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A workflow for the sustainable development of closure models for bubbly flows

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Abstract

Many years of research in developing closure models for polydisperse bubbly flows have produced a plethora of empirical and semi-empirical models. The continuous development and analysis of such models requires their constant validation with the steadily increasing number of validation cases in the literature.

In this paper we present a pipeline for the fully-automated analysis of OpenFOAM simulations using the Snakemake workflow management system. The pipeline is applied to an extensive collection of well-established validation cases for bubbly flows and allows the fast and efficient production of large amounts of results that are summarized in well-structured reports. An optional post-processing step introduces a fuzzy logic controller developed for the detailed analysis of these results by quantifying the agreement of the simulation with the available experimental data. It is demonstrated how such quantification enables the systematic evaluation of new closure models and contributes to a more sustainable model development.

Keywords:

Baseline, bubbly flow, OpenFOAM, workflow, artificial intelligence

1. Introduction

Understanding and predicting multiphase flows is crucial for the development of reliable, safe and efficient devices in the nuclear, chemical, energy and oil-and-gas industry. Computational fluid dynamics (CFD) has proven to be an indispensable tool that adds to a better understanding of multiphase flows on all relevant scales, from single bubbles to the flow in large industrial components. Much effort was focused on achieving predictive capabilities of CFD simulations during the last decades. Today, the Eulerian-Eulerian two-fluid methodology is widely used for analysing multiphase flows on the industrial component-scale. Low computational cost and great flexibility in terms of possible flow geometries have made it the state-of-the-art approach for multiphase flow analysis in the industry. The reliability of results depends on the availability of accurate closure models and their correct application. Although good predictions can often be obtained for single cases, there is an ongoing effort to reduce the empiricism of models in favour of more mechanistic formulations for a better accuracy and generality of these models.

Decades of developing new models for Eulerian-Eulerian CFD have produced a vast amount of literature on the subject, and a huge number of both models and validation cases [1, 2, 3]. For each required Euler-Euler closure a multitude of empirical or semi-empirical models exists in the literature from which the CFD engineer is free to choose. This accumulation of models makes it increasingly difficult to give best practice guidelines for the simulation of bubbly flows. Evaluating new models and comparing them against the plethora of available alternatives becomes an increasingly tedious endeavour.

However, the huge amount of data to be found in the literature offers the opportunity to apply workflow tools for a faster and more efficient processing of CFD data. In other fields of research, such as bio-informatics [4] and RNA sequencing in particular [5], the development of workflows has already proven to be fundamental for gaining a deeper understanding of large data sets. The enormous amount of CFD data produced from existing validation cases and the increasing number of closure models make a fast and efficient tool to process all this data a crucial part of the Euler-Euler model development in the future. Furthermore, such automation allows us to explore the possibility of including data science and artificial intelligence tools in the analysis and evaluation process of new Euler-Euler models.

37

38 In Section 2 of this paper we describe the current status of Eulerian-
39 Eulerian CFD modeling of multiphase flows. We will review the conven-
40 tional way of developing and testing new models and highlight the issues
41 that arise from following such an approach. We then present the alternative
42 ‘baseline’ strategy [6] developed at Helmholtz-Zentrum Dresden-Rossendorf
43 (HZDR), which aims at converging towards a fixed set of universal closure
44 models, so-called baseline models. An overview of the current collection of
45 validation cases for baseline model testing available at HZDR is given. In
46 Section 3 we then present the Snakemake workflow, which was developed
47 for the fully-automated pre-processing, running and post-processing of the
48 extensive amount of OpenFOAM cases in our collection. Section 4 will apply
49 fuzzy logic, a subset of artificial intelligence, for the evaluation of simulation
50 results. We will describe the parts of a fuzzy logic controller, designed to
51 infer from two error metrics an output metric that allows us to compare the
52 performance of new Euler-Euler models with the baseline model set. Results
53 of a demonstration case are then presented in Section 5 where we test a new
54 lift force correlation against the current baseline model. We describe the per-
55 formance of the workflow and present validation graphs of selected cases to
56 demonstrate the fuzzy logic evaluation. An overview of fuzzy logic results for
57 the entire case collection aims to demonstrate the potential of such artificial
58 intelligence tools for a sustainable Euler-Euler model development. Conclu-
59 sions and an outlook to where our future work is going is given in Section
60 6.

61 2. Background

62 2.1. Conventional Euler-Euler model development

63 The description of two-phase flows with the Eulerian-Eulerian methodol-
64 ogy requires many closure models. Closure models need to describe all the
65 detailed flow phenomena, which the usually coarse computational grid can-
66 not resolve. For polydisperse bubbly flows a dozen such closures is needed:
67 interfacial force closures, i.e. drag, shear lift, turbulent dispersion, virtual
68 mass and wall lubrication forces [7], turbulence closures for the shear and
69 bubble-induced turbulence of the liquid phase [8], and closures describing
70 the polydispersity of bubbles, i.e. a population balance model, and models
71 for both coalescence and breakup events [9]. A lot of different model options
72 for each of these closures have emerged in the literature, each of which comes
73 with a multitude of adjustable model parameters.

74 Table 1 lists a selection of such models suitable for the modeling of bubbly
75 flows, part of which are provided by OpenFOAM [10] and by the *HZDR*
76 *Multiphase Addon for OpenFOAM* [11]. Listed are five drag models, three lift
77 models, three models for turbulent dispersion, two for virtual mass and four
78 for wall lubrication, three different turbulence models for the liquid and three
79 different models for bubble-induced turbulence, two different approaches for
80 population balance modeling, five different coalescence and four different
81 binary breakup models. These 34 options alone give a total of 129600 possible
82 model combinations. This number becomes even more extensive considering
83 all the models in the literature not yet included in the HZDR model library.
84 Numerous model parameters inherent in every sub-model further add to the
85 complexity. The description of polydisperse bubbly flows using the Euler-
86 Euler approach is inarguably based on a highly complex set of intricately-
87 linked models making the interpretation of CFD results extremely difficult.

Table 1: Closure models for polydisperse bubbly flow available with the *HZDR Multiphase Addon for OpenFOAM* [11]. The current baseline model set is indicated in bold text.

Required closures		Model options	Parameter
Interfacial forces	Drag	Ishii and Zuber [12]	-
		Schiller and Naumann [13]	-
		Tomiyama et al. [14]	-
		Tomiyama et al. [15]	-
		Tomiyama et al. [16]	-
Shear lift	Tomiyama et al. [17]	Legendre and Magnaudet [18]	-
		Moraga et al. [19]	-
		Burns et al. [20]	1
Turbulent dispersion	Gosman et al. [21]	Gosman et al. [21]	1
		Lopez de Bertodano [22]	1
		Crowe et al. [23]	1
Virtual mass	Lamb [24]	Lamb [24]	-
		Hosokawa et al. [25]	-
Wall lubrication	Antal et al. [26]	Antal et al. [26]	2
		Frank [27]	3
		Tomiyama [28]	1
		k-omega-SST [29]	12
Turbulence	Shear-induced	k-epsilon [30]	6
		k-omega [31]	5
		Ma et al. [32]	-
Bubble-induced	Rzehak and Krepper [33]	Rzehak and Krepper [33]	-
		Sato and Sadatomi [34]	1
		Class method [35]	-
Poly-dispersity	Population balance	Ishii et al. [36]	-
		Liao et al. [9]	9
Coalescence	Coulaloglou and Tavlarides [37]	Coulaloglou and Tavlarides [37]	2
		Lehr et al. [38]	2
		Luo [39]	2
		Prince and Blanch [40]	3
		Liao et al. [9]	4
		Lehr et al. [38]	-
Breakup	Laakkonen et al. [41]	Laakkonen et al. [41]	4
		Luo and Svendsen [42]	3

88 There is no consensus about the use of any of those closure models. In the
89 literature usually a different set of models is chosen by each research group
90 [43, 1, 7, 44]. Model constants tend to be tuned for each specific validation
91 case. Despite a large number of publications on the model development
92 for the last two decades little progress is seen towards Eulerian-Eulerian
93 simulations with reliable predictive abilities [6].

