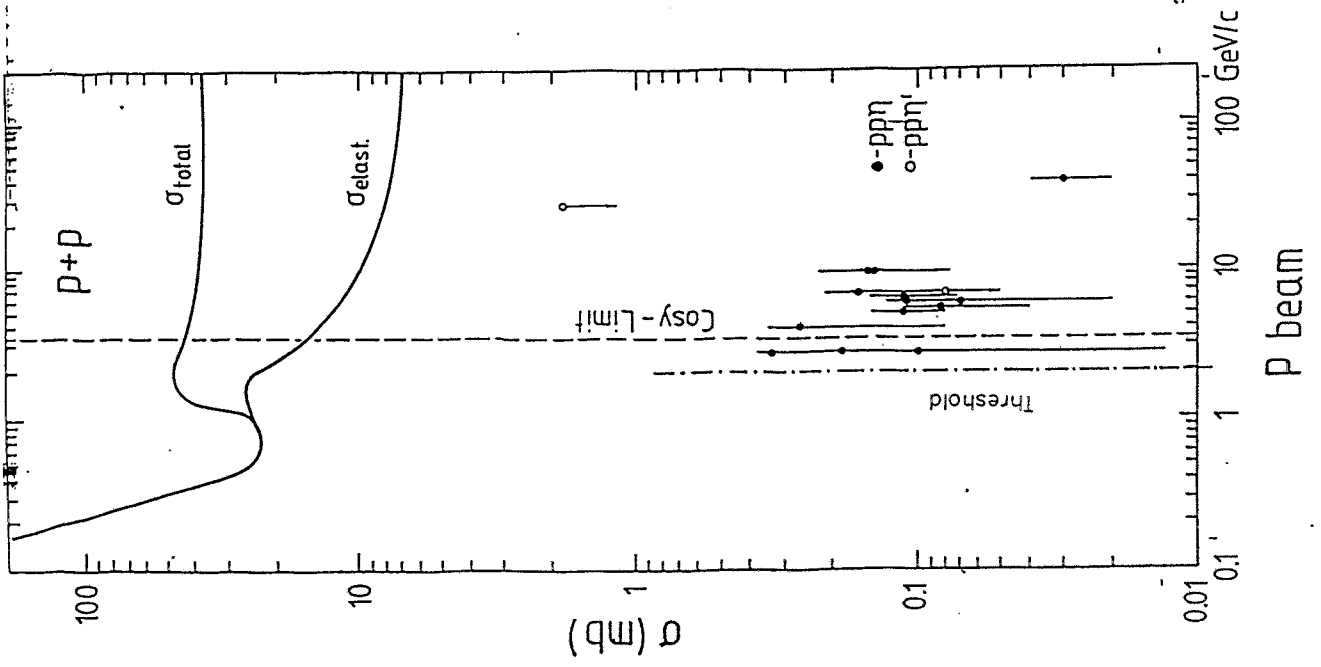
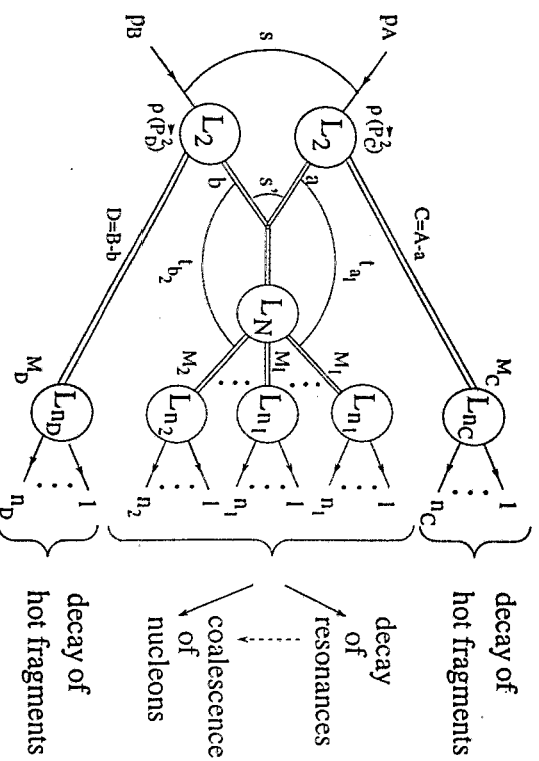


Fig. 6 Cross-section  $pp \rightarrow ppn$  in comparison to the total cross-section :

H. Müller     $K^\pm$  in heavy-ion collisions

# Decomposition of phase-space Nucleus-Nucleus



# Nucleus-Nucleus

- Differential cross section

$$d\sigma_{AB}(s; \vec{\alpha}) = \sum_a \sum_{z_a} \sum_b \sum_{z_b} \sigma_{a z_a b z_b} \frac{dW_{a z_a b z_b}(s; \vec{\alpha}_N)}{\int dW_{a z_a b z_b}(s; \vec{\alpha}_N)}$$

$\sigma_{a z_a b z_b}$ : Glauber

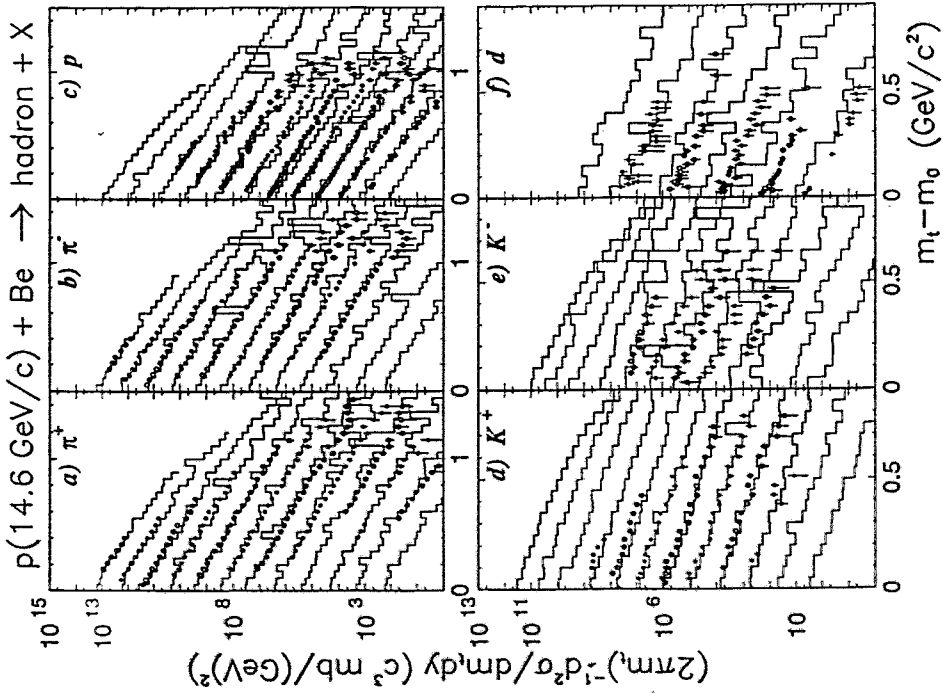
- Probability of populating channel  $\vec{\alpha}_N = (\alpha_1, \dots, \alpha_N, \alpha_C, \alpha_D)$

$$dW(s; \vec{\alpha}_N) \propto dZ_C(\alpha_C) dZ_D(\alpha_D) \left\{ \prod_{i=1}^N dZ_I(\alpha_I) \right\} dZ_N(s')$$

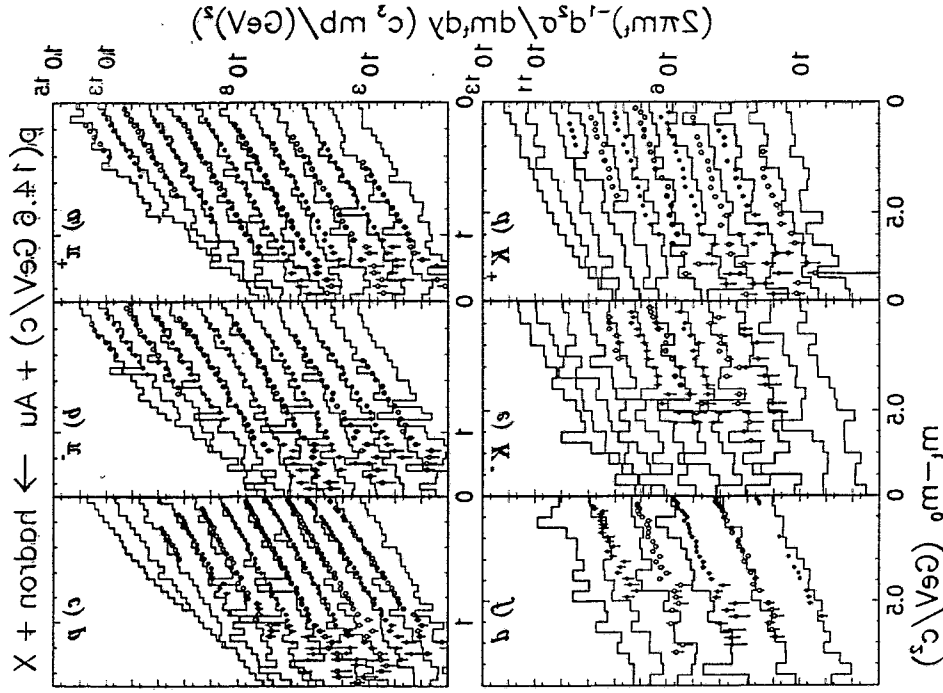
- Number of final states in  $\alpha_J$  ( $J = C, D$ )

$$dZ_J(\alpha_J) = dN_J^2 \frac{d^3 P_J}{E_J} \rho(\vec{P}_J^2) \left( \frac{V_J}{(2\pi)^3} \right)^{n_J-1} \left\{ \prod_{i=1}^{n_J} (2\sigma_i + 1) 2m_i dm_i F_i(m_i) \right\} \left( \frac{M_J}{\Theta_J} \right) K_1 \left( \frac{M_J}{\Theta_J} \right) dL_{n_J}(M_J; \alpha_J)$$