94 2.2. The ‘Baseline’ Strategy

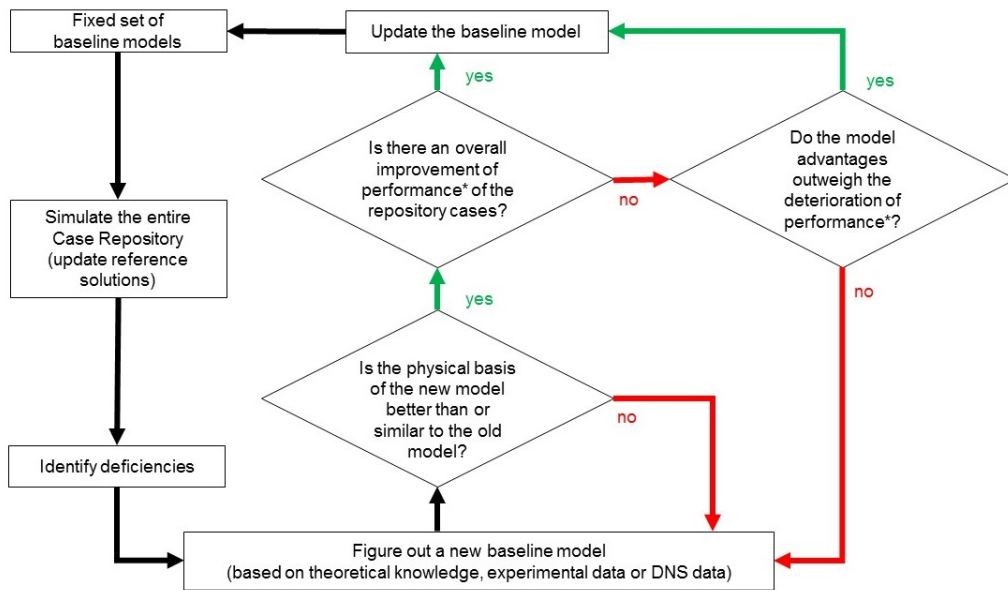
95 The aim of the baseline strategy at HZDR is to arrive at a single univer-
96 sal set of Eulerian-Eulerian two-fluid models that can predict bubbly flows
97 in any flow configuration. Baseline models should offer a certain range of
98 applicability regarding the local flow characteristics. The baseline model set
99 is fixed, as are the model constants. For different flow situations the contri-
100 bution of each of the phenomena listed in Table 1 will of course vary, but the
101 baseline model set should predict such changes without any further tuning.
102 As described by Lucas et al. [6] for the sake of generality the models chosen
103 for each phenomena should preferably be mechanistic models that are based
104 on local flow conditions rather than empirical models derived from observa-
105 tions made in a specific experiment. The baseline model set should produce
106 convincing results for a large range of different validation cases in order to
107 prove its predictive abilities for future cases.

108 Table 1 lists the current set of baseline models for polydisperse bubbly
109 flow at HZDR in bold letters. Find the detailed equations for these models
110 in Liao et al. [8]. Over the years the models listed here have proven to
111 repeatedly produce good results for a variety of cases [9, 7, 8].

112 Figure 1 illustrates the general process of updating this fixed set of base-
113 line models in case a new model has been developed or found in the literature.
114 In a first step the new model needs to be analysed regarding the model re-
115 quirements of the baseline model set. Various features need to be checked,
116 such as a physical and mechanistic basis of the model, its generality or its
117 derivation from advanced experiments. If the advantages of the new model
118 become apparent, it will then be tested in a next step. This part of the
119 process is essential as it aims to demonstrate an overall improvement of the
120 CFD predictions for a collection of cases. This case collection contains an
121 extensive selection of validation cases, which will be described in the next
122 section. Generally, a new model will replace the current baseline model if an
123 improvement for the majority of our validation cases can be demonstrated.

124 During the continuous model development we try to identify deficiencies of
 125 models, in which we should invest our efforts for further improvement.

126 As illustrated on the right hand side of the flow diagram in Figure 1 a
 127 model update can be considered even if overall case results do not improve.
 128 The advantages of a new model then need to outweigh the deterioration of
 129 results. The coupling of physical phenomena is complex making a straight-
 130 forward model evaluation impossible at times. Worse results obtained with
 131 a better model can be caused by the interdependence of the current set of
 132 baseline models, where potential shortcomings of one model are possibly
 133 compensated by the tuning of another.



*Performance= agreement with experiments/DNS and numerical stability/computing time

Figure 1: Schematic of the process employed to update baseline models.

134 2.3. The current collection of cases at HZDR

135 As described above, the process of testing new models involves the simu-
 136 lation of a large number of validation cases. The case collection at HZDR
 137 currently contains 56 pipe and bubble column cases, with the case number
 138 continuously growing. Cases differ regarding their geometry, gas injection,
 139 bubble sizes, water quality etc. Keywords were introduced to categorise the

140 cases and their sub-cases as illustrated in Table 2. The keywords illustrated
141 are not complete, but rather form a starting point to label existing cases.
142 More cases are to be added in the future in order to diversify the collection
143 and its keywords, as well as to simply increase the amount of validation data.

144 Case setups are standardised using the best-practice guidelines given in
145 Lucas et al. [45] and simulated using the *HZDR Multiphase Addon for Open-*
146 *FOAM*, which was customized and extended for the various model develop-
147 ments at HZDR. All cases are under Git version control and managed in
148 GitLab [46]. GitLab Continuous Integration and Continuous Development
149 (CI/CD) mechanisms allow an efficient maintenance of the case collection,
150 as well as its extension by new cases.

Table 2: Overview of cases with all active keywords.

Cases		Geo-metry		Gas in-jection		Gas phases		Bubble size change		Bubble sizes		Water quality			State		Devel-opment		
		Pipe	Bubble column	Bottom	Wall	one-gas	multiple-gas	Fixed	Density-change	Coalescence-breakup	Monodisperse	Polydispersperse	Filtered	Tap water	Contaminated	Steady-state	Transient	Fully developed	Developing
Wang et al. (1987)	W1	X		X		X		X		X		X			X		X		
	W2	X		X		X		X		X		X			X		X		
	W3	X		X		X		X		X		X			X		X		
Liu and Bankoff (1993)	LB1	X		X		X		X		X		X			X		X		
	LB2	X		X		X		X		X		X			X		X		
Liu (1998)	L11A	X		X		X		X		X			X		X		X		
	L21B	X		X		X		X		X			X		X		X		
	L21C	X		X		X		X		X			X		X		X		
	L22A	X		X		X		X		X			X		X		X		
Pfleger (1999)		X	X			X			X	X		X			X			X	
Deen (2001)		X	X		X		X		X				X		X			X	
Hibiki (2001)	H11	X		X		X		X		X		X			X		X		
	H12	X		X		X		X		X		X			X		X		
	H13	X		X		X		X		X		X			X		X		
	H31	X		X		X		X		X		X			X		X		
	H32	X		X		X		X		X		X			X		X		
	H33	X		X		X		X		X		X			X		X		
Shawkat (2008)	S21	X		X		X		X		X		X			X		X		
	S23	X		X		X		X		X		X			X		X		
	S31	X		X		X		X		X		X			X		X		
	S33	X		X		X		X		X		X			X		X		
Hosokawa (2009)	H11	X		X		X		X		X			X		X		X		
	H12	X		X		X		X		X			X		X		X		
	H21	X		X		X		X		X			X		X		X		
	H22	X		X		X		X		X			X		X		X		
Akbar et al. (2012)	13		X	X			X			X		X				X		X	
	3		X	X		X		X		X		X			X		X		
Hosokawa and Tomiyama (2013)	H1	X		X		X		X		X			X		X		X		
	H2	X		X		X		X		X			X		X		X		
	H3	X		X		X		X		X			X		X		X		
	H4	X		X		X		X		X			X		X		X		
Kim (2016)	K1	X		X		X		X		X			X		X		X		
	K2	X		X		X		X		X			X		X		X		
	K3	X		X		X		X		X			X		X		X		
	K4	X		X		X		X		X			X		X		X		
Lucas et al. (2005)	fd_19	X		X		X		X			X	X			X		X		
	fd_37	X		X		X		X			X	X			X		X		
	fd_39	X		X		X		X			X	X			X		X		
	fd_41	X		X		X		X			X	X			X		X		
	fd_59	X		X		X		X			X	X			X		X		
	fd_61	X		X		X		X			X	X			X		X		
	fd_63	X		X		X		X			X	X			X		X		
	fd_85	X		X		X		X			X	X			X		X		
	d_19	X		X		X			X	X					X			X	
	d_37	X		X		X			X	X					X			X	
	d_39	X		X		X			X	X					X			X	
	d_41	X		X		X			X	X					X			X	
	d_59	X		X		X			X	X					X			X	
	d_61	X		X		X			X	X					X			X	
	d_63	X		X		X			X	X					X			X	
	d_85	X		X		X			X	X					X			X	
	Lucas et al. (2010)	30	X			X	X			X		X	X			X			X
		40	X			X	X			X		X	X			X			X
41		X			X	X			X		X	X			X			X	
42		X			X	X			X		X	X			X			X	
52		X			X	X			X		X	X			X			X	

151 *2.4. The challenge of evaluating new models*

152 Each case in the case collection produces results that are compared to
153 validation data, i.e. experimental data. Some fully-developed cases produce
154 steady-state results, for other transient cases the results need to be time-
155 averaged. Typical graphs for analyzing results are gas void fraction profiles,
156 liquid and gas velocity profiles, sometimes profiles of turbulent quantities,
157 such as the turbulent kinetic energy. Transient cases produce the respective
158 mean values of the same quantities.

159 In case a new model is tested the computed results additionally need
160 to be compared with the old baseline reference solution. For each of the
161 plots various curves need to be compared: the computed result using the
162 new model, the reference result obtained with the current baseline model set
163 and the measured data for validation. Examples of such graphs are given
164 in Figure 2. The reason why this kind of evaluation is a time-consuming
165 challenge is twofold:

166 First, the sheer number of results to evaluate is extensive and hard to
167 handle. It is difficult to demonstrate an overall improvement for the total
168 number of currently 56 cases, each of which produces three to five graphs.
169 Assuming only three graphs for each case, a total of 168 plots has to be
170 evaluated. These plots are typically scattered across case folders. The issue
171 becomes even more pressing with an increasing number of cases and plots,
172 which for baseline development purposes is intended. Therefore, a **workflow**
173 for an automated production of such graphs and their neat presentation in a
174 single report is developed, as will be presented in Section 3.

175 Second, the information in some graphs can be vague and the decision
176 if there is an improvement of results can become rather subjective. Plotted
177 results need to be evaluated and compared, which is typically done during
178 long and difficult discussions among experts. For a better qualitative judge-
179 ment and quantification of the performance of new models we will therefore
180 introduce a **fuzzy logic approach** in Section 4 that is meant to aid the
181 decision-making process.

182 3. Automation of cases in a workflow

183 Workflow engines are designed to automate the successive execution of
184 commands and applications for large-scale data analyses. The generation of
185 data via workflows follows so-called FAIR principles [47] for a good manage-
186 ment of scientific data, which should be transparent and reproducible. Out
187 of a large number of potential workflow systems (such as [48] etc.) for the
188 work presented here we chose Snakemake and developed a workflow, which
189 will be described in the next sections.

190 3.1. The Snakemake library

191 Snakemake is a general purpose Python library originally developed for
192 applications in the field of bio-informatics [4]. The library allows to build
193 complex algorithms that process large data-sets using scientific software, and
194 manages the resulting output.

195 As described by Evdokimov et al. [49] the Snakemake library provides
196 several features that make it a suitable framework for managing the extensive
197 amount of CFD simulations we are interested in here, and their subsequent
198 analysis:

- 199 • The syntax of Snakemake offers great flexibility in terms of the scripting
200 languages that jobs can be composed of, which allows individual case-
201 by-case setups.
- 202 • The library comes with interfaces to common cluster schedulers re-
203 quired for high-performance computing.
- 204 • Snakemake was built for parallization enabling us to spawn parallel case
205 jobs on separate nodes of a cluster to maximize speed. Furthermore,
206 it can adapt the number of jobs in execution to the allocated workflow
207 resources.
- 208 • Its modularity allows to rerun downstream analysis and re-process sub-
209 sets of jobs without the need to rerun the entire pipeline.
- 210 • The post-processing output is aggregated and put into a single place
211 with the possibility to include results of hundreds of cases.
- 212 • On the low-level a case-by-case approach allows to easily split work
213 among researchers in a team, and

- 214 • On the top-level common CI/CD software design practices are applica-
215 ble and allow the consistent integration of the library into our existing
216 case repository.

217 3.2. Workflow overview

218 The details of the workflow on both the case- and the top-level, are de-
219 scribed and illustrated in Evdokimov et al. [49]. The following section will
220 briefly summarize the main steps and workflow specifications relevant for our
221 baseline model development.

222 The workflow consists of the following three steps reflecting a *bottom-up*
223 method of determining job execution:

- 224 1. During a *configuration step* an algorithm searches in sub-folders for
225 **Snakefiles** that define the specifications of the pre-processing, solv-
226 ing and post-processing job for each individual case. **Snakefiles** are
227 designed in such a way that they allow the independent workflow ex-
228 ecution of a selection of cases. Larger cases that include extensive
229 parameter-variations (e.g. Lucas et al. [50] with hundreds of systematic
230 case setup variations) are setup via templates building file structures
231 and sub-cases. Once the *configuration* step has completed, the estab-
232 lished file structure is ready for launching the workflow.
- 233 2. The workflow then runs the selected cases during the *solution step*.
234 Workflow reports containing the plots of all the cases are produced
235 using the report-generating feature embedded in the Snakemake library.
- 236 3. A third optional *post-processing* step produces a case-by-case overview
237 of the agreement of the computed results with the validation data. This
238 step is particularly important for the testing of new baseline models and
239 incorporates the fuzzy logic system described in Section 4. Computed
240 results are not only compared to the validation data, but also to the
241 reference solution obtained by applying the baseline model set.

242 3.3. Workflow reports

243 Snakemake reports are generated in the form of static web-pages, which
244 are easily deployed and shared on a web-server. CI/CD mechanisms for
245 the workflow execution allow deploying reports onto web-servers as soon as
246 a certain job has finished making results instantly accessible to the whole
247 research team. A demonstration of the final workflow report via screenshots
248 is presented in Evdokimov et al. [49]. A side panel lists all cases simulated,

249 which upon selection will show the corresponding validation plots on the
250 main page for inspection. For further illustration purposes we refer to the
251 demonstration report provided by the Snakemake library on a public web-
252 page [51]. This report gives an impression of the typical report structure for
253 results.

254 The Snakemake workflow gives us an efficient tool to produce a large
255 amount of plots and to represent them in a well-structured report. The
256 evaluation of these reports for the baseline model development remains the
257 task of the user, but can be supported by artificial intelligence tools, such as
258 the fuzzy logic controller described in the next section.

259 **4. Evaluation of results**

260 The decision whether or not a computed *simulation* result is better than
 261 the *baseline* reference solution can be quite easy to make, such as in the plot
 262 illustrated on the left hand side of Figure 2, or it can be less obvious, such
 263 as the example on the right hand side.

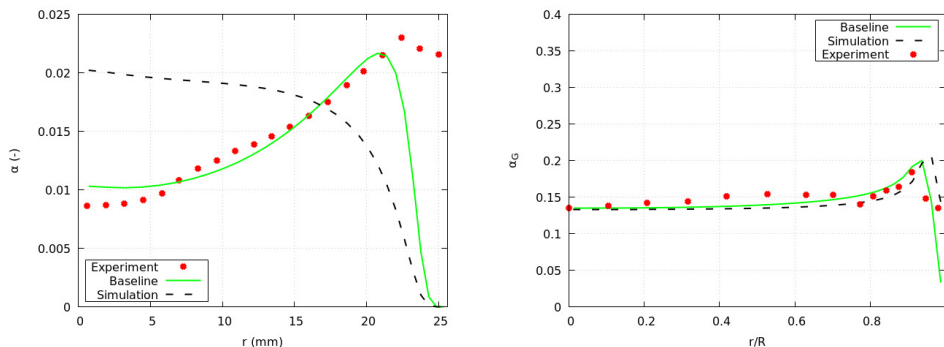


Figure 2: Gas void fraction profiles of fullyDeveloped_39 (left) and case L11A (right).

264 Fuzzy logic is a subset of artificial intelligence, which can accommodate
 265 the imprecision of the real world and support such a decision-making process.
 266 By using linguistic variables fuzzy logic can deal with imprecise, vague and
 267 uncertain information and approximate human reasoning.