$\rho$ : Internal momentum distribution

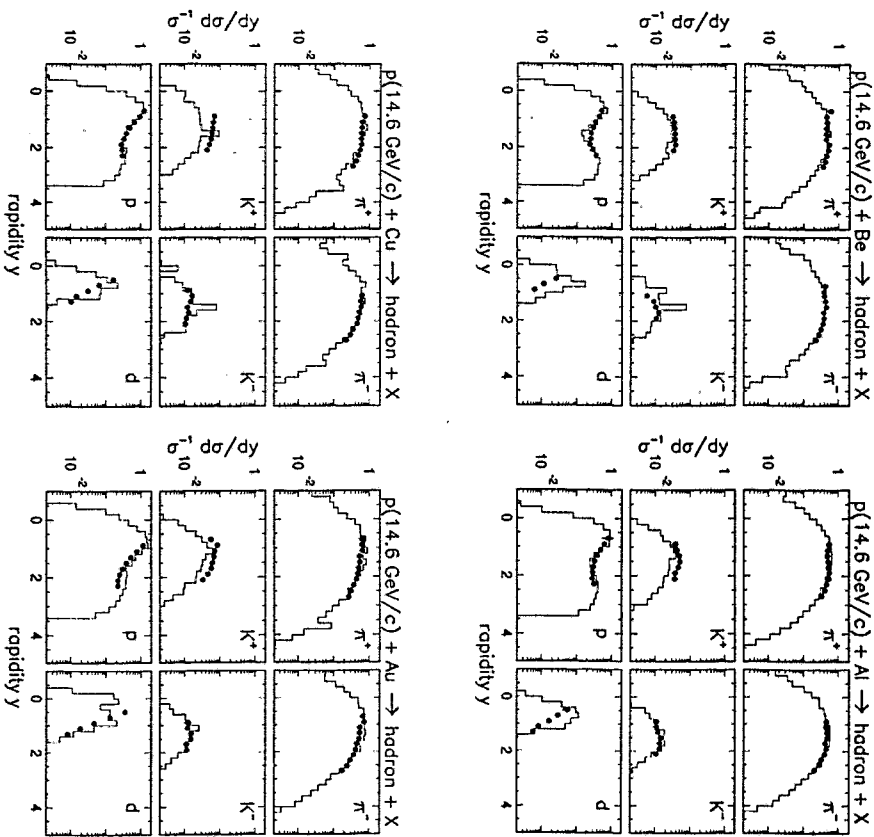


Invariant cross sections in the rapidity interval  $0.4 < y < 2.8$  as a function of  $m_t - m_0$  with  $m_t^2 = m_0^2 + p_t^2$ . Spectra are multiplied by powers of 10. Data (points) from E802 collaboration [T. Abbott et al., Phys. Rev. D 45 (1992) 3096] are compared with ROC calculations (histograms)

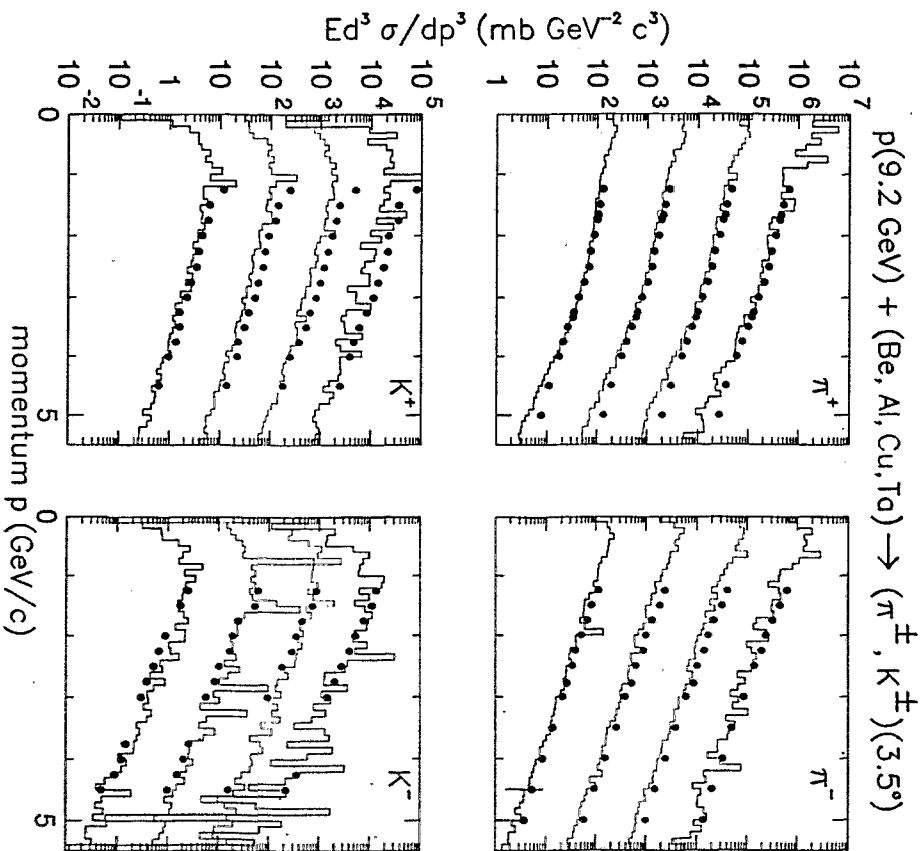


$y > 4.0$  invariant rapidity sections cross sections as a function of  $m_t - m_0$  with  $m_t^2 = m_0^2 + p_t^2$ . Spectra are multiplied by powers of 10. Data (points) from E802 collaboration [T. Abbott et al., Phys. Rev. D 45 (1992) 3096] are compared with ROC calculations (histograms)

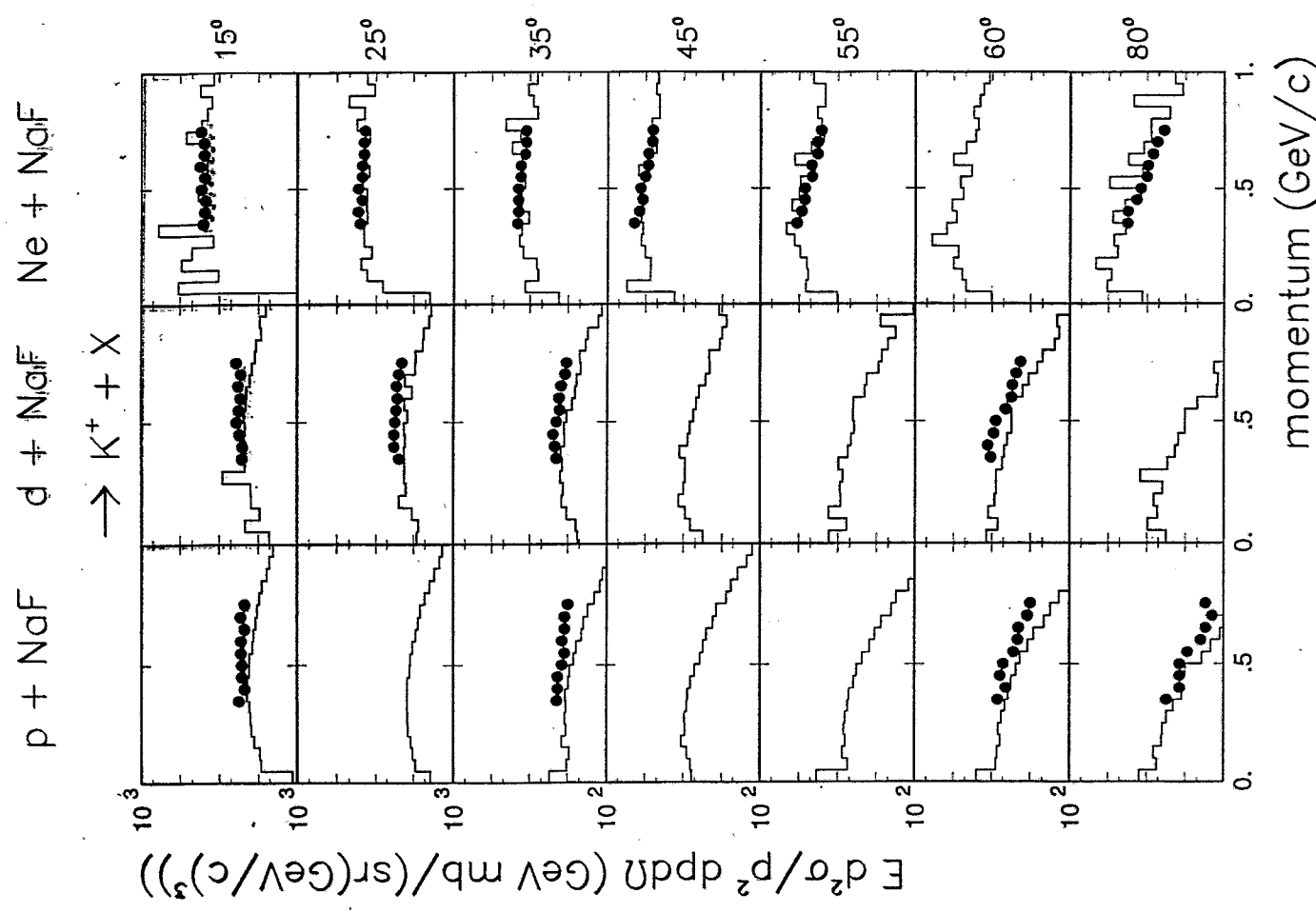
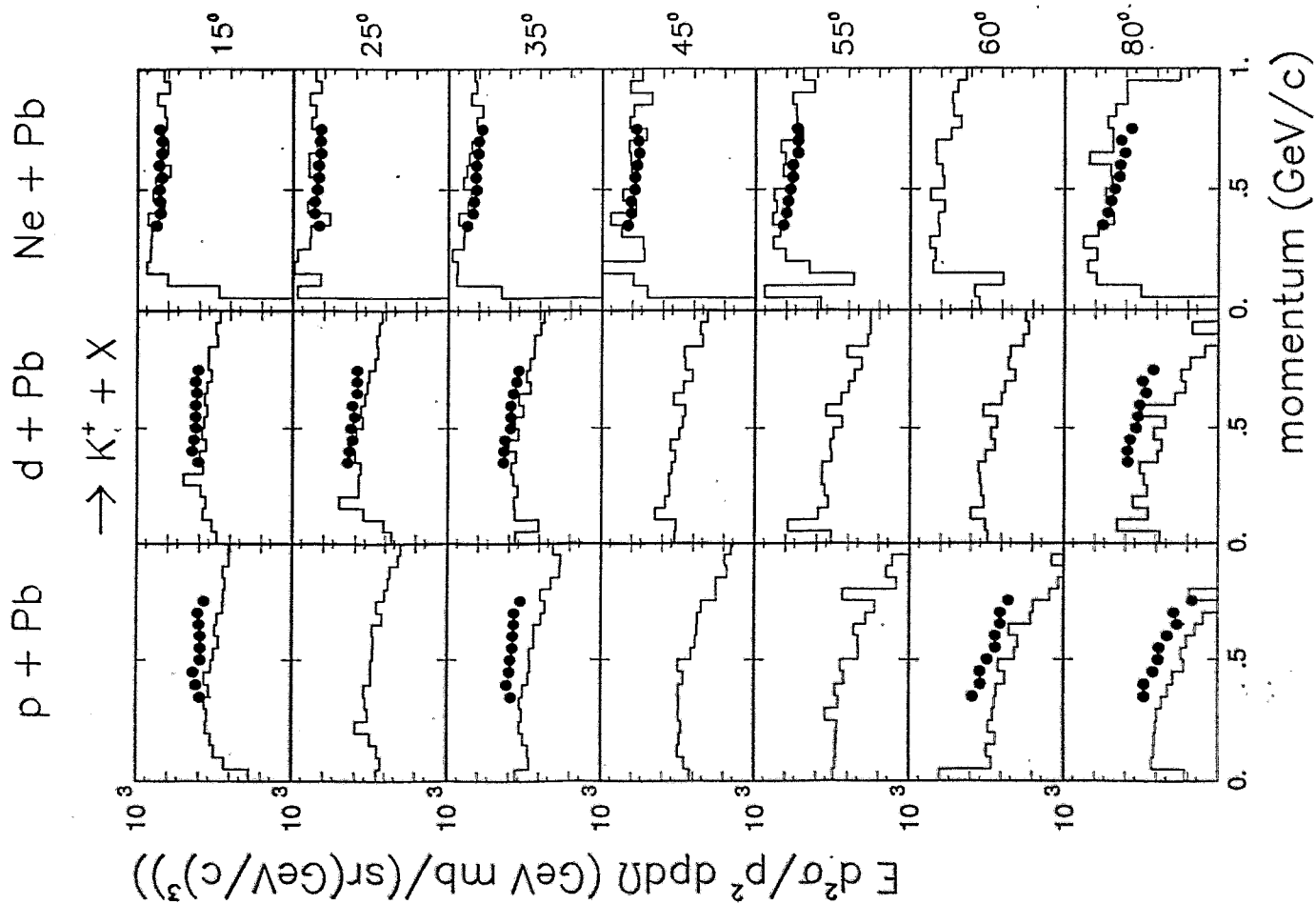
# Rapidity distributions