268 The `scikit-fuzzy` library ([52], [53]) allows the integration of such fuzzy
 269 logic tools into our workflow, where it can be utilized for the testing of new
 270 models. From the system design point of view the library takes responsibility
 271 for the correct and robust implementation of the underlying algebra and the
 272 numerical algorithms, while on the top level we investigate metrics and their
 273 value boundaries suitable to our multiphase CFD problems. In essence, we
 274 propose a *fuzzy logic controller* for the purpose of evaluating and comparing
 275 CFD results. In the next sections we briefly describe how this controller
 276 works.

277 *4.1. The fuzzy logic system*

278 Fuzzy logic uses a specific terminology, which is briefly introduced here
 279 for a better understanding of the following sections. When a value is re-
 280 ferred to as being crisp this means it is explicit and concise. *Fuzzification*
 281 is the process of decomposing such crisp values into a spectrum of different

282 linguistic categories, referred to as fuzzy sets. A typical fuzzy logic system
 283 is illustrated in Figure 3. The system consumes and *fuzzifies* several crisp
 284 inputs, which means numerical floating-point or integer values are *mapped*
 285 onto linguistic sets via *membership functions*. These *membership functions*
 286 are normalized and might be considered as weight-factors of the expert sys-
 287 tem. *Inference logic* combines the numerous *fuzzy input sets* via a set of
 288 rules to produce *fuzzy output sets*, which themselves represent linguistic sets.
 289 Finally, these output sets are summed up, *defuzzified* and mapped onto a
 290 single crisp output value.

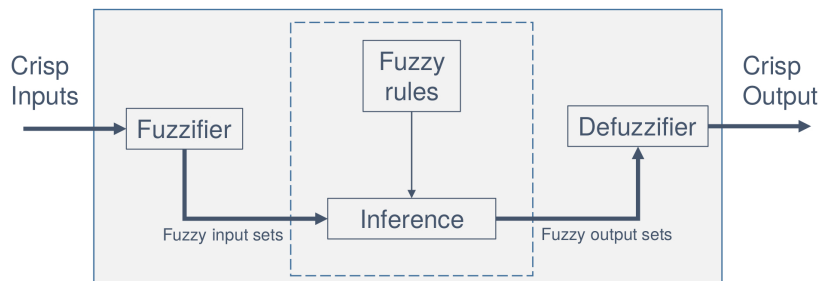


Figure 3: Schematic of a fuzzy logic system.

291 The inputs specified for the fuzzy system demonstrated here are two error
 292 metrics that will be described in the next section. One of the advantages of
 293 the fuzzy logic approach lies in its modularity allowing us to extend this
 294 list of fuzzy input variables in the future. In our case the desired output
 295 of the fuzzy logic system is a value between 0 and 1 quantifying how good
 296 the computed CFD result agrees with the measured validation data. We will
 297 refer to this crisp output as **goodness-value** G of the CFD prediction.

298 4.2. The crisp inputs: error metrics

299 The crisp inputs for our fuzzy logic system are specific error metrics that
 300 describe the similarity of two curves: our computed result, such as the gas
 301 void fraction profile, and the corresponding experimental data for validation.
 302 Various metrics could be used, but for demonstration purposes the number
 303 here is limited to two, which complement each other. The error metrics below
 304 are defined using the example of evaluating sorted sets of gas void fraction
 305 data. Hereby, the sorted set represents the radial profile in case of round

306 geometries or the lateral profile in case of rectangular columns. Metrics for
 307 the other validation fields are computed accordingly.

308 As a quantitative measure the **Mean relative error MRE** is defined
 309 as:

$$\text{MRE} = \frac{1}{N} \sum_{n=1}^N \frac{|\alpha_{n,sim} - \alpha_{n,exp}|}{\bar{\alpha}_{exp}} \quad (1)$$

310 with N being the number of values, the computed values of the gas void
 311 fraction α_{sim} and the experimentally measured ones α_{exp} , and $\bar{\alpha}$ the arith-
 312 metic average. The MRE describes the quantitative distance between two
 313 curves along the ordinate. It is normalized by the mean experimental value
 314 for the entire profile in order to avoid a heavier penalty of discrepancies for
 315 data points with smaller experimental values. Possible values for the MRE
 316 range from 0 to ∞ . We therefore limit values to a maximum of 1. Note that
 317 a case with a $\text{MRE} > 1$ therefore will not receive a heavier penalty than cases
 318 with a $\text{MRE} = 1$. Most cases in our collection, however, fall into the range
 319 of $0 < \text{MRE} < 1$.

320 As a qualitative measure the **Pearson correlation coefficient PCC** is
 321 defined as the covariance of the two gas void fraction data sets divided by
 322 the product of their standard deviation:

$$\text{PCC} = \frac{\sum_{n=1}^N (\alpha_{n,sim} - \bar{\alpha}_{sim})(\alpha_{n,exp} - \bar{\alpha}_{exp})}{\sqrt{\sum_{n=1}^N (\alpha_{n,sim} - \bar{\alpha}_{sim})^2} \sqrt{\sum_{n=1}^N (\alpha_{n,exp} - \bar{\alpha}_{exp})^2}} \quad (2)$$

323 The Pearson correlation coefficient determines the similarity of the two
 324 data sets, i.e. the shapes of the two curves. The range of the Pearson
 325 coefficient is $-1 < \text{PCC} < 1$. Examples of PCC values are illustrated in
 326 Figure 4, where simulation profiles are compared with experimental data. A
 327 negative coefficient indicates a negative linear correlation and a low similarity
 328 between curves, such as in the case of a predicted wall peak for a measured
 329 core peak profile. A positive coefficient represents a positive linear correlation
 330 of the data set meaning a high similarity of shapes, as illustrated for the
 331 almost matching profiles on the right hand side.

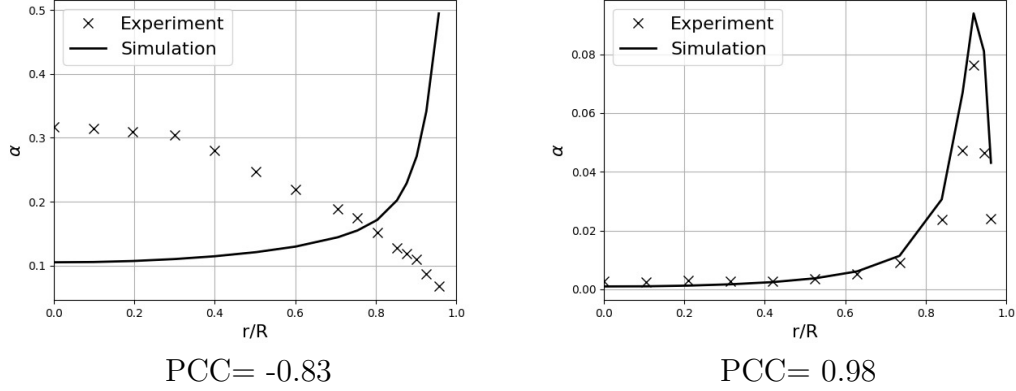


Figure 4: Pearson correlation coefficients computed for different data sets of gas void fraction profiles.

332 The PCC criteria is not sensitive to shifts of the profiles along the or-
 333 dinate, but sensitive to shifts along the abscissa. Thus, it complements the
 334 MRE metric, which is mainly sensitive to shifts along the ordinate.

335 *4.3. Membership functions*

336 A fuzzy set of linguistic terms is assigned to each input and output metric
 337 as illustrated in Table 3. The process of turning crisp variables into linguistic
 338 sets is termed *fuzzification*.

Table 3: Linguistic sets assigned to each variable.

Variable	Linguistic sets	Parameters a,b,c
MRE	"low"	0, 0, 0.3
	"medium"	0, 0.3, 1.0
	"high"	0.3, 1.0, 1.0
PCC	"high"	0.4, 1.0, 1.0
	"medium"	-1.0, 0.4, 1.0
	"low"	-1.0, -1.0, 0.4
G	"perfect"	0.7, 1.0, 1.0
	"good"	0.5, 0.7, 0.9
	"tolerable"	0.3, 0.5, 0.7
	"bad"	0.1, 0.3, 0.5
	"defect"	0.0, 0.0, 0.3

339 Membership functions $\mu_i(x)$ tie the input and output variables x for each
 340 linguistic set item i of the above table to a number, which can be understood
 341 as an impact value. Piece-wise *triangle* functions are used:

$$\mu_i(x) = \begin{cases} 0 & x \leq a \\ \frac{x-a}{b-a} & a \leq x \leq b \\ \frac{c-x}{c-b} & b \leq x \leq c \\ 0 & c \leq x \end{cases} \quad (3)$$

342 with parameters a , b and c specified separately for each item of the set
 343 as listed in Table 3. The triangle-shaped membership functions assigned to
 344 the linguistic terms listed in Table 3 are illustrated in Figure 5.