Data (blue points) from E802 collaboration [T. Abbott et al., Phys. Rev. Lett. **66** (1991) 1567, Phys. Rev. D **45** (1992) 3096] are compared with ROC calculations (red histograms).

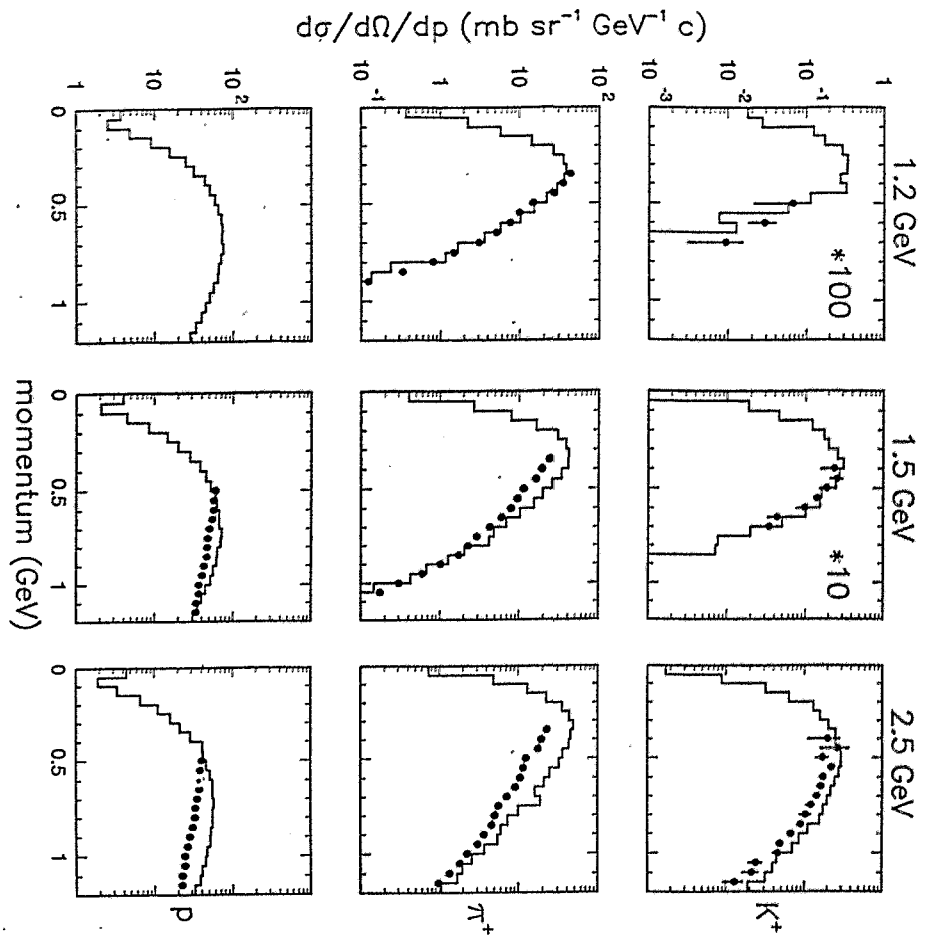






# Study of

## subthreshold $K^-$ production



### 1 Introduction

### 2 Model calculations

#### 2.1 Total cross sections and inclusive spectra

#### 2.2 Correlations

##### 2.2.1 Background

##### 2.2.2 Momentum spectra

##### 2.2.3 Invariant-mass spectra

##### 2.2.4 Missing-mass spectra

##### 2.2.5 Ratio of kaon- to pion-pair production

### 3 Experimental set-up

#### 3.1 General layout

#### 3.2 Momentum and angular acceptance

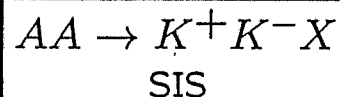
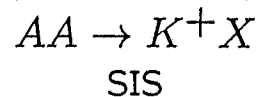
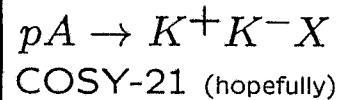
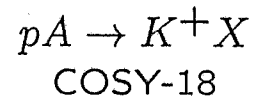
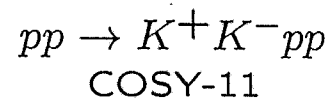
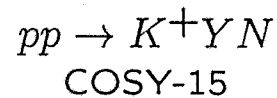
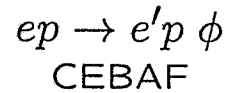
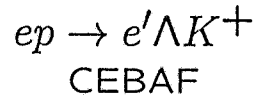
#### 3.3 Particle identification

#### 3.4 Resolution

#### 3.5 Counting rates

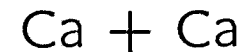
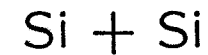
### 4 Proposed measurements

## Near- and sub-threshold strangeness production

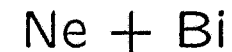


## Data subthreshold $K^-$ production

- available



1.0 ... 2.1 GeV per nucleon



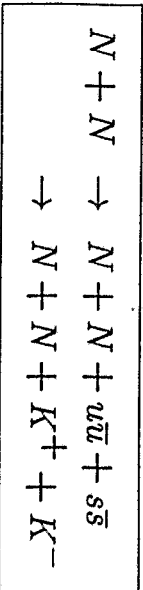
1.6 ... 2.0 GeV per nucleon

- not available

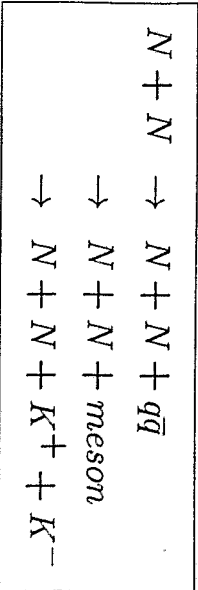
data from hadron-nucleus

# $K^-$ production

## 1. direct



## 2. via mesonic resonances



- well established:

$$\phi(1020) \quad \Gamma = 4.2 \text{ MeV}$$

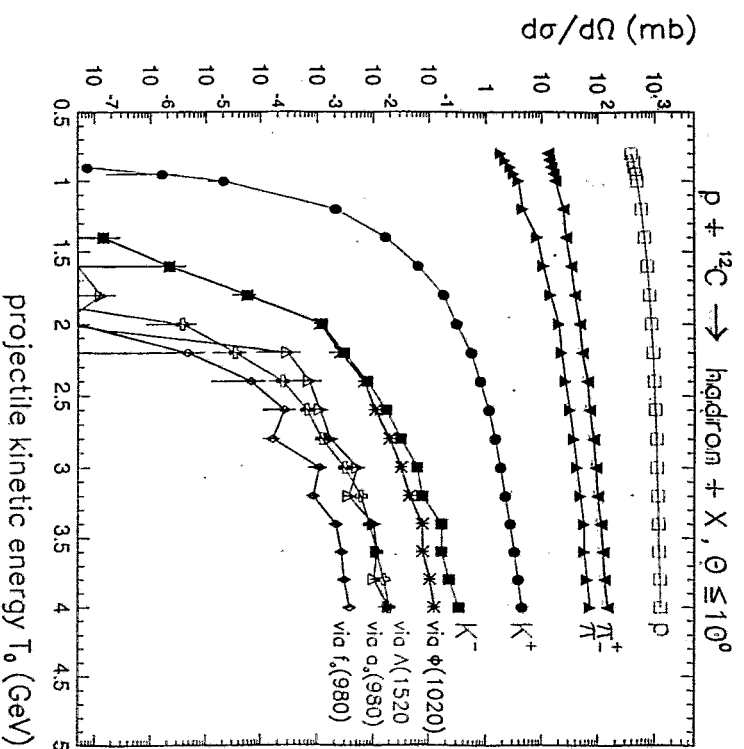
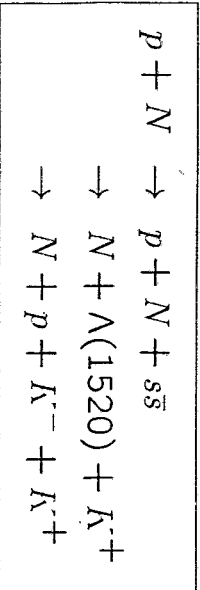
- structure under discussion:

$$a_0(980) \quad \Gamma = 50 \dots 300 \text{ MeV}$$

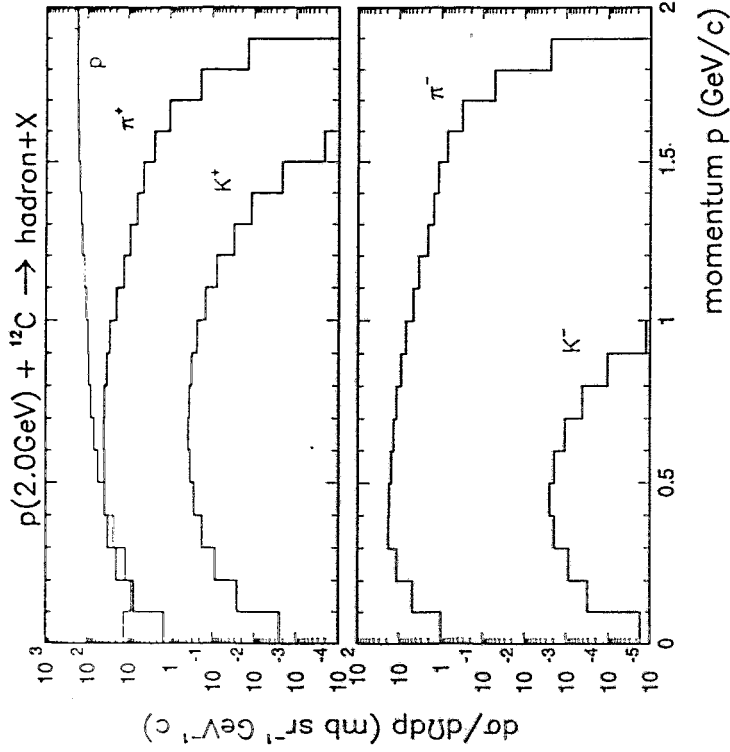
$$f_0(980) \quad \Gamma = 40 \dots 400 \text{ MeV}$$

## 3. via baryonic $\Lambda(1520)$ resonance

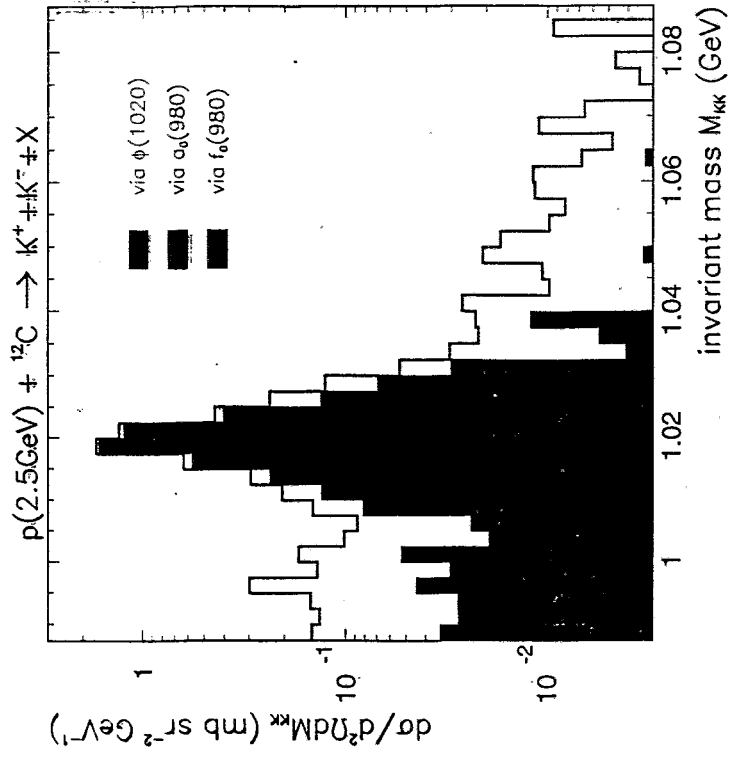
$\Gamma = 15.6 \text{ MeV}$



Energy dependence of differential cross sections calculated with the ROC model. In case of  $K^-$  production the contributions from intermediate resonances are indicated

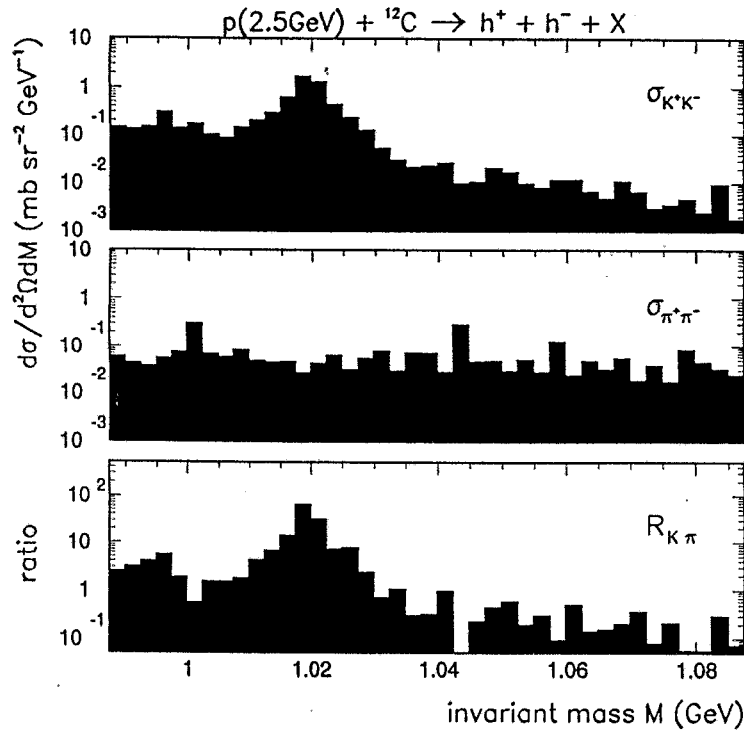


Calculated momentum spectra of positively and negatively charged particles produced in  $p^{12}\text{C}$  interactions at angles  $\Theta \leq 10^\circ$



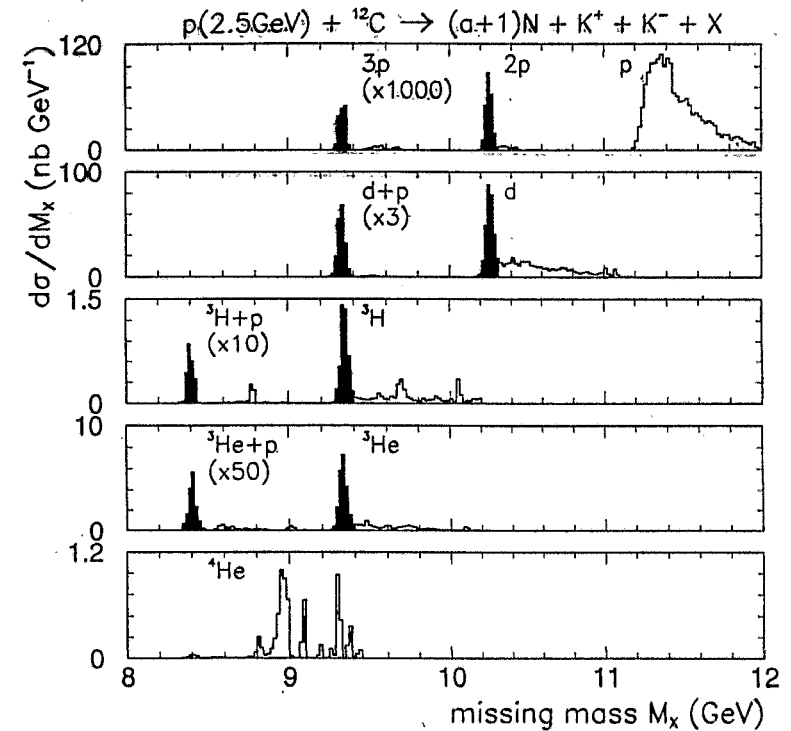
Calculated  $K^+K^-$  invariant-mass spectrum for emission angles  $\theta \leq 10^\circ$

- strength of  $\phi(1020)$  production
- propagation of  $\phi(1020)$ ,  $K^+$  and  $K^-$  through nuclear matter