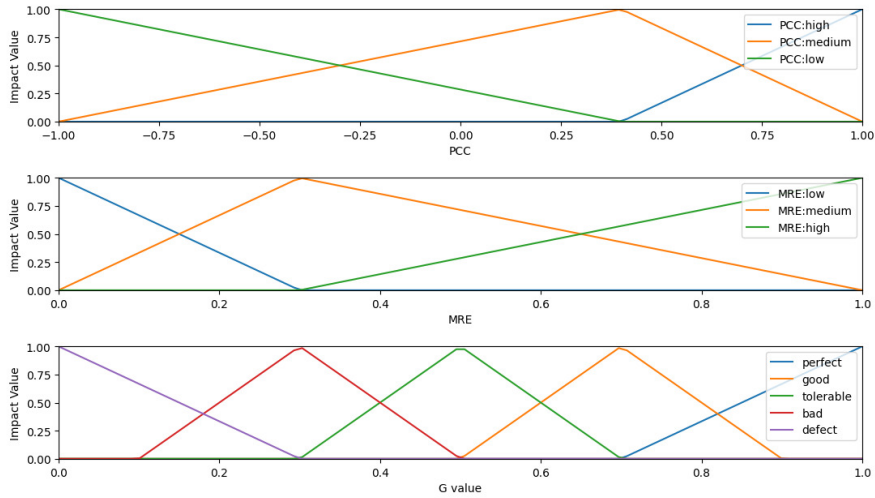


Figure 5: Membership functions for the fuzzy input and output sets. The x axis represents the crisp value space, the y value represents the membership function output value for each linguistic term.

345 For a specific metric value the membership function output represents
 346 a fuzzy degree of membership in the qualifying linguistic set. Thus, value
 347 intervals are constrained to a uniform range from zero to one for all input
 348 and output metrics, and the fuzzy set is *normalized*. For a crisp value x a
 349 fuzzy set now is defined as a pair:

$$A(x) = (i, \mu_i(x)) \quad (4)$$

350 where item i is a linguistic term and $\mu_i(x)$ the membership function ex-
351 pressing the degree of membership in that term.

352 4.4. Fuzzy rule base

353 Operations can be defined on the various fuzzy sets by means of their
354 membership function. This allows us to prescribe an intuitive rule base,
355 which is easy to interpret.

356 The current workflow evaluation consists of the following five rules:

- 357 1. If PCC:low AND MRE:high \rightarrow Defect G
- 358 2. If (PCC:low AND MRE:medium) OR (PCC:medium AND MRE:high) \rightarrow
359 Bad G
- 360 3. If (PCC:medium AND MRE:medium)
361 OR (PCC:high AND MRE:high)
362 OR (PCC:low AND MRE:low) \rightarrow Tolerable G
- 363 4. If (PCC:high AND MRE:medium) OR (PCC:medium AND MRE:low) \rightarrow
364 Good G
- 365 5. If PCC:high AND MRE:low \rightarrow Perfect G

366 A simplified visual representation for the target "Goodness" metric G is
367 illustrated in Figure 6.

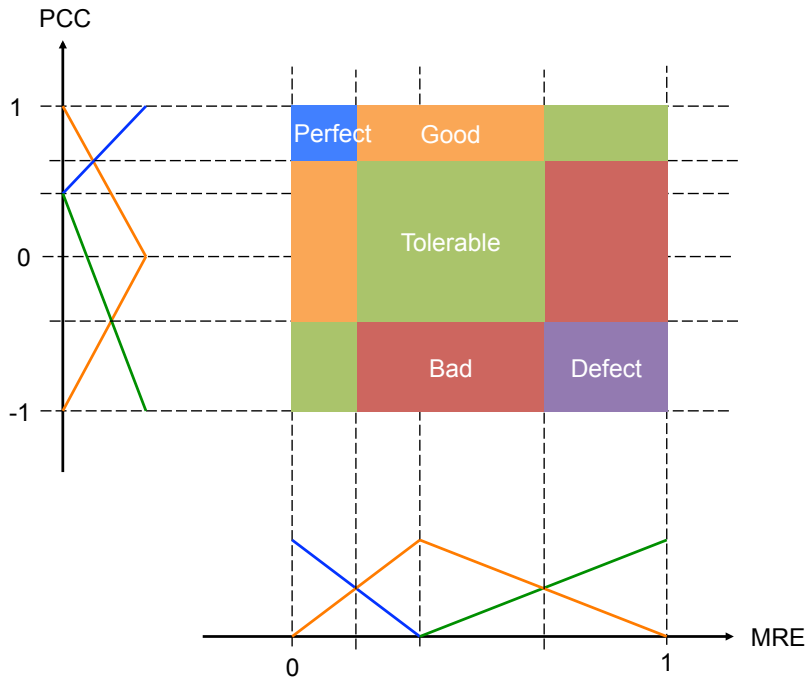


Figure 6: A schematic view of the relationship between the fuzzy input metrics and the output metric G .

368 Fuzzy operators are applied to obtain one value representing the result
 369 of each rule. Logical *min/max* operators correspond to the AND/OR rules
 370 mentioned above [54]. Input for these operators are the membership values
 371 of the fuzzified input variables, and the output is a single value.

372 An example is illustrated in Figure 7 for a case with $PCC = 0.49$ and
 373 $MRE = 0.36$. A single fuzzy rule, rule 4 for the fuzzy set *Good* of the
 374 G metric, is exemplified. The condition (PCC:high AND MRE:medium) OR
 375 (PCC:medium AND MRE:low) can be translated into $\max(\min(0.15, 0.91),$
 376 $\min(0.85, 0)) = 0.15$. This output is used for the implication of the fuzzy
 377 rule as described in the next section.

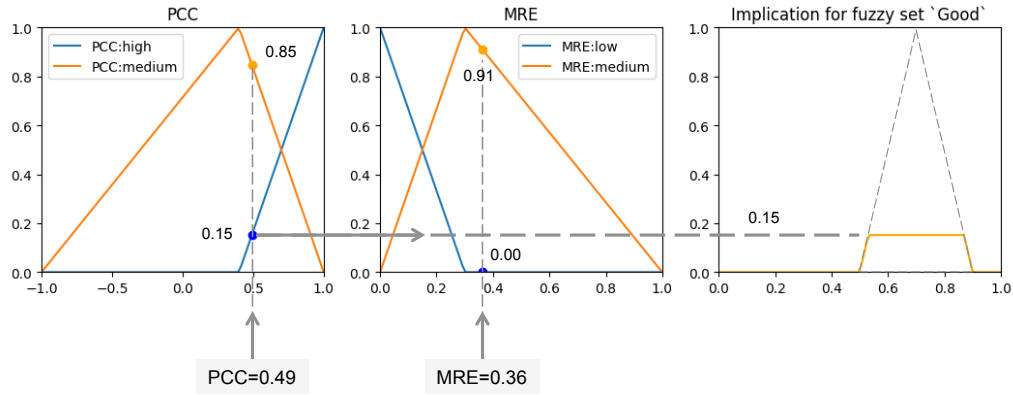


Figure 7: Application of rule 4 via fuzzy operators for an example of two input metrics.

378 *4.5. Implication and defuzzification*

379 An implication method turns the single output value into the consequence
 380 of the fuzzy rule. The consequent fuzzy sets are represented by the member-
 381 ship functions of the output sets. Input for the implication method is the
 382 value outputs given by each of the antecedent rules, such as rule 4 above.

383 Mamdani-type inference was applied for the implication process as it is an
 384 intuitive method, well-suited to human input, allowing an interpretable rule
 385 base and with widespread acceptance [54]. It works with the *min* implication
 386 operator to infer the output functions, as it is illustrated for rule 4 on the right
 387 hand side of Figure 7. The five fuzzy rules produce the output functions for
 388 the five potential sets of the goodness variable. Figure 8 illustrates the whole
 389 inference process for the above example with $PCC = 0.49$ and $MRE = 0.36$.
 390 In the example only three out of five output sets qualify during the inference
 391 step.