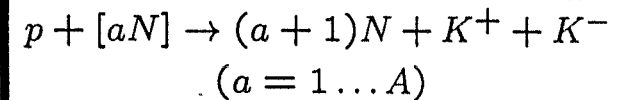


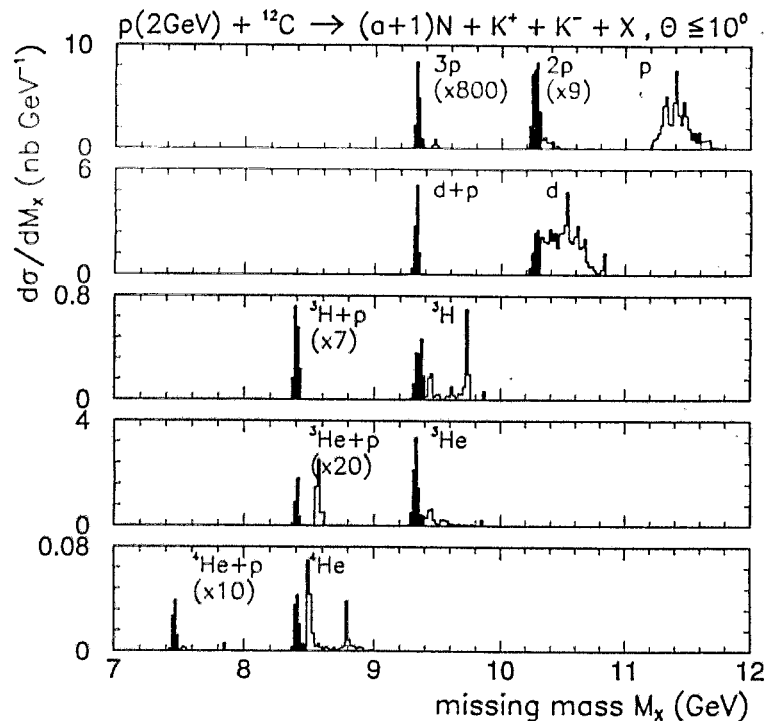
Calculated invariant mass spectra of kaon ( $\sigma_{K^+K^-}$ ) and pion pairs ( $\sigma_{\pi^+\pi^-}$ ) and the ratio  $R_{K\pi} = \sigma_{K^+K^-} / \sigma_{\pi^+\pi^-}$  for  $p^{12}\text{C}$  interactions at 2.5 GeV

- enhanced strangeness production due to locally heated nuclear matter?
- admixture of  $s\bar{s}$  component to the wave function of nucleons???

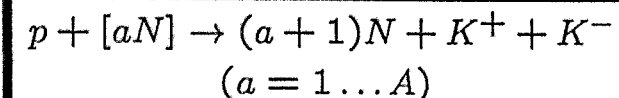


Calculated missing mass spectra from  $p^{12}\text{C}$  interactions at 2.5 GeV for the production of  $K^+/K^-$  pairs accompanied by  $(a+1)$  nucleons with  $a$  being the number of participants according to





Calculated missing mass spectra from  $p^{12}\text{C}$  interactions at 2.0 GeV for the production of  $\text{K}^+/\text{K}^-$  pairs accompanied by  $(a+1)$  nucleons with  $a$  being the number of participants according to



## Counting rates

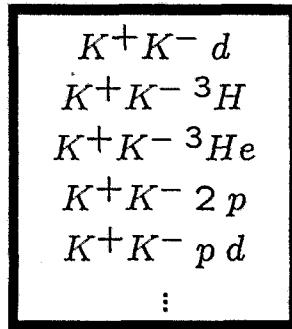
Decay-in-flight and detection efficiencies of 40% for  $\text{K}^+$ , 80% for  $\text{K}^-$  and 90% for all other particles have been taken into account. Counting rates smaller than  $1 \text{ h}^{-1}$  have been omitted (except for  $\text{K}^+\text{K}^-$  at 1.5 GeV)

Energy/GeV	2.5	2.0	1.5
Luminosity/cm <sup>-2</sup> s <sup>-1</sup>	$4 \cdot 10^{32}$	$3 \cdot 10^{32}$	$2 \cdot 10^{32}$
Detected particles	counts/h		
$\text{K}^+\text{K}^-$	2300	140	0.05
$\pi^+\pi^-(M_{\pi\pi} \geq 0.98\text{GeV})$	3000	300	5
$\text{K}^+\text{K}^- 2p$	50	—	—
$\text{K}^+\text{K}^- d$	200	20	—
$\text{K}^+\text{K}^- dp$	20	2	—
$\text{K}^+\text{K}^- {}^3\text{He}$	5	3	—
$\text{K}^+\text{K}^- {}^3\text{H}$	2	1	—

# Proposed measurements

Energy and target mass number  
dependence of

1. invariant-mass spectra  $K^+K^-$ 
  - strength of  $\phi(1020)$  production
  - propagation of  $\phi(1020)$ ,  $K^+$  and  $K^-$  through matter
2. ratio of  $K^+/K^-$  to  $\pi^+/\pi^-$  pair production
  - production of strange and non-strange particles at the same transferred four-momentum
3. missing-mass spectra



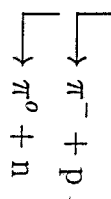
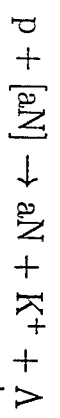
- determination of number of participants
- key for the understanding of the reaction mechanism



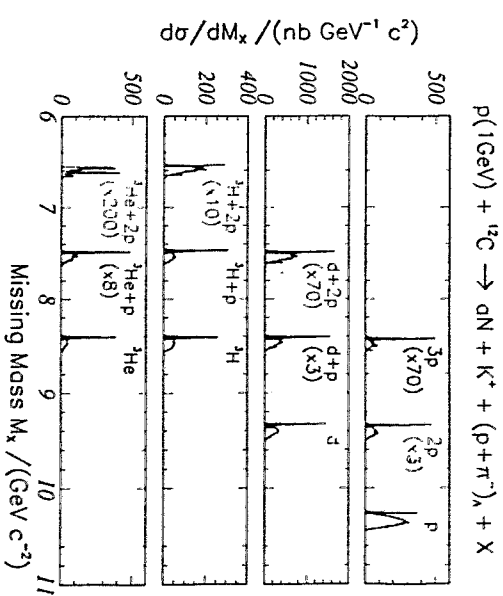
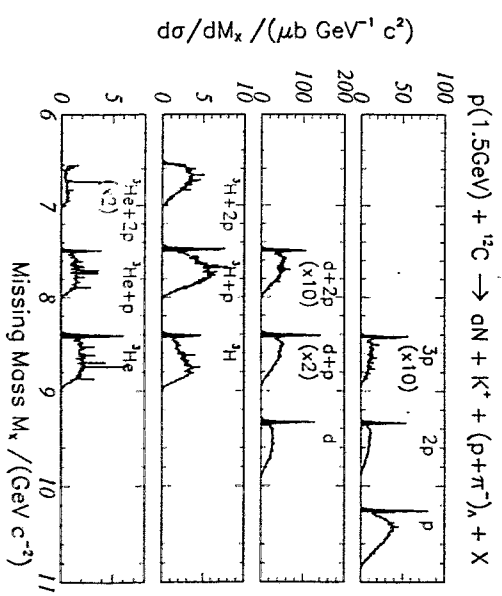
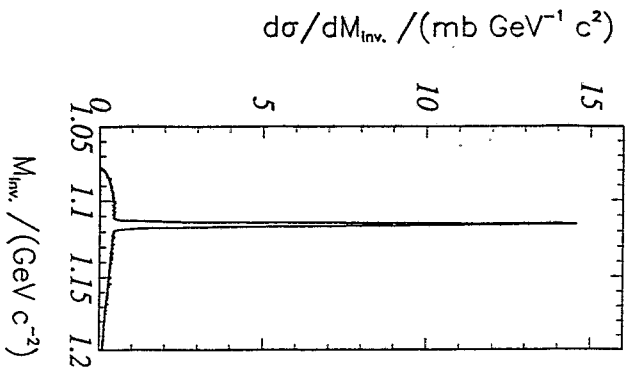
C. Schneider  $K^+$  experiments at ANKE

# 4π-Geometrie

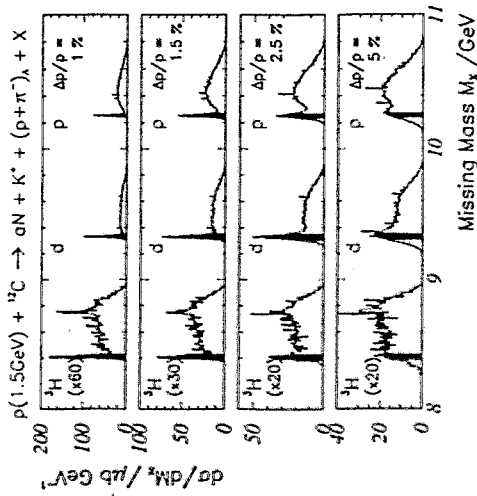
Besonderheit der K<sup>+</sup>-Missing Mass-Messung



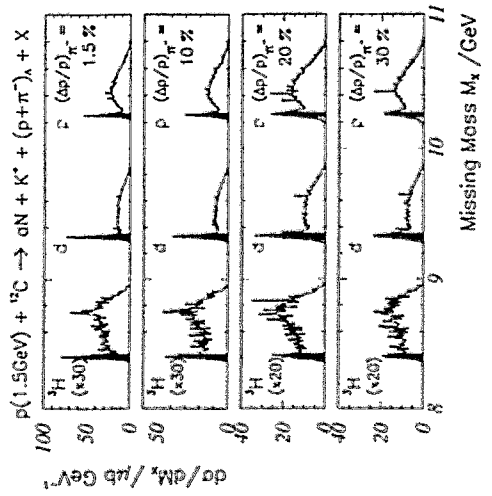
$$M_{Sp}^2 = p_{Sp}^2 = (p_{ini} - p_{K^+} - p_{p_\Lambda} - p_{\pi_\Lambda^-} - \sum_{i=1}^d p_i)^2$$