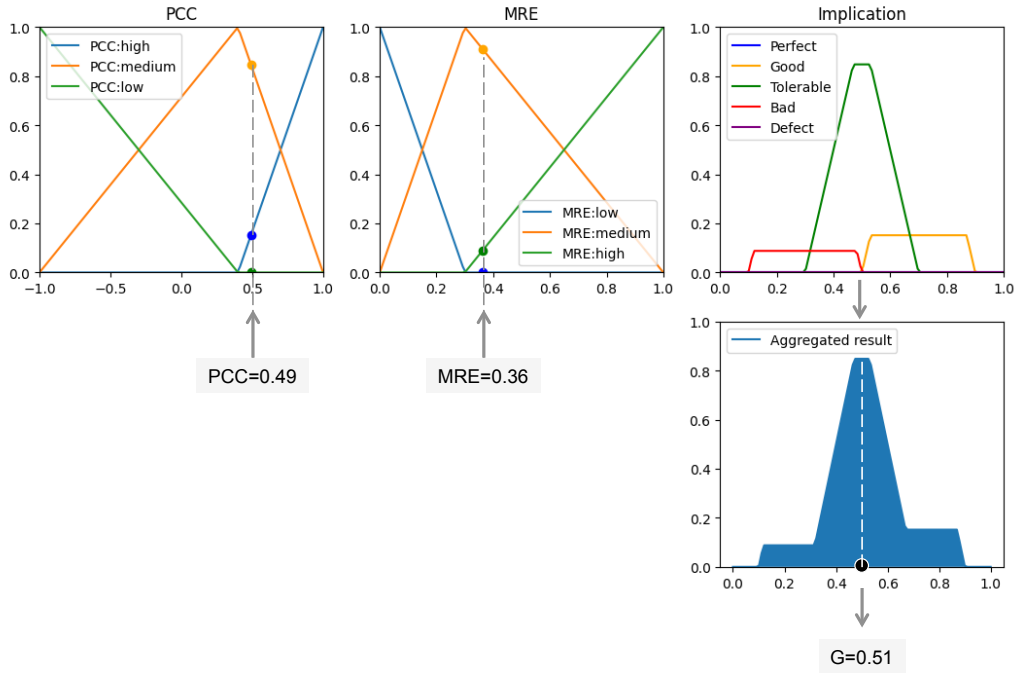


Figure 8: Inference system including all rules for an example of two input metrics.

392 The consequent functions of all rules then need to be aggregated, which
 393 is done by a simple *max* function. In a last step the aggregated function is
 394 defuzzified. The `scikit-fuzzy` library allows to choose from several meth-
 395 ods suggesting different trade-offs between the smoothness of the response
 396 surface and the robustness of the final defuzzification step. In the model
 397 evaluation attempted here we tried to track the smallest variations to allow
 398 a continuous differentiation of results. Therefore, our chosen defuzzification
 399 method relies on area measurements of the aggregated result. Defuzzification
 400 is performed by the *bisector* method, which finds the vertical line that di-
 401 vides the aggregated result into two sub-regions of equal area. The response
 402 surface of our current two-input, one-output, five-rule fuzzy logic system is
 403 illustrated in Figure 9.

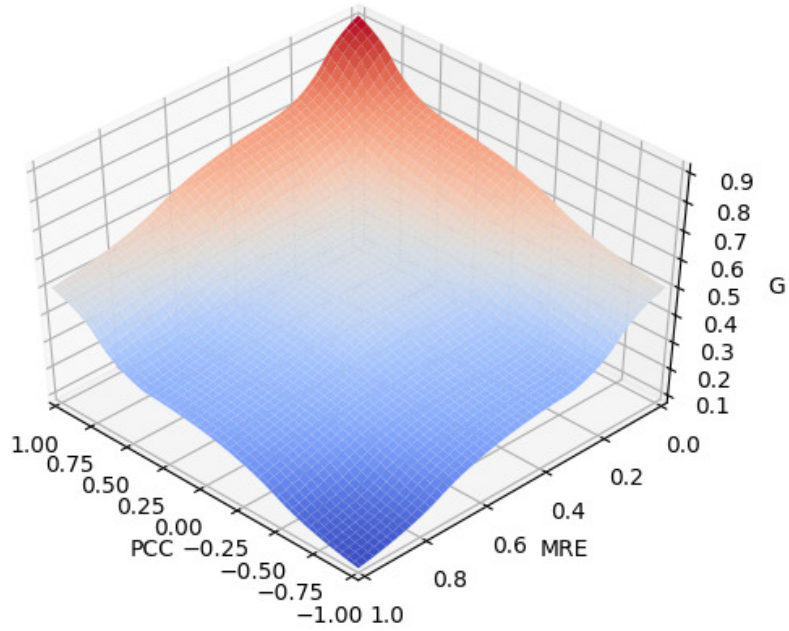


Figure 9: Response surface of the fuzzy logic system.

404 *4.6. Evaluation for the case collection*

405 The fuzzy logic approach offers a convenient framework for an evaluation
 406 algorithm, which could be easily repurposed, extended and redefined. The
 407 alternative usage of an equivalent multidimensional target function requires
 408 the strict definition of potentially controversial input values fitting a specific
 409 output metric. Fuzzy logic makes it easy to reach a consensus amongst re-
 410 searchers by using relations between linguistic sets derived from these values.
 411 Errors divided into a *low*, *medium* and *high* subset are easily agreed on, but
 412 certain values fitting these sets are not.

413 As described above for each case in the case collection several fields are
 414 investigated for the validation of the CFD results, e.g. gas void fractions or
 415 velocity profiles. A goodness value G is computed for each of those individual
 416 validation fields and is meant to describe how good the predicted profile
 417 agrees with the experimental data.

418 The average over all these individual goodness values for the available
419 validation fields produces a single value for each case. This single value rep-
420 represents the overall goodness of the CFD prediction for the case investigated.
421 In the future different weightings for the various validation fields could be
422 considered.

423 When testing a new model the above procedure is done twice, for the
424 results using the new model and for the reference solution obtained with the
425 baseline model set. An improvement or deterioration of the CFD results for a
426 specific case can then be expressed via the difference in the overall goodness
427 of the computed and the baseline result.

428 **5. Demonstration case: Testing a new lift force correlation**

429 To demonstrate the efficiency of the baseline workflow and its fuzzy logic
 430 tool, this section will now investigate results when testing a new lift force
 431 correlation. We will refer to the results obtained with the Tomiyama correla-
 432 tion [17] as *baseline* results, and the results with a new correlation for the lift
 433 coefficient proposed by Hessenkemper et al. [55] as *computed* results. This
 434 section does not aim to validate the new correlation, but to demonstrate the
 435 benefits and future potential of the developed workflow tools in assisting the
 436 baseline model development.

437 We will give an impression of the performance and reporting features of
 438 the workflow when analysing a certain selection of cases. The evaluation of
 439 results via fuzzy logic will then be verified for a selected case. Finally, an
 440 overview of the overall goodness evaluation for all cases is presented.

441 *5.1. Workflow performance*

442 For the following analysis we restrict our selection of repository cases to
 443 the ones that have already been published elsewhere, as listed in Table 4. The
 444 individual case setups in OpenFOAM are described in the references given,
 445 and are to be found in the *HZDR Multiphase Case Collection for OpenFOAM*
 446 [56]. Including all sub-cases the total number of cases investigated here is 36.
 447 The simulation of each individual sub-case demands three to eight processors
 448 and an execution time of up to two hours.

Table 4: List of cases for the workflow demonstration.

Experimental reference	Cases	Setup	CPUs/Case
Hosokawa and Tomiyama [57]	4	[58]	4
Liu [59]	4	[58], [60]	4
Shawkat et al. [61]	4	[60]	4
Hosokawa and Tomiyama [62]	4	[60], [63]	8
Kim et al. [64]	4	[63]	8
Lucas et al. [50]	16	[65]	3

449 The Snakemake workflow processes all these cases with a total execution
 450 time of ~ 5 h (the entire case collection takes ~ 10 h). A total of 236 plots
 451 (baseline relevant and auxiliary) is generated automatically. In the plots
 452 relevant for the baseline evaluation the computed results are compared to

453 both the experimental data and the reference solution. Examples of such
454 plots are illustrated in Figure 2. The fuzzy logic evaluation of these results
455 during the optional post-processing step is done with an execution time of
456 only four minutes.

457 5.2. Verification of the fuzzy logic output

458 For a single case this section will now analyse the computed results and
459 compare them with the error metrics and the goodness output computed by
460 the fuzzy logic system. Figure 10 illustrates the validation plots produced
461 for exemplary case L11A of Liu [59], and associated values of error metrics
462 and the G output metric.

463 The predicted gas void fraction profiles show a generally good shape,
464 both the baseline and the computed profile. This generally good agreement
465 with the experiment is well represented by high values of the PCC . The
466 result with the Hessenkemper lift appears slightly deteriorated due to a shift
467 of the wall peak towards the wall, which is well captured by a drop of the
468 respective PCC . There are no significant changes in MRE . The drop in
469 overall goodness and a negative ΔG reflect the subjective evaluation of the
470 gas void fraction profiles.

471 The profiles for the turbulent kinetic energy are examples of curves with
472 distinctively different shapes compared to the experimental data (wall-peak
473 vs. core-peak). This judgement is well captured by very low values for the
474 PCC , as well as very high values for the MRE . Comparing the baseline
475 result to the new model no significant changes are observed. Consequently,
476 the ΔG computed by the fuzzy logic system is relatively small.

477 The profiles for the liquid velocity show a good agreement with the exper-
478 iment in terms of the shape. The difference to the experimental data slightly
479 increases with the new model, as correctly captured by the MRE metric.

480 All the resulting G values of the validation fields are averaged to produce
481 one value for the overall goodness of the CFD predictions for the case. The
482 difference in results between the two lift force models is expressed by the
483 difference ΔG . For the L11A case the new lift model slightly decreases the
484 overall G and deteriorates results, which corresponds to our judgement for
485 the plots in Figure 10.

Validation plots	Metrics	Baseline	Simulation	ΔG
	MRE PCC G	0.089 0.701 0.713	0.091 0.349 0.651	 -0.062
	MRE PCC G	1.064 -0.933 0.095	0.962 -0.973 0.099	 0.004
	MRE PCC G	0.066 0.793 0.770	0.082 0.683 0.713	 -0.057
Overall G		0.526	0.487	-0.039

Figure 10: Goodness evaluation for the validation fields of case L11A.

486 *5.3. Overview of all case evaluations*

487 The above evaluation of results expressed via the G metric is performed
488 for each of the cases under investigation. Figure 11 illustrates the overall
489 goodness values of all cases, represented as bars ranging from zero to one.
490 Numbers next to each case indicate in green the cases which have improved,

491 and in red the deteriorated ones, such as L11A on the top. A ΔG value
 492 averaged over all cases aims to quantify the general trend in results. Thus,
 493 the plot allows to obtain a first overview of the general performance of a new
 494 model.

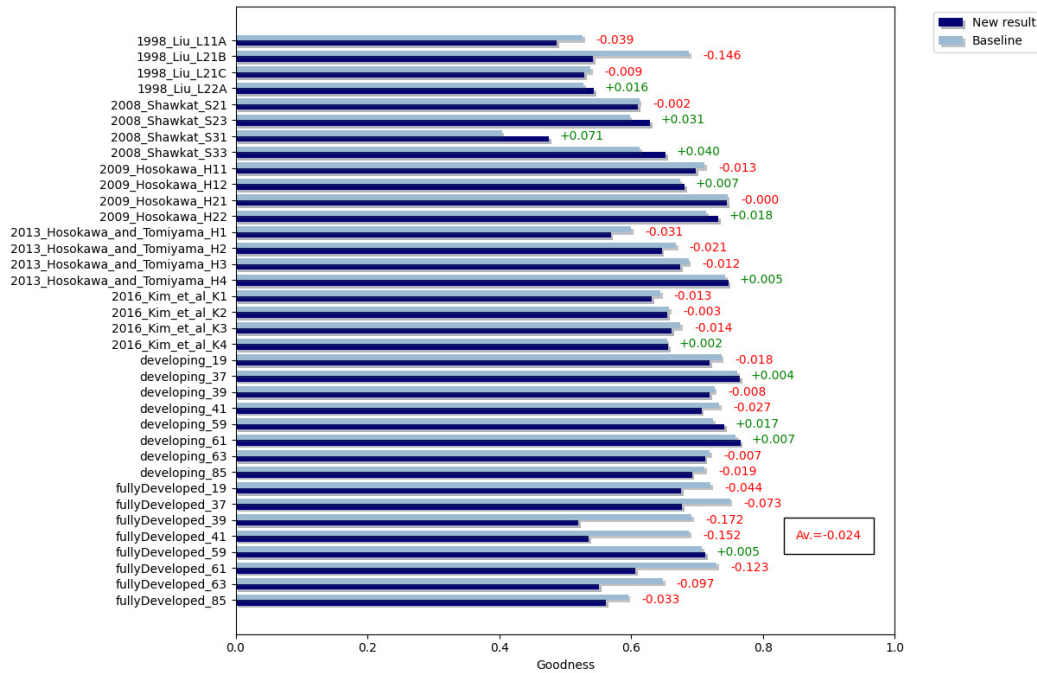


Figure 11: Plots for the overall goodness of all 36 demonstration cases. Light blue bars represent the reference solution obtained with the baseline lift model, deep blue bars the solution obtained with the new lift model. Numbers next to each case indicate the difference in overall goodness, with red indicating a deterioration and green an improvement of results.

495 Similar plots are produced for the individual validation fields, such as the
 496 gas void fraction plot presented in Figure 12. The goodness values are based
 497 on the computed mean relative errors and Pearson correlation coefficients
 498 illustrated in Figure 13.

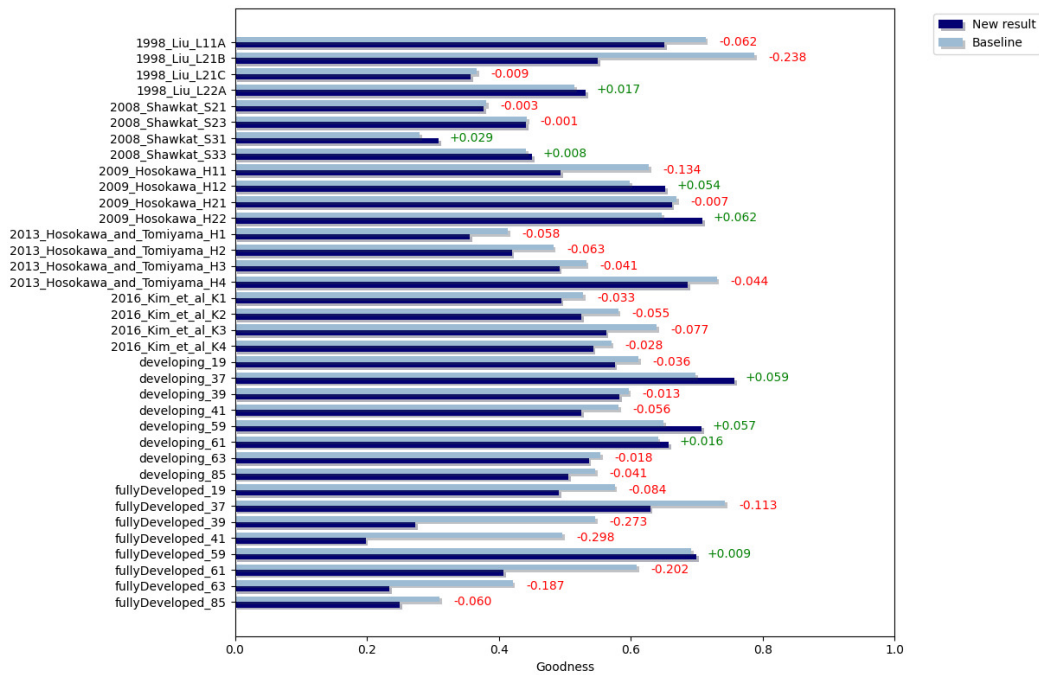


Figure 12: Goodness output for the gas void fraction prediction of all 36 demonstration cases.