# Impulsauflösung an ANKE

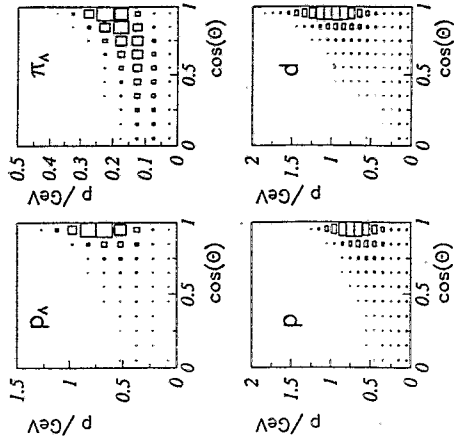


# Auflösung mit 4π-Pionen-Detektor

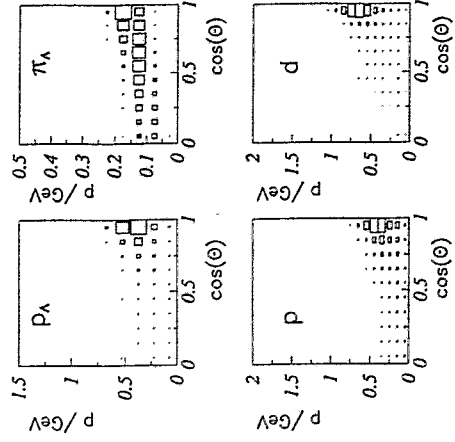


# Winkel-Impuls-Korrelationen

## Projektilenergie 1,5 GeV



## Projektilenergie 1,0 GeV



### Raten am ANKE-Spektrometer

Energie $T_N$ / GeV	1,5	1,0
Luminosität/cm <sup>-2</sup> s <sup>-1</sup>	$3 \cdot 10^{32}$	$3 \cdot 10^{32}$
Gemessene Teilchen	Teilchen/h	
$K^+\pi^-pp$	930	0,0015
$K^+\pi^-ppp$	-	-
$K^+\pi^-pd$	60	0,3
$K^+\pi^-p^3H$	-	-

### Raten mit 4 $\pi$ -Pioner-Detektor

Energie $T_N$ / GeV	1,5	1,0
Luminosität/cm <sup>-2</sup> s <sup>-1</sup>	$3 \cdot 10^{32}$	$3 \cdot 10^{32}$
Gemessene Teilchen	Teilchen/h	
$K^+\pi^-pp$	23000	3
$K^+\pi^-ppp$	36	-
$K^+\pi^-pd$	2040	39
$K^+\pi^-p^3H$	18	2

H.W. Barz    Calculations of  $K^\pm$  spectra

# CASIMIR (1980-85)

4. Starre + H<sub>2</sub>

Dubna : INC  
CERN :  $\pi, N$

$E/A = 2 \dots 4 \text{ GeV}$

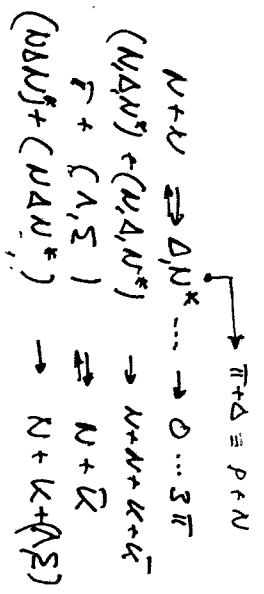
## Tafeln:

$$N^+ \Delta^{++} \dots < N^* \xrightarrow{\tau=K}$$

$$\bar{K}^{\pm 0} (p=2\pi)$$

$$K, \bar{K}^{\pm 0}, K^{\pm}, \bar{K}^{\pm 0}$$

## Reaktionen:



## Querschnitte:

$\sigma_{Tf}$ ;  $\Delta N^* \Rightarrow$   
(Resonanz +  $K_0$ )  
Frophenävarianz, isotropie

## kein Potential

## Mehrteilchenprozesse:

$\sigma \sim A^{1/3} \cdot \Delta^{1/3} \cdot n$   
 $\sigma_T \sim A^{5/3}$  (Volumen)  
 $\sigma_{K^+} \sim A^{6/3}$   
 $\sigma_{K^-} \sim A^{7/3}$   
 $\sigma_{\pi^+} \sim A^{8/3}$   
 $\sigma_{\pi^-} \sim A^{9/3}$   
 $\sigma_{N+K} \rightarrow K^-$

## Beispiele:

1)  $e + Ta \quad E/A = 536 \text{ GeV}$

2)  $Si + Si, \quad E/A = 2.1 \text{ GeV}$

$\rightarrow K^-$ , in wenig isotropie

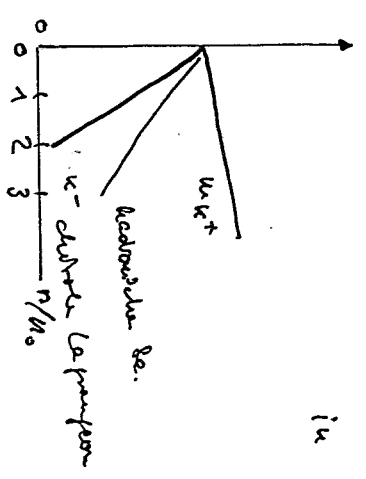
- a)  $\pi + A \rightarrow K^+ N \quad 75\%$
- b)  $N + K \rightarrow N + K + K^+ K^- \quad 25\%$

## Vergleich: $K (1984)$

(i: & Fang &  $K_0$ ;  $\pi + K \rightarrow K^+ N (25\%)$   
neglected

$N + K \rightarrow K^+ K^+ N$   
in medium

$\sigma_{\text{dhn}} = 3 \times \sigma_0$



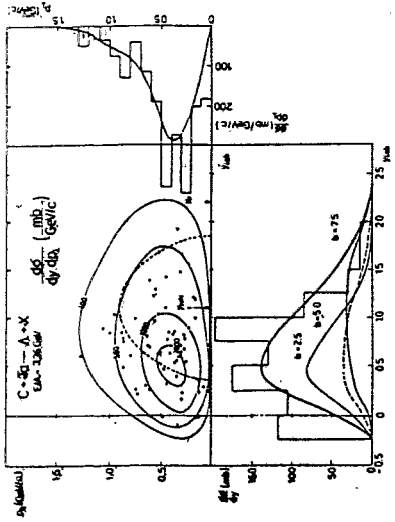


Fig. 12. Centour plot in the rapidity plane of the calculated differential cross section  $d\sigma/dy dp_T$  for A-production. The full circles represent the 65 A-particles detected in the reaction C+Ta at  $E_{lab}/A = 2.8$  GeV [ref. 1]. The dashed line shows the kinematical limit of the reaction NN→N<sub>1</sub>N<sub>2</sub>K. The arrows indicate the position of the NN system and projectile on the y-axis, respectively. The histograms are experimental results. The different curves in the rapidity spectra (labelled by the impact parameter b) show how the effect of flowing down the A-particles increases with decreasing impact parameter.

TABLE I  
Comparison between calculated and measured partial cross sections and mass multiplicities

Type	Cascade calculations		Experiment <sup>1)</sup>	
	$\sigma_i$ (mb)	$\langle n_i \rangle$	$\sigma_i$ (mb)	$\langle n_i \rangle$
had.	3 200		$3445 \pm 140$	
$\pi^+$	11 800	4.3	$11 800$	$3.4 \pm 0.2$
$\pi^-$	14 400	4.4	$12 800$	$3.7 \pm 0.3$
$K^+$	11 900	3.8	$94 \pm 21$ <sup>2)</sup>	$0.625 \pm 0.006$
$K^-$	94	0.028		
$\Lambda$	10	0.046		
$\Sigma$	14	0.057		
$\Lambda + \Sigma$	24	0.065	$217 \pm 35$ <sup>2)</sup>	$0.083 \pm 0.01$
$K^*$	E.4	0.0026		

<sup>1)</sup> Ref. 1), <sup>2)</sup> Ref. 2).

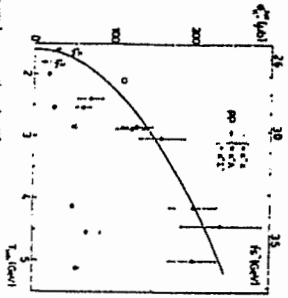


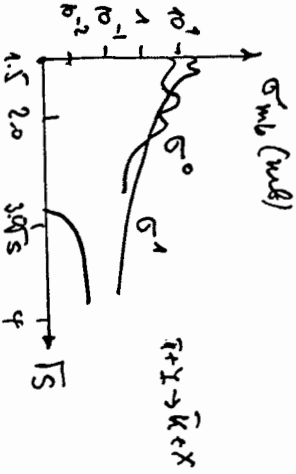
Fig. 3. Total and partial cross sections for  $\pi^+$  production in  $pp$  collisions. The full line indicates the fit used in (2.16).

where  $K_{1i}$  is their relative weight depending on energy. The only absolute weights of the different channels known at present seem from the experiment [1] mentioned above:  $\sigma_n$ ,  $\sigma_p$ ,  $\sigma_{\pi^+}$ ,  $\sigma_{\pi^-}$ ,  $\sigma_{\pi^0}$ ,  $\sigma_{\pi^+}$ ,  $\sigma_{\pi^-}$ ,  $\sigma_{\pi^0}$  (31:47:13). In addition, at two other energies the relative weights are known from best fits in the phase-space model to experimental data [2]. This information is summarized in our fit

$$K_{1i} = 4.35(T - 1.87) \exp(-4(T - 2.1)) + 1, \quad (2.16)$$

where  $T$  is the logarithm of the center-of-mass energy,  $\ln(s)$ , in GeV, and the constant term has been chosen to be the known reflection while for

$$\sigma_{\pi^+} = 125 \mu b \left( \frac{T}{\ln 2} - 1.575 \right)^{0.57}$$





B. Kämpfer    Current studies of strange particle production

# Let's Make Strangeness

## II. Heavy-Ion Collisions

**Present** Theoretical Activities in Rossendorf

## Hard QCD Processes at RHIC - LHC



beam 1      midrapidity      beam 2

1.  $\sqrt{s} = 200 - 5500$  AGeV: RHIC - LHC      B.K./Pavlenko (1996)

uds democracy  $\rightarrow$  charm becomes interesting

2.  $E_{lab} = 158$  AGeV: SPS      B.K. (1996)

kaons + Lambdas flow as anything else (protons, pions)