499 Plots visualizing the change in goodness for each case, such as the ones
500 above, have proven to be a useful tool for analysing the performance of a new
501 model. Not only do they provide a neat case-by-case overview of results,
502 but also help pointing the researcher to the cases most affected by a new
503 model. Figure 12 indicates a slight change of gas void fraction results for
504 case L11A, but a more substantial change for case fullyDeveloped_39. This
505 is confirmed by the corresponding plots in Figure 2. Table 5 illustrates the
506 detailed input and output metrics for both cases, with the quality of CFD
507 predictions adequately quantified by the fuzzy logic system.

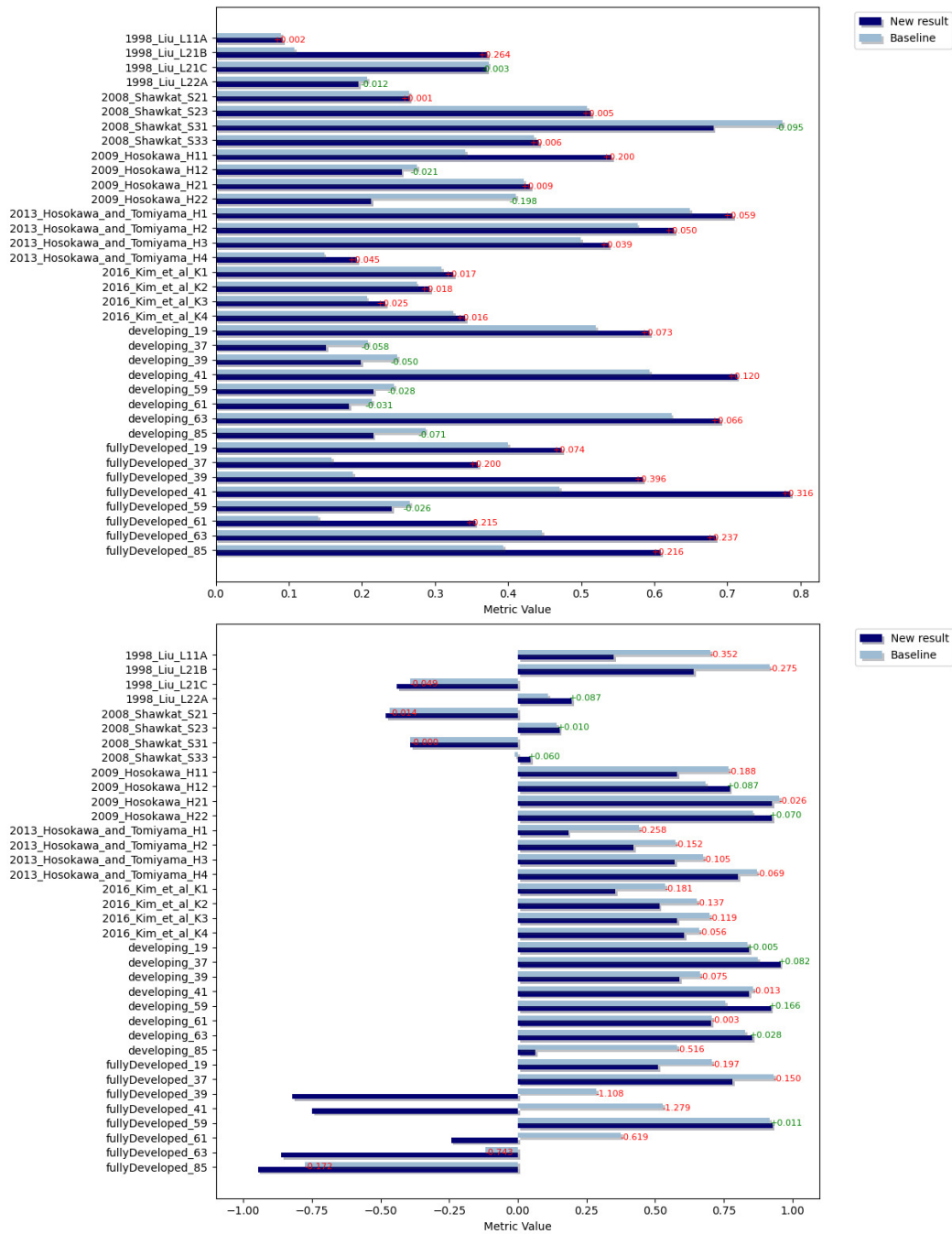


Figure 13: Computed error metrics for the gas void fraction prediction of all 36 demonstration cases. Top: Mean relative error. Bottom: Pearson correlation coefficient.

Table 5: Comparison of the computed fuzzy logic metrics for the gas void fraction profiles in Figure 2.

	fd_39	L11A
Baseline		
MRE	0.188	0.089
PCC	0.287	0.701
G	0.546	0.713
New model		
MRE	0.585	0.091
PCC	-0.822	0.349
G	0.273	0.651
ΔG	-0.273	-0.062

508 The presented fuzzy logic plots above are a powerful tool assisting in
 509 the model evaluation and comparison for the baseline model development
 510 using a large number of cases. Note, however, that results will not cease
 511 to require the careful interpretation by the experienced researcher taking
 512 into account the underlying physical phenomena. An obvious limitation of
 513 the current validation strategy is that bubbly flow cases typically require a
 514 set of interdependent closures rather than isolated, individual models. This
 515 means the computed error metrics and corresponding goodness evaluation
 516 is only able to demonstrate the accuracy of all closure models combined.
 517 How well each individual closure model performs remains a task of careful
 518 interpretation by the investigator.

519 For a more detailed analysis of a new closure model the researcher can
 520 facilitate the keywords presented in Table 2, which are assigned to each sub-

521 case. Via keyword selection during the configuration step of the workflow
522 the model analysis can be tailored to specific cases of interest with certain
523 features.

524 The fuzzy logic analysis demonstrated here constitutes a first step towards
525 a more automated model evaluation. In the future a more refined control of
526 the results is possible by introducing alternative and/or additional metrics.
527 Furthermore, core and near-wall regions could be analysed separately adopt-
528 ing different error metrics and fuzzy sets for these individual flow regions
529 if needed. The optimal use of fuzzy sets and metric combinations will be
530 determined by the expert community and will evolve by gaining experience
531 over time.

532 6. Conclusions

533 The development of closure models that can predict the behaviour of
534 multiphase flows continues to be a challenge due to the increasing number of
535 available model options, and their intricately-linked interactions. The base-
536 line strategy offers a way towards a more sustainable model development. By
537 setting the goal of establishing a fixed set of models and related model con-
538 stants it is turning away from case-specific tuning, and instead gives priority
539 to the generality and predictive capabilities of models. The practical imple-
540 mentation of such a strategy involves the continuous validation of a large
541 number of cases available in the literature, which continues to grow. Within
542 the last few years of baseline research the HZDR team has accumulated a
543 diverse set of such validation cases and built an extensive case collection.

544 We have presented here a Snakemake workflow that now allows the flexible
545 and fully-automated pre-processing, simulation and post-processing of all
546 these OpenFOAM cases at scale. The automated production of hundreds of
547 validation plots and their representation in a single, easily accessible web-
548 report allow an efficient analysis of our CFD results and their comparison to
549 the experimental validation data.

550 Such advanced case management enables us to integrate artificial intelli-
551 gence tools that assist in the analysis and evaluation of the extensive amount
552 of results. The work presented here introduces a fuzzy logic controller quan-
553 tifying the agreement of computed CFD results with the validation data.
554 By comparing new results with a reference solution obtained with the base-
555 line model set this fuzzy logic tool allows the systematic evaluation of new
556 Euler-Euler models. The testing of a new lift force correlation demonstrates
557 the potential of such an approach with comprehensive plots illustrating neat
558 case-by-case comparisons of the accuracy of the CFD predictions.

559 The further development of the fuzzy logic evaluation and its extension by
560 more input metrics is ongoing. A particular focus will be on metrics describ-
561 ing the convergence behaviour and runtime performance of cases to obtain
562 an alternative criteria by which to compare various Euler-Euler models. Fur-
563 thermore, the uncertainty of the validation data should be included into the
564 evaluation. The application of fuzzy logic is just one of many potential ways
565 of including data science tools into the baseline model development. Another
566 valuable area of further work is the integration of case-specific keywords into
567 the model evaluation for further categorisation, which suits various machine
568 learning algorithms.

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