3.  $E_{lab} = 1 - 2$  AGeV: SIS      Kolomeitsev/Voskresensky/B.K. (1996)

explorative study of in-medium effects

large-angle scattering  $\rightarrow$  large  $t \rightarrow$  perturbative QCD processes

u,d,s are treated on equal footing  $\rightarrow$  no exceptional rôle of strangeness  
(unless soft processes become important)



destructive interferences  $\rightarrow$  no liberation of u,d,s towards midrapidity  
charm becomes interesting:  $c =$  lightest of heavy quarks

attacked problems:

- primordial vs. thermal c production

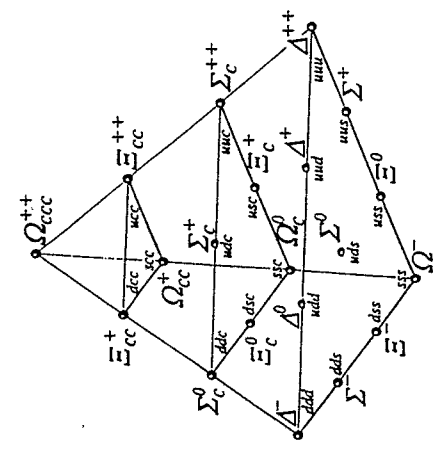
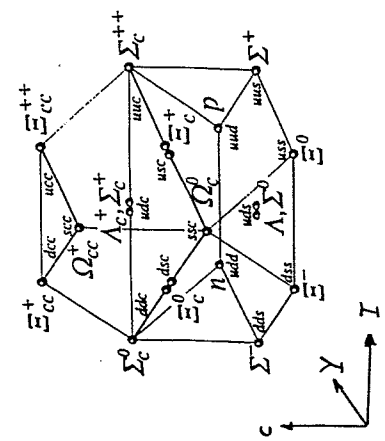
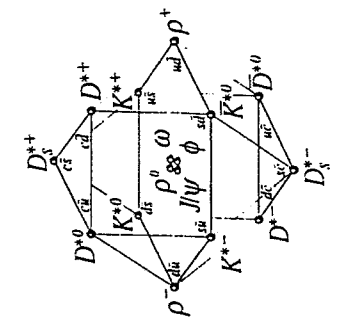
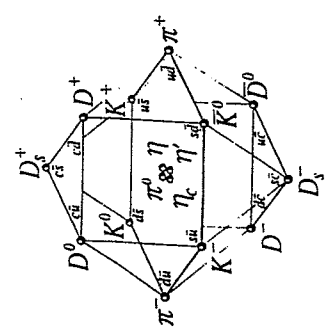
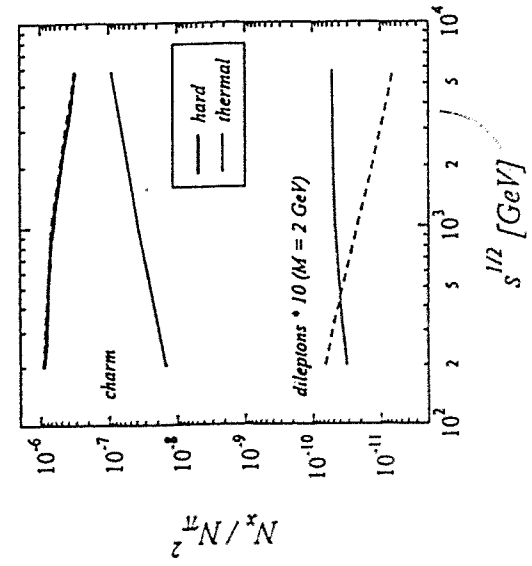
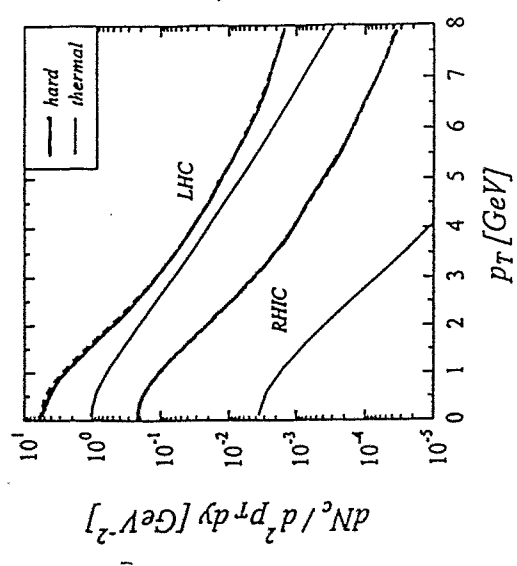
- open charm decay:  $c \bar{c} \rightarrow D, \bar{D}$

$D, \bar{D} \rightarrow \mu^\pm +$  anything  $\rightarrow$  uncorrelated lepton pairs

$\rightarrow$  huge combinatorical background for dileptons

$\rightarrow$  give up the hope for a thermal signal?

nuclear  
gluon  
shadowing  
→ depletion



Kaons flow as anything else in Pb + Pb at 158 AGeV

NA 49 preliminary data

- thermal model:  $T, \mu \rightarrow$  local momentum distribution
- hydro model:  $u, \mu \rightarrow$  flow
- + long. boost invariant flow (axisymmetry)
- + linear transverse flow profile
- + Cooper-Frye formalism with unique freeze-out time

$$\frac{dN^i}{m_{\perp} dm_{\perp} dy} = N_i \int_0^1 d\xi \xi m_{\perp} I_0 \left( \frac{p_{\perp} \sinh(\rho)}{T} \right) K_1 \left( \frac{m_{\perp} \cosh(\rho)}{T} \right),$$

$$\rho = \text{arctanh}(v_{\perp}(\xi)), \quad v_{\perp}(\xi) = \frac{3}{2} v_{\perp}^{aver} \xi,$$

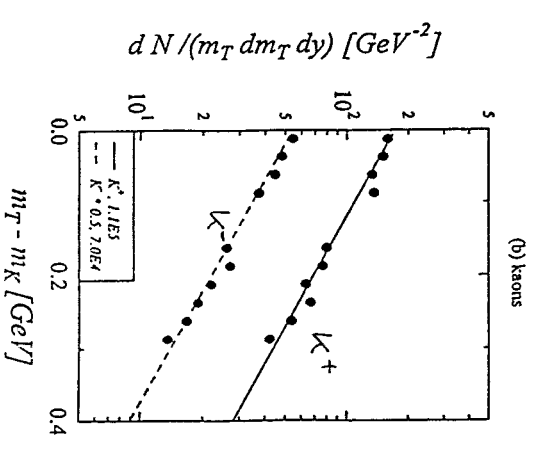
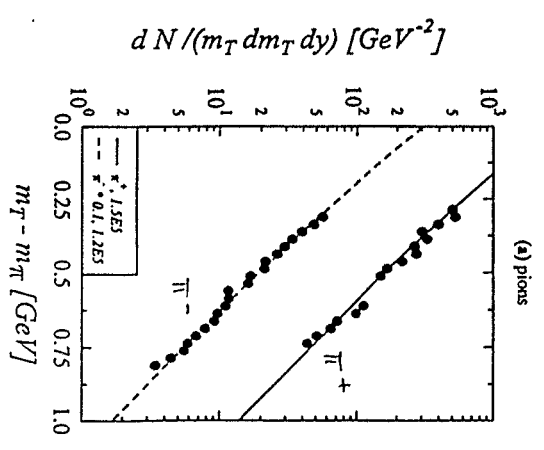
$$N_i = g_i R_{f.o.}^2 T_{f.o.} \lambda_i \exp\left\{\frac{\mu_i}{T}\right\} / \pi (\hbar c)^3$$

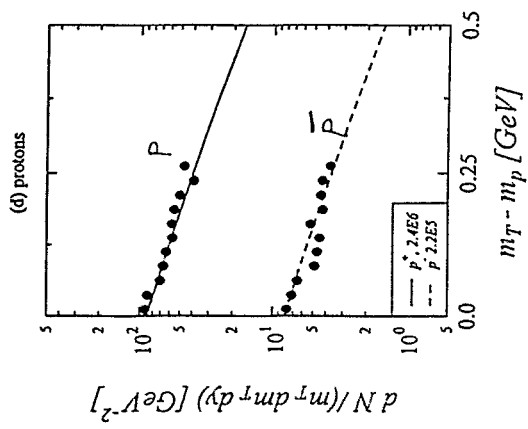
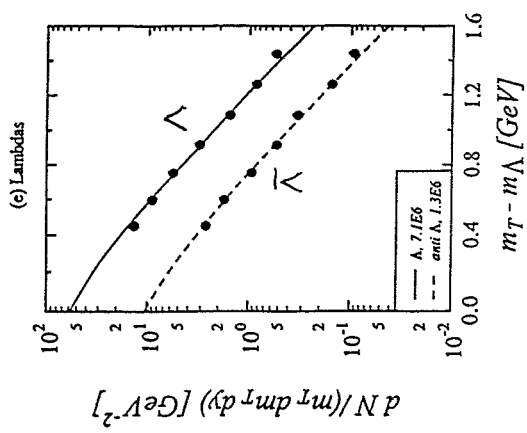
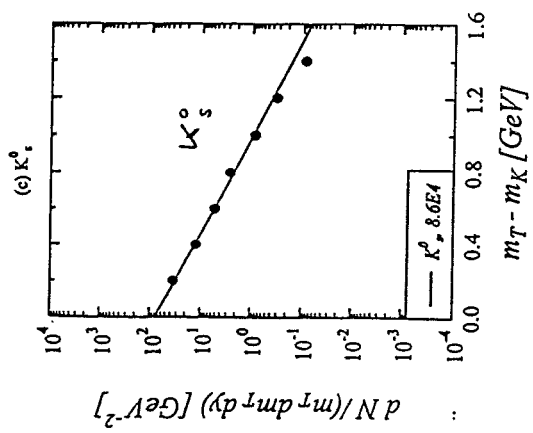
NA 49 normalized

NA 44 unnormalized, wider  $p_{\perp}$  ranges

$$T = 120 \text{ MeV}$$

$$\langle v_{\perp} \rangle = 0.43 c$$





# K<sup>-</sup> Spectra in HICs at BEVALAC/SIS Energies

studies of in-medium effects:

Brown/Ko/Wu/Xia (1991)  $M^*(T, \rho) \rightarrow \sigma(T, \rho)$

Li/Ko (1996)  $\omega_\pi(k; T, \rho) \rightarrow \sigma(T, \rho)$

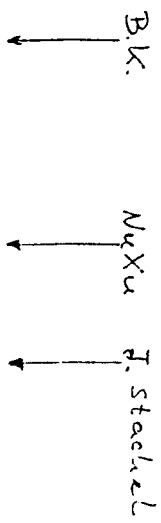
Kolomeitsev/Voskresensky/B.K. (1995)  $K^-$  quasiparticle excitations

Waise et al (1994/96)

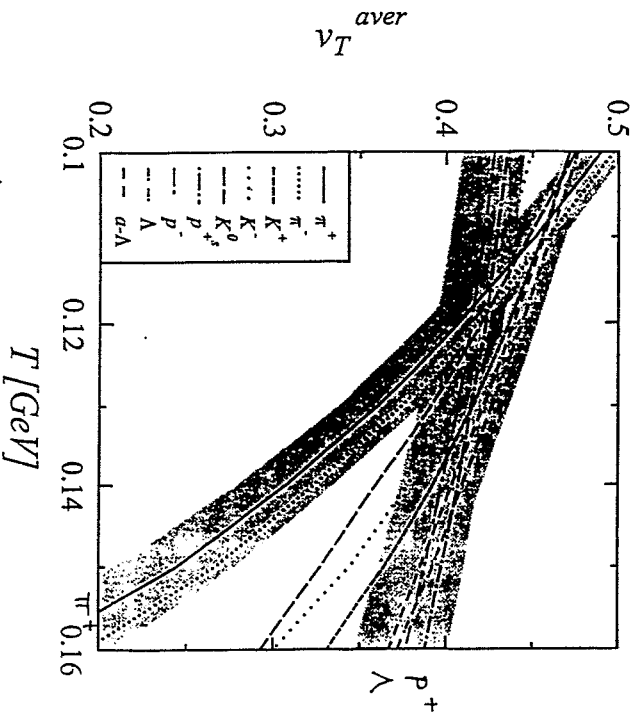
extended studies by Brown/Rho ... Muto ... Yabu ... Kohodera since 1992

K condensation

new: 2<sup>nd</sup> branch with  $K^- = \Lambda p^{-1}$



Fit of the NA49 slope parameters



explorative study of  $K^-$  freeze-out:

1. fireball model:

(a) thermal + chemical equilibration

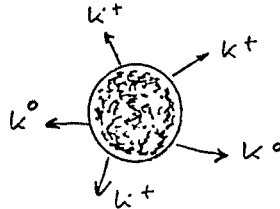
(b) simplified dynamics

(c) allows complicated dispersion relation

→  $T(t), \rho(t)$

2. leakage of  $K^+$ :  $\lambda_{K^+} \gg \lambda_{K^-}$

→ strangeness destillation



3. adjust  $\mu_{K^+}$  from  $S = 0$  and  $N_{K^+}^{exp}$

→ s sits mainly in  $\Lambda, \Sigma$

→  $\sigma_{K^+}$  is needed

	$E_{lab}$ [AGeV]	$\sigma_{K^+}$ [mb]	
Ne + NaF	2.1	$23 \pm 8$	Schnitzer et al. (1989)
-"-	1.0	$0.3 \pm 0.1$	Grosse (1993) KaoS
Au + Au	1.0	$41 \pm 7$	Miskovic et al. (1994) KaoS

used for interpolations

4. procedure for hopping on shell: time scale arguments →

- upper branch: frozen-in spectrum

- lower branch: change to vacuum spectrum

5. results for

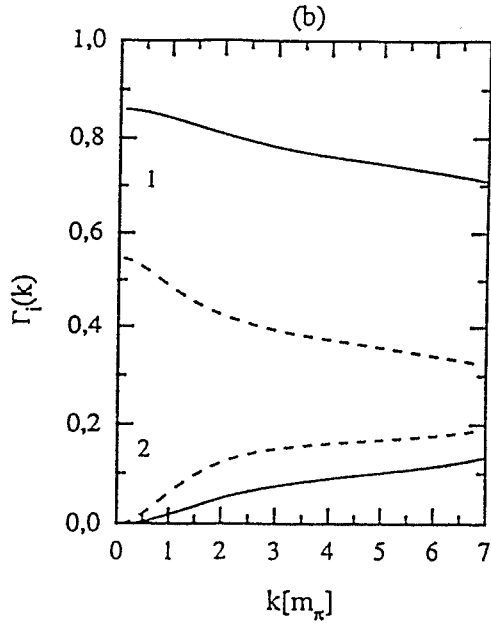
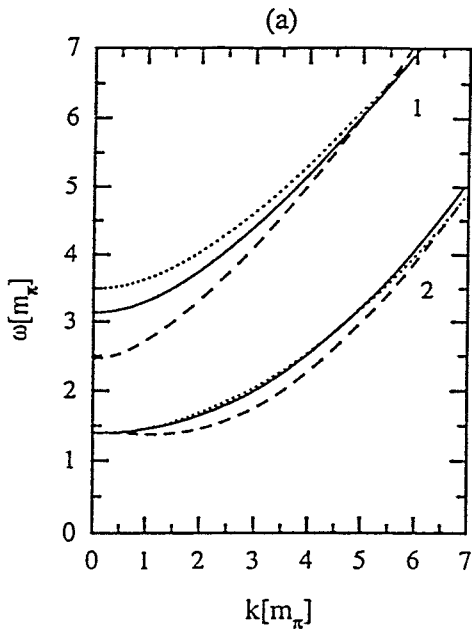
	$E_{lab}$ [AGeV]	
Si + Si	2.10	Barsch et al. (1985)
Ne + NaF	2.10	Shor et al. (1989)
Ni + Ni	1.85	Schröter et al. (1994) FSR
Si + Si	1.65	Carrol et al. (1988)
Si + Si	1.40	Shor et al. (1989, '92)
Si + Si	1.16	-"-

$N_{\bar{K}^+} + N_{\bar{K}^0}$  1.8 KaoS under consideration

dispersion relation

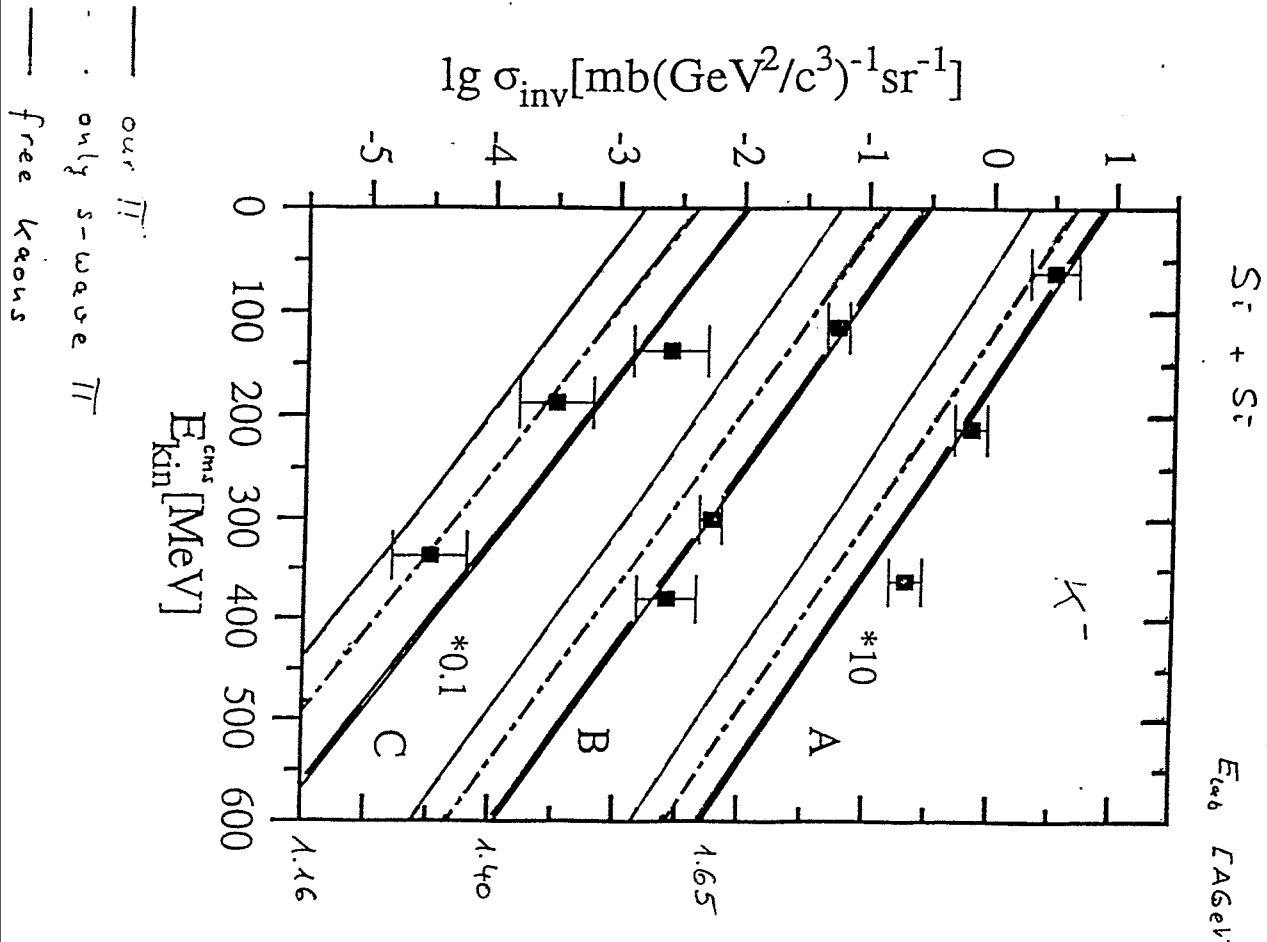
occupation factors

$K^-$



$m_1^*$ : weaker density dependence than Weise et al. (1996)

—  $0.6 \rho_0$   
 - - -  $3 \rho_0$   
 .....  $\rho_0 \rightarrow 0$





Au + Au